

# **Standard Model (backgrounds) at the LHC**

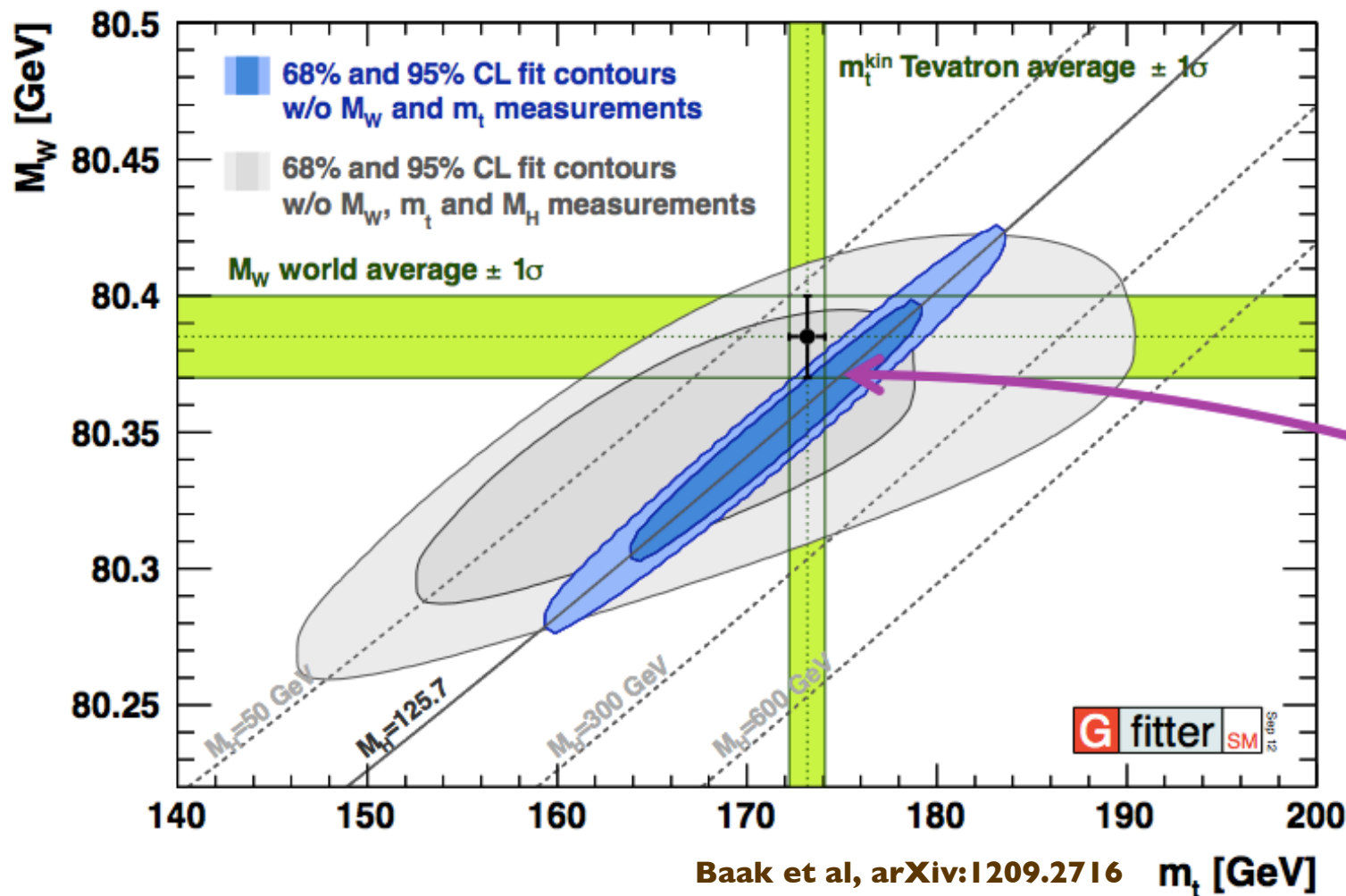
**(part 3)**

**Prospects in Theoretical Physics 2013**  
**Institute for Advanced Study, Princeton**  
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**Michelangelo L. Mangano**  
TH Unit, Physics Department, CERN  
[michelangelo.mangano@cern.ch](mailto:michelangelo.mangano@cern.ch)

# Top quark mass

# Top quark mass



**Direct measurements (Tevatron averages):**

$$m_{\text{top}} = 173.20 \pm 0.87 \text{ GeV}$$

$$m_W = 80385 \pm 15 \text{ MeV}$$

**New EW fit results for  $m_{\text{top}}$  ( $m_W$ ), including  $m_H$ , excluding the direct measurement of  $m_W$  ( $m_{\text{top}}$ ):**

$$m_{\text{top}} = 175.8^{+2.7}_{-2.4} \text{ GeV}$$

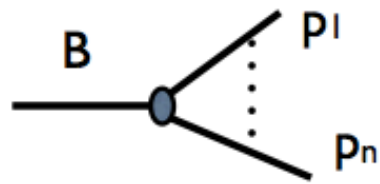
$$m_W = 80359 \pm 11 \text{ MeV}$$

**Inclusion of  $m_H$  in EW fits greatly tightens correlation between  $m_W$  and  $m_{\text{top}}$  introducing perhaps a slight tension ?**

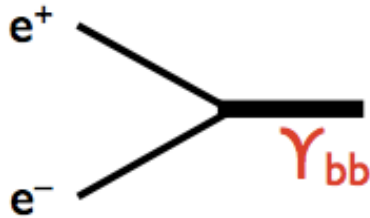
**Continued improvement in the direct determination of  $m_W$  and  $m_{\text{top}}$  remains a high priority**

# Measuring the mass of heavy quarks: b/c

## 1. measure mass of B-hadrons or $\Upsilon_{bb}$



$$m_B^2 = \left( \sum_{i=1, \dots, n} p_i \right)^2$$

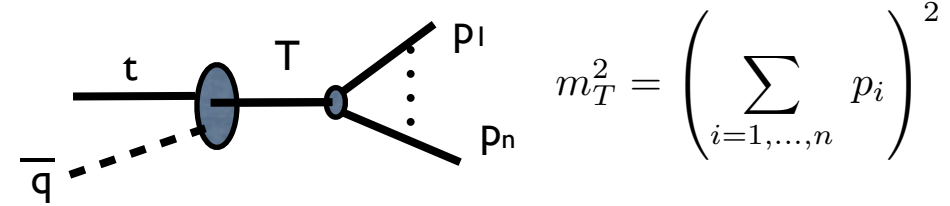


$$m_\Upsilon = \sqrt{s_{e^+e^-}}$$

## 2. $m_b = F_{\text{lattice/potential models}}(m_B, m_\Upsilon, \alpha_{\text{QCD}})$

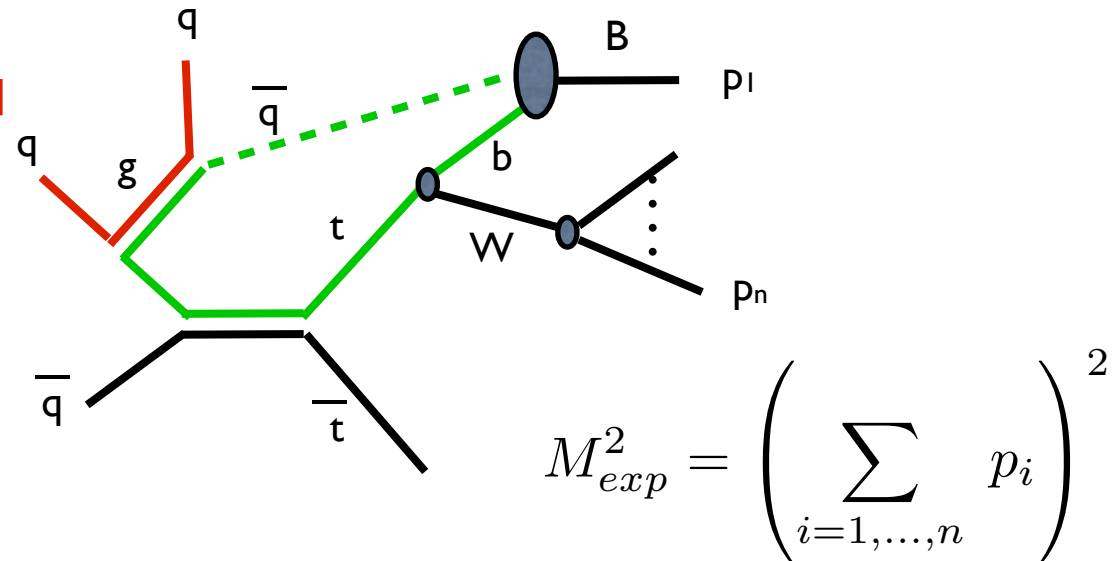
# Determination of $m_{\text{top}}$ in hadronic collisions

If  $\Gamma_{\text{top}}$  were  $< 1$  GeV, top would hadronize before decaying. Same as b-quark



$$m_t = F_{\text{lattice/potential models}}(m_T, \alpha_{\text{QCD}})$$

But  $\Gamma_{\text{top}}$  is  $> 1$  GeV, top decays before hadronizing. Extra antiquarks must be added to the top-quark decay final state in order to produce the physical state whose mass will be measured



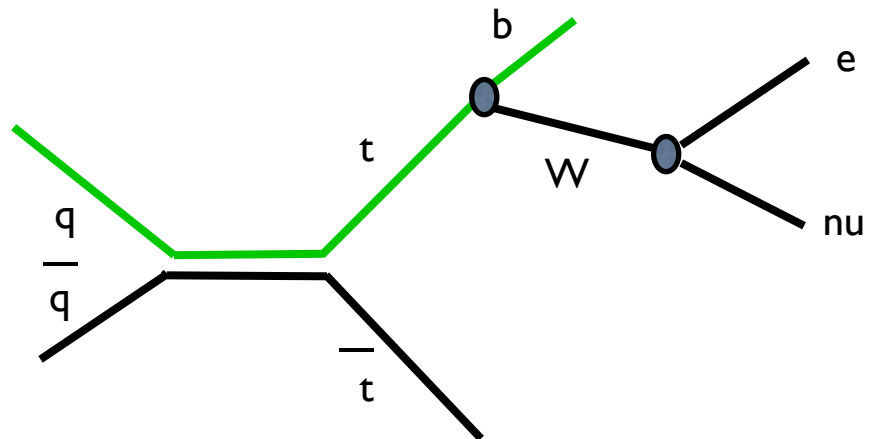
As a result,  $M_{\text{exp}}$  is not equal to  $m_{\text{top}}^{\text{pole}}$ , and will vary in each event, depending on the way the event has evolved.

The top mass extracted in hadron collisions is not well defined below a precision of  $O(\Gamma_{\text{top}}) \sim 1$  GeV

Goal:

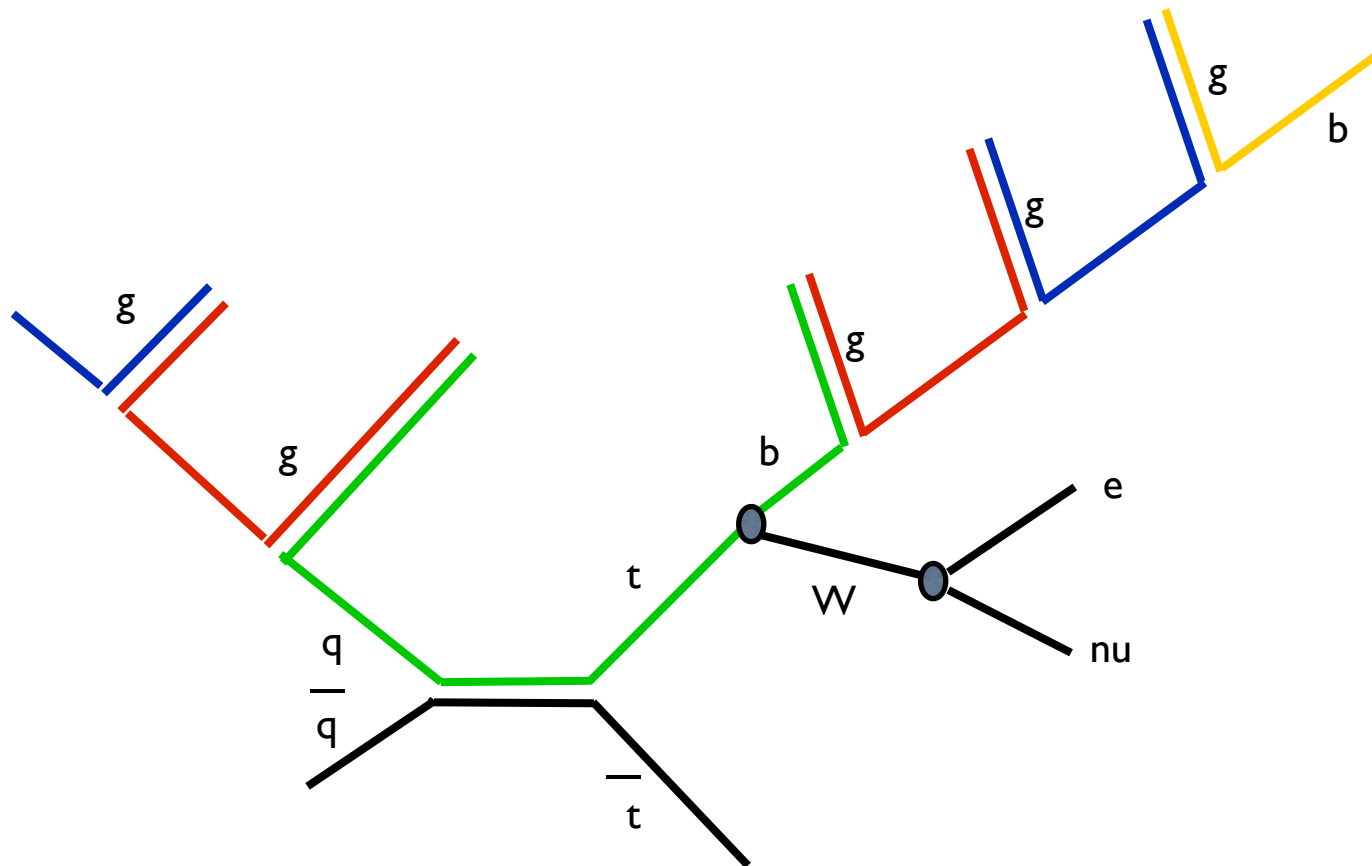
- correctly quantify the systematic uncertainty
- identify observables that allow to validate the theoretical modeling of hadronization in top decays
- identify observables less sensitive to these effects

# I. Hard Process



## 2. Shower evolution

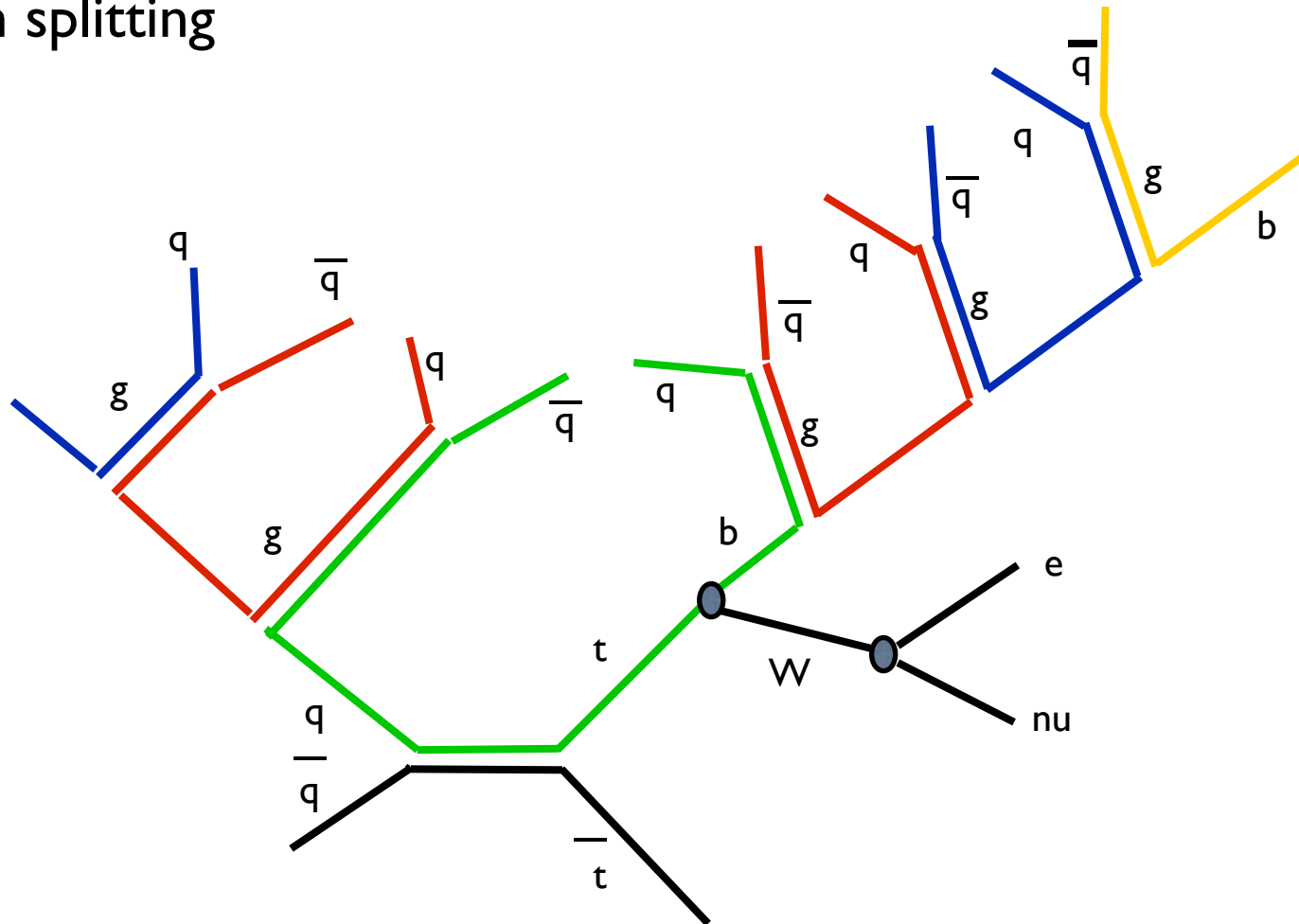
## 2. Shower evolution



1. Hard Process

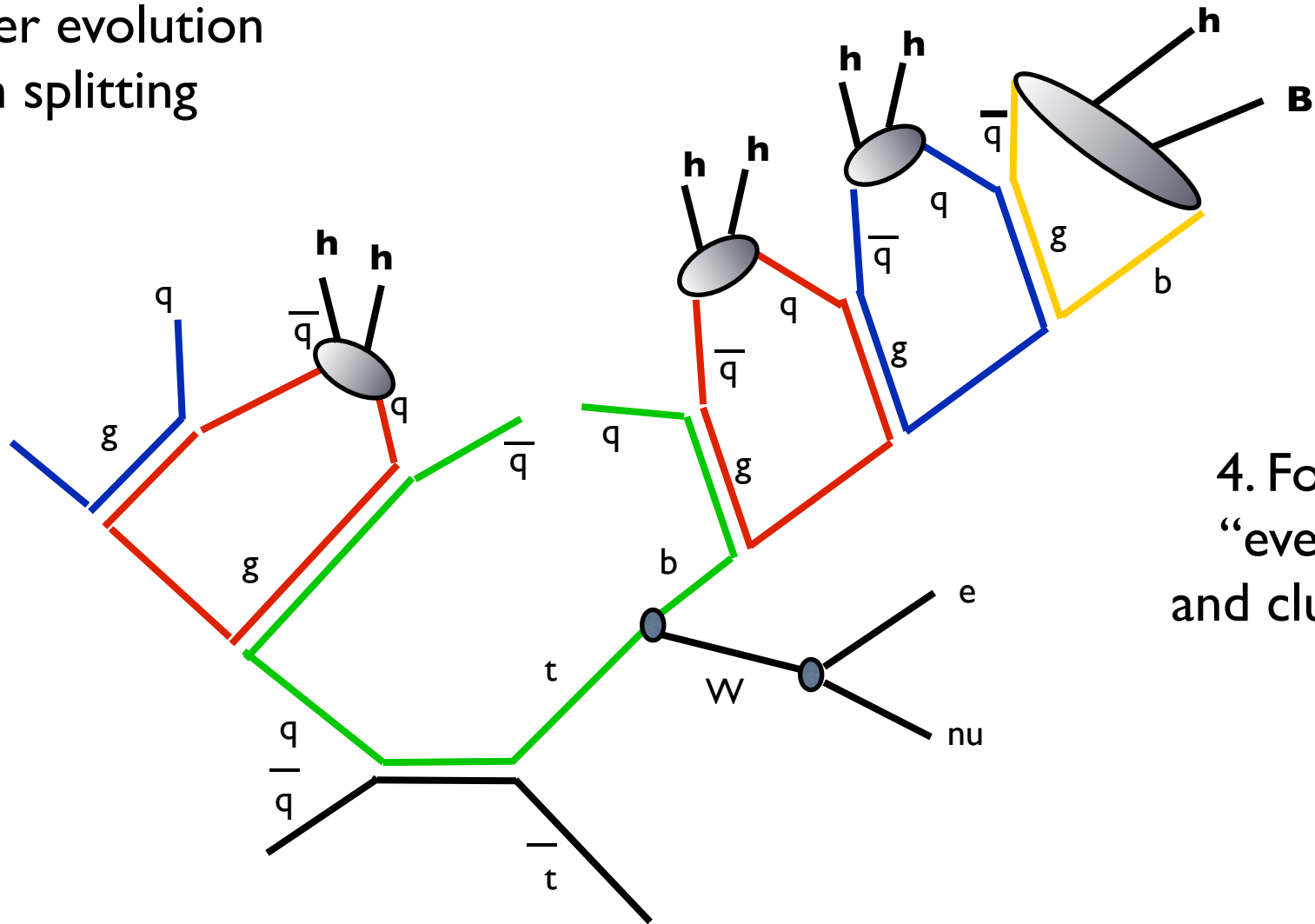
2. Shower evolution

3. Gluon splitting



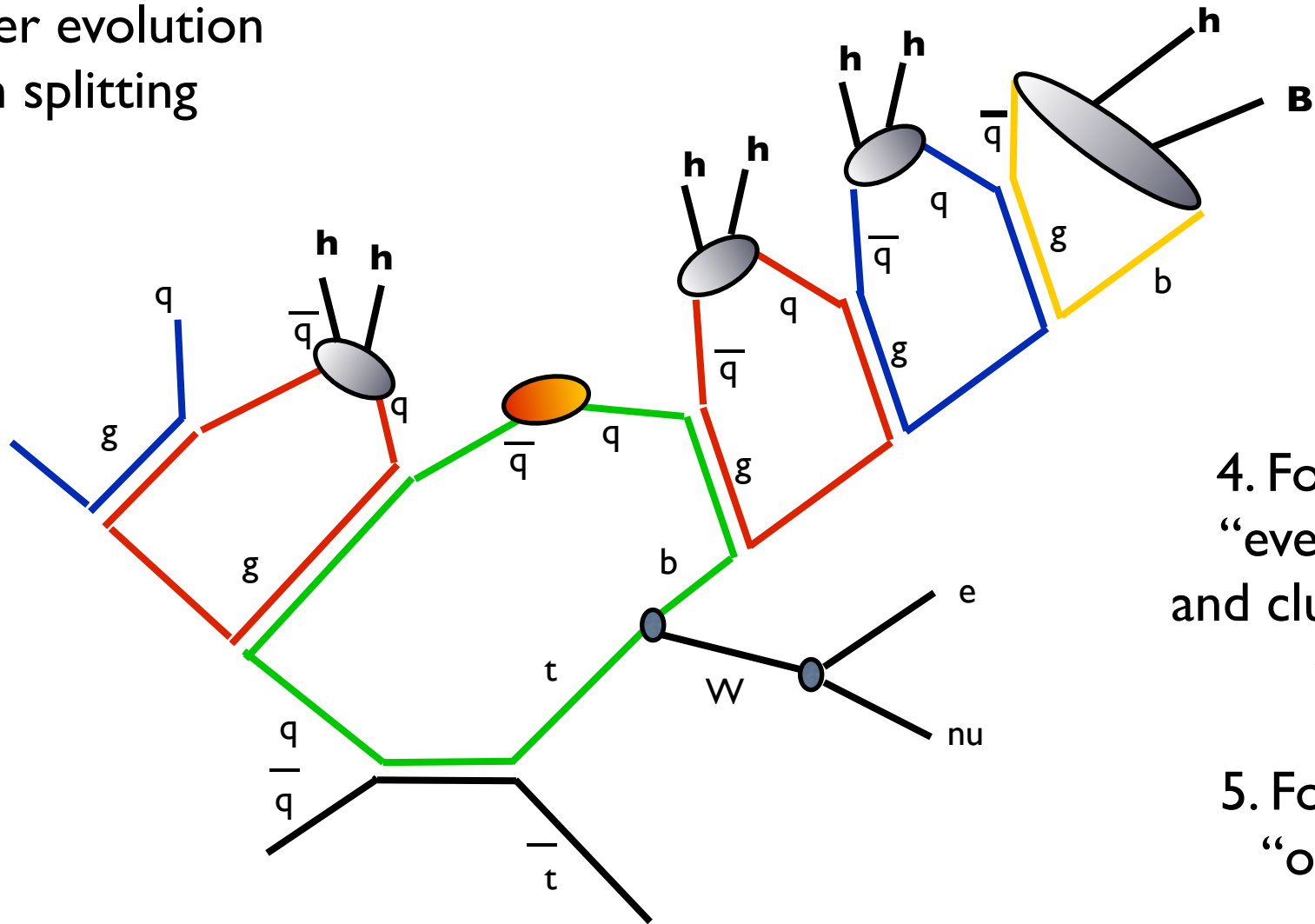


1. Hard Process
2. Shower evolution
3. Gluon splitting



4. Formation of "even" clusters and cluster decay to hadrons

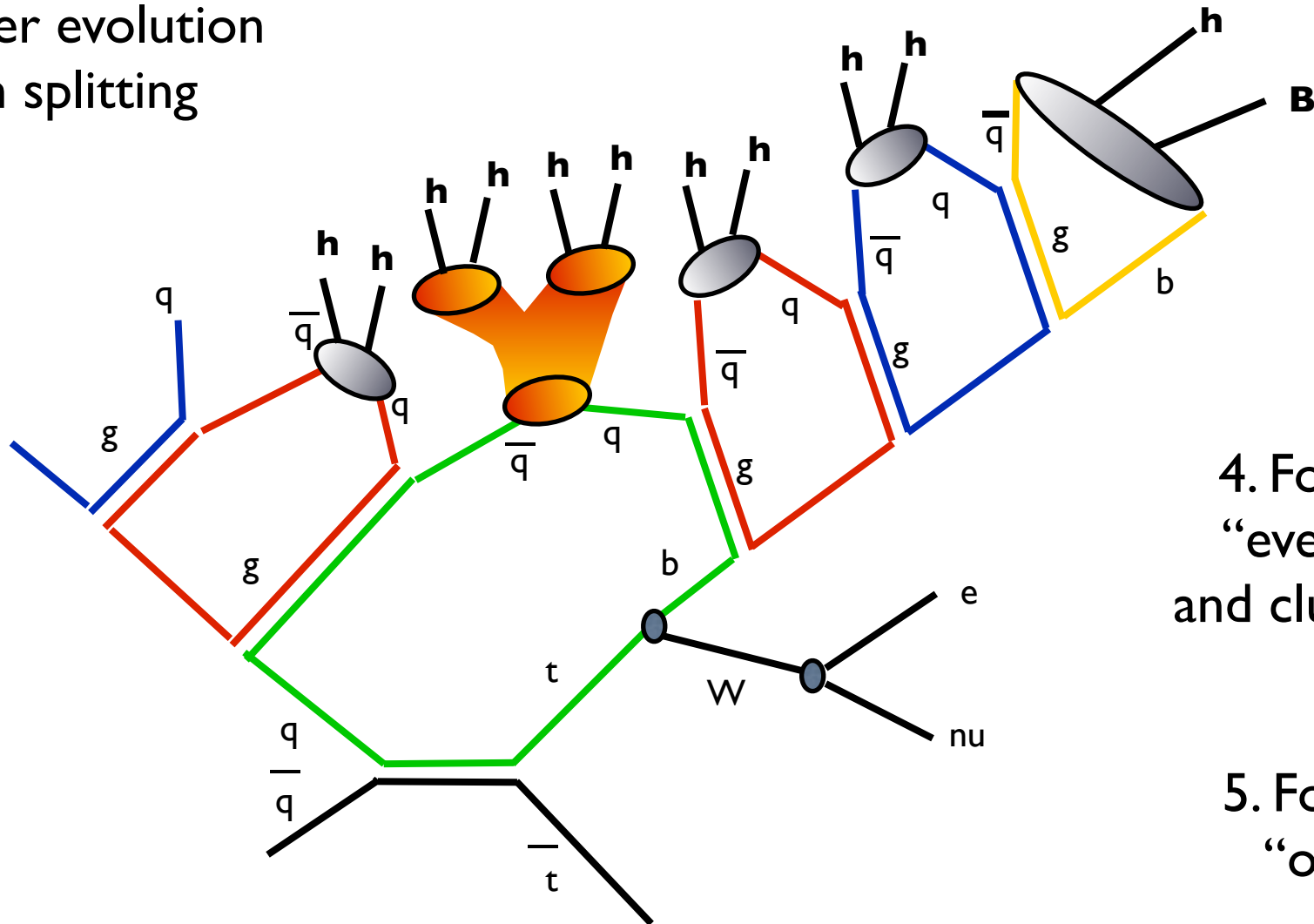
1. Hard Process
2. Shower evolution
3. Gluon splitting



4. Formation of  
"even" clusters  
and cluster decay  
to hadrons

5. Formation of  
"odd" cluster

1. Hard Process
2. Shower evolution
3. Gluon splitting

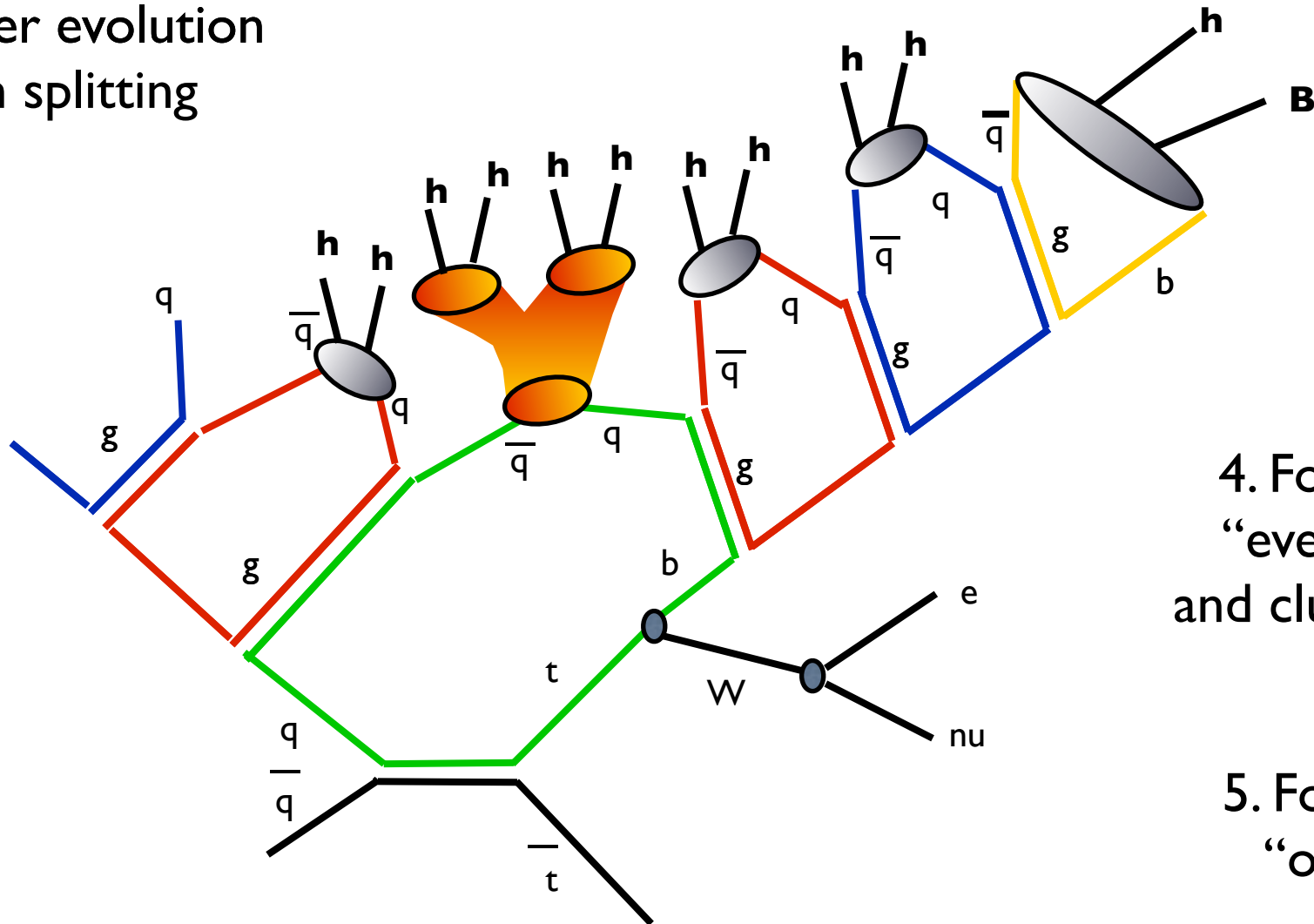


4. Formation of  
"even" clusters  
and cluster decay  
to hadrons

5. Formation of  
"odd" cluster

6. Decay of "odd" clusters, if  
large cluster mass, and decays  
to hadrons

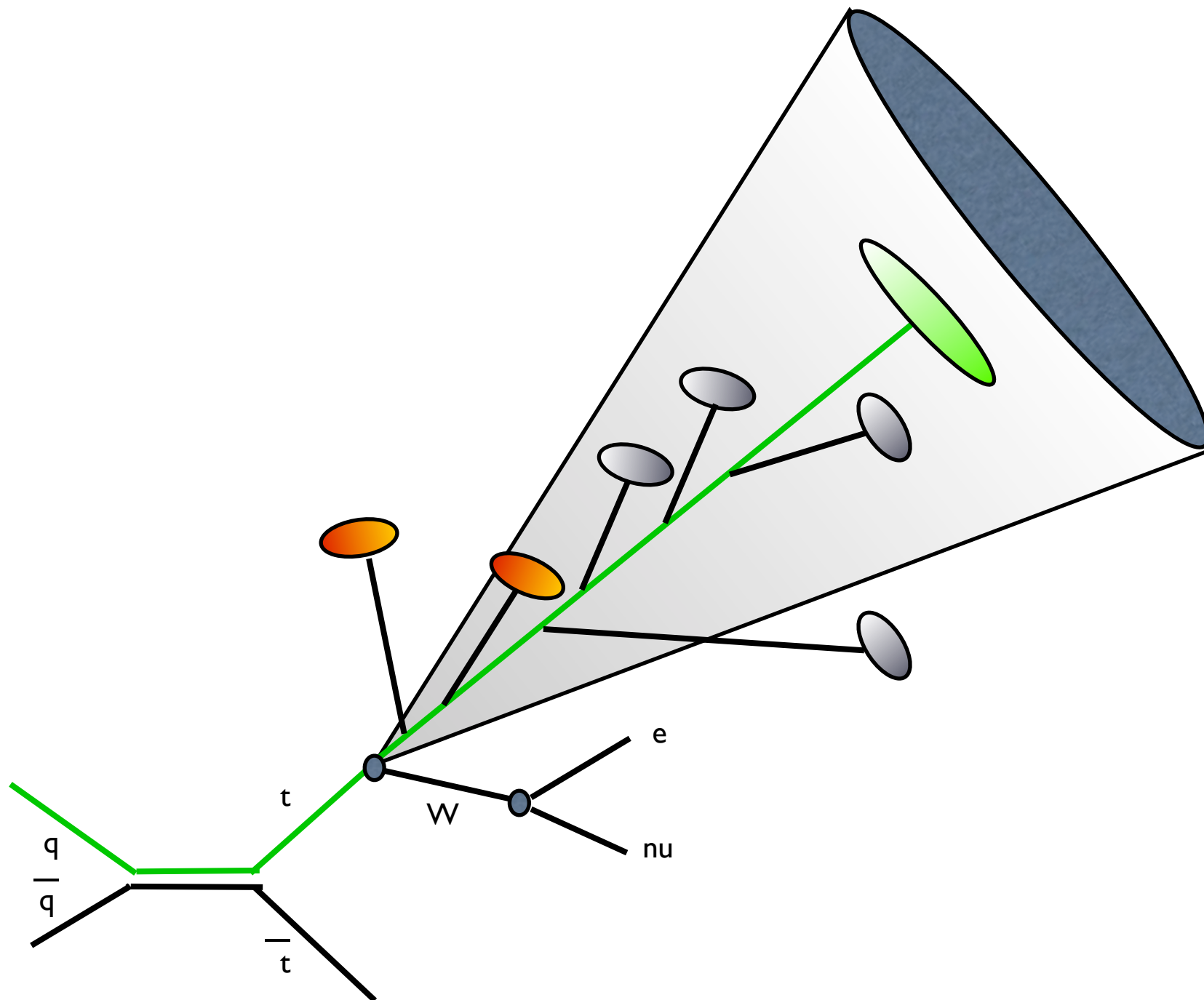
1. Hard Process
2. Shower evolution
3. Gluon splitting



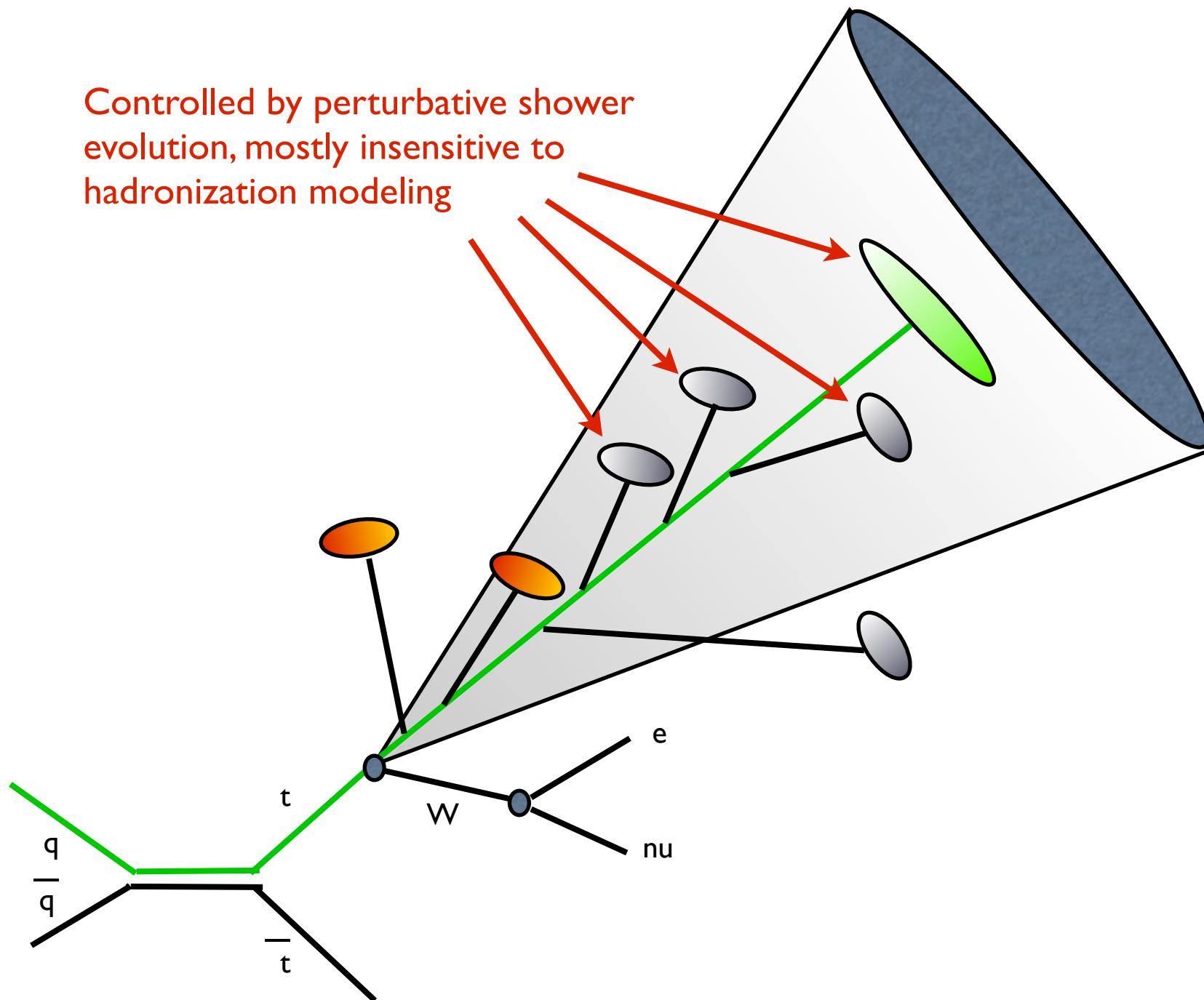
4. Formation of “even” clusters and cluster decay to hadrons

5. Formation of “odd” cluster

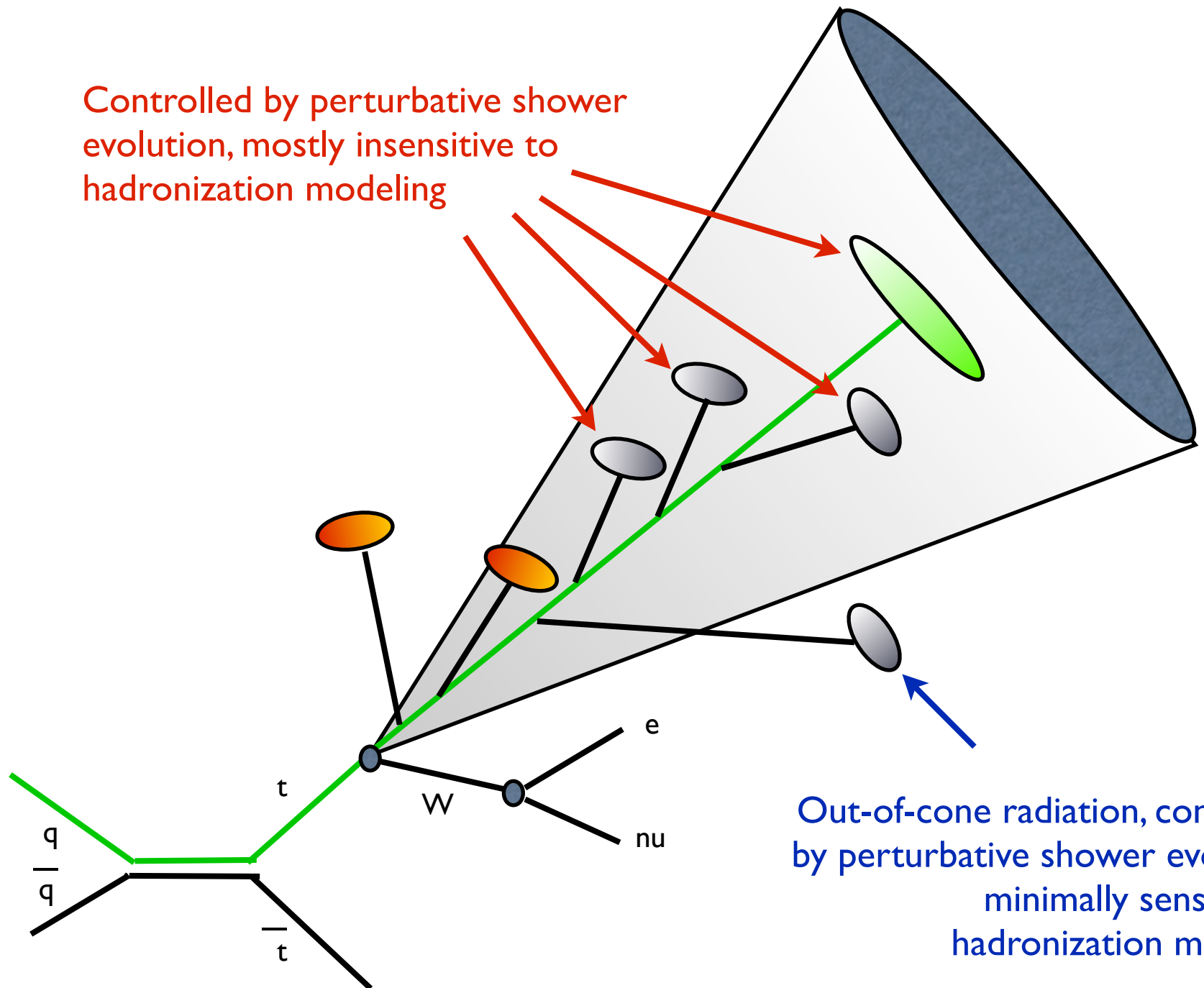
6. Decay of “odd” clusters, if large cluster mass, and decays to hadrons



Controlled by perturbative shower evolution, mostly insensitive to hadronization modeling



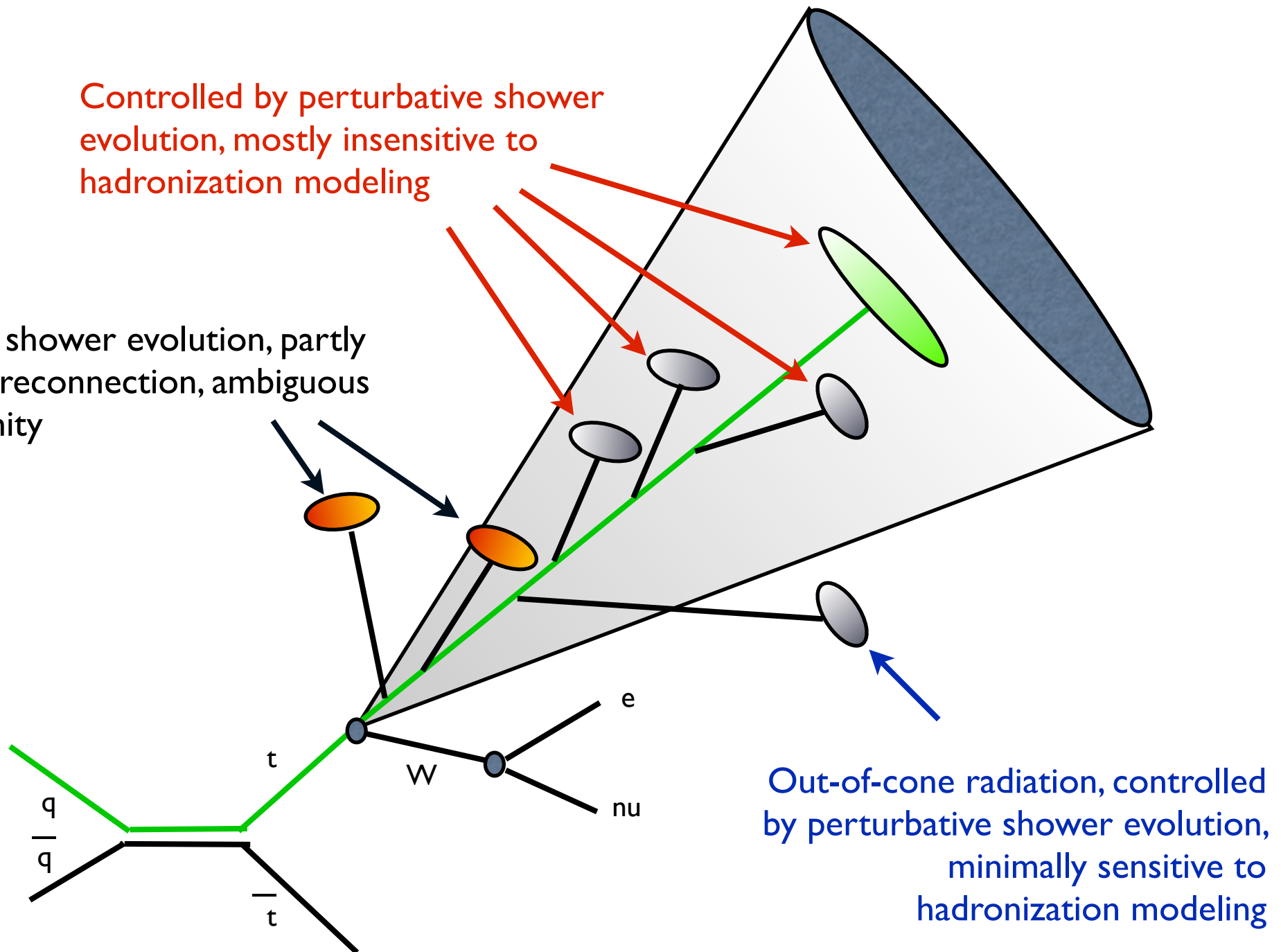
Controlled by perturbative shower evolution, mostly insensitive to hadronization modeling



Out-of-cone radiation, controlled by perturbative shower evolution, minimally sensitive to hadronization modeling

Controlled by perturbative shower evolution, mostly insensitive to hadronization modeling

Partly shower evolution, partly color reconnection, ambiguous paternity



Out-of-cone radiation, controlled by perturbative shower evolution, minimally sensitive to hadronization modeling



**What is the impact, and what are the modeling uncertainties, due to the “odd” clusters?**

**How does their contribution to  $m_{\text{top}}$  depend on the top production dynamics and kinematics?**

- gg vs qqbar initial state
- dependence on  $p_{\text{top}}$
- LHC vs Tevatron

$$m_{\text{top}}^2 \text{ “=” } (p_W + p_{\text{b-jet}})^2$$

“=” : this relation defines a template distribution, whose shape depends on  $m_{\text{top}}^{\text{MC}}$

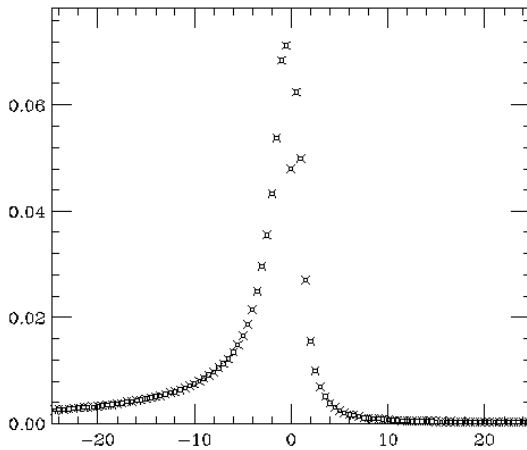
$$p_{\text{b-jet}} = p_{\text{jet}}(\text{even clusters}) + p_{\text{jet}}(\text{odd clusters})$$

**define “jet” as clusters within  $\Delta R < 0.4$  from b-quark direction**

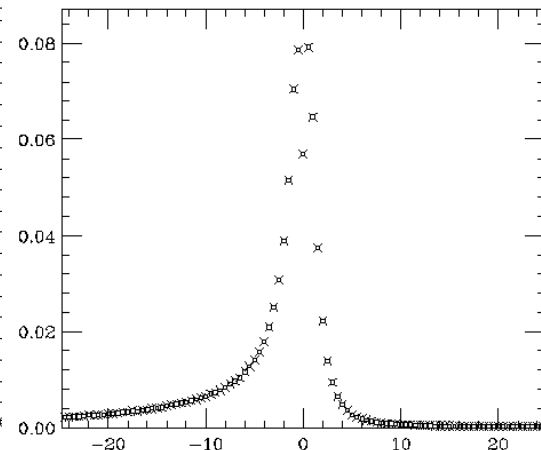
# Example: $m_{\text{top}}$ vs $p_{\text{T}}(\text{top})$

$m_{\text{top}}(\text{E+O}) - 172.5$

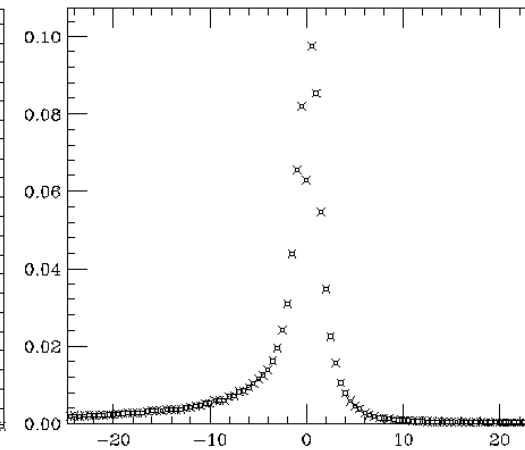
$p_{\text{T}} < 100 \text{ GeV} \langle \rangle = -3.5 \text{ GeV}$



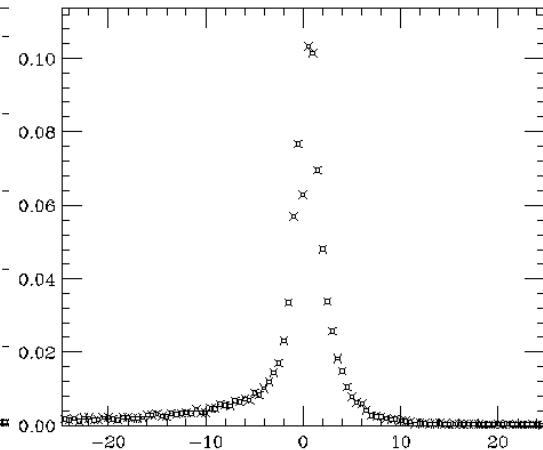
$100 < p_{\text{T}} < 200 \langle \rangle = -2.8 \text{ GeV}$



$200 < p_{\text{T}} < 300 \langle \rangle = -1.95 \text{ GeV}$

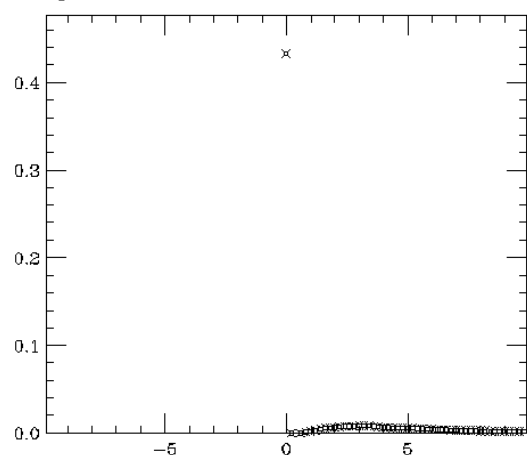


$p_{\text{T}} > 300 \langle \rangle = -0.98 \text{ GeV}$

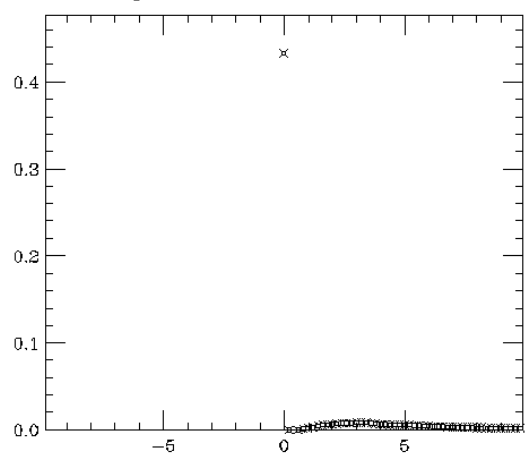


$m_{\text{top}}(\text{E+O}) - m_{\text{top}}(\text{E})$

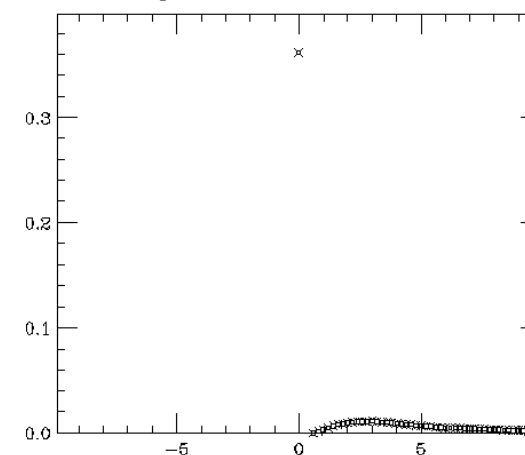
$p_{\text{T}} < 100 \text{ GeV} \langle \rangle = 1.08 \text{ GeV}$



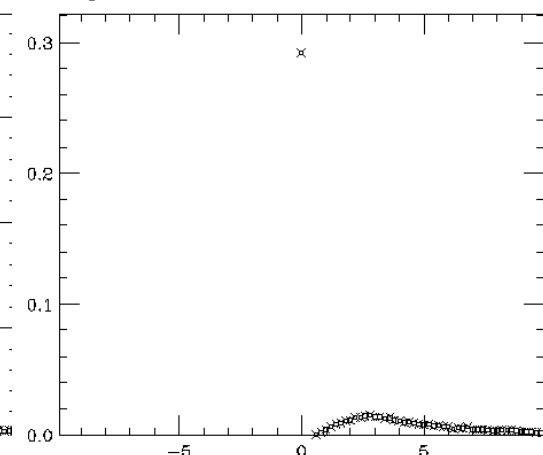
$100 < p_{\text{T}} < 200 \langle \rangle = 1.38 \text{ GeV}$



$200 < p_{\text{T}} < 300 \langle \rangle = 1.83 \text{ GeV}$



$p_{\text{T}} > 300 \langle \rangle = 2.24 \text{ GeV}$



**Notation:**

$m_{\text{top}}(\text{E+O})$ : include both even and odd clusters

$m_{\text{top}}(\text{E})$ : include only even

**A good way to validate the modeling systematics using data is to monitor the dependence of the reconstructed  $m_{\text{top}}$  on the production environment. E.g.**

- **$m_{\text{top}}$  vs  $p_t$**

- **$pp \rightarrow t \bar{t}$  implies that hadronization of top decay products differs from hadronization of  $\bar{t}$  decay products  $\Rightarrow m_t$  vs  $m_{\bar{t}}$  at the LHC probes possible hadronization systematics**

- **$q \bar{q} \rightarrow t \bar{t}$  vs  $gg \rightarrow t \bar{t} \Rightarrow m_{\text{top}}(\text{Tevatron})$  vs  $m_{\text{top}}(\text{LHC})$  is a probe of hadronization systematics**

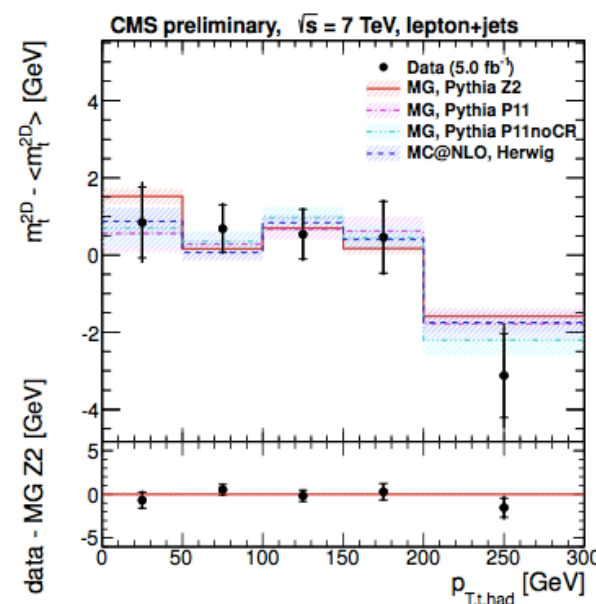
- **ditto for  $m_{\text{top}}$  from single top events**

# Dependence of Top Mass on Event Kinematics

CMS-PAS-TOP-12-029

NEW

	Fig.	Observable
color recon.	1	$\Delta R_{q\bar{q}}$
	2	$\Delta\phi_{q\bar{q}}$
	3	$p_{T,t, \text{had}}$
	4	$ \eta_{t, \text{had}} $
ISR/FSR	5	$H_T$
	6	$m_{t\bar{t}}$
	7	$p_{T,t\bar{t}}$
	8	Jet multiplicity
b-quark kin.	9	$p_{T,b, \text{had}}$
	10	$ \eta_{b, \text{had}} $
	11	$\Delta R_{b\bar{b}}$
	12	$\Delta\phi_{b\bar{b}}$



- First top mass measurement binned in kinematic observables.
- Additional validation for the top mass measurements.
- With the current precision, no mis-modelling effect due to
  - ◆ color reconnection, ISR/FSR, b-quark kinematics, difference between pole or  $\overline{\text{MS}}$  masses.

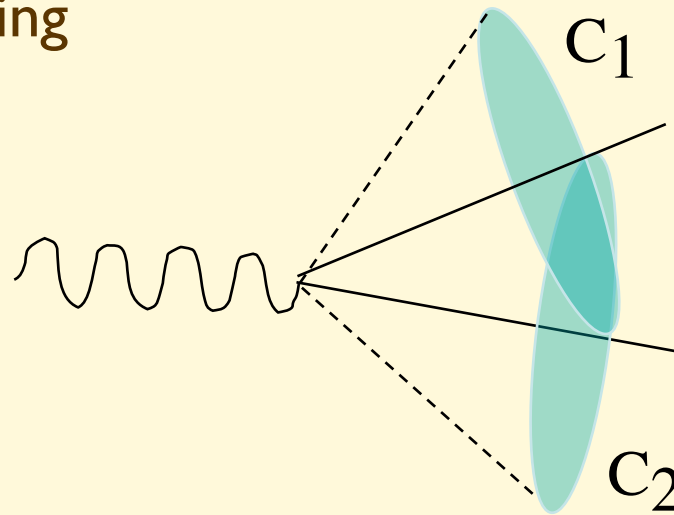
CMS-PAS-TOP-12-031

$$\Delta m_t = m_t^{\text{had}} - m_{\bar{t}}^{\text{had}} = -272 \pm 196 \text{ (stat)} \pm 122 \text{ (syst.) MeV}$$

# Multijet final states

# Main limitation of shower approach:

Because of angular ordering



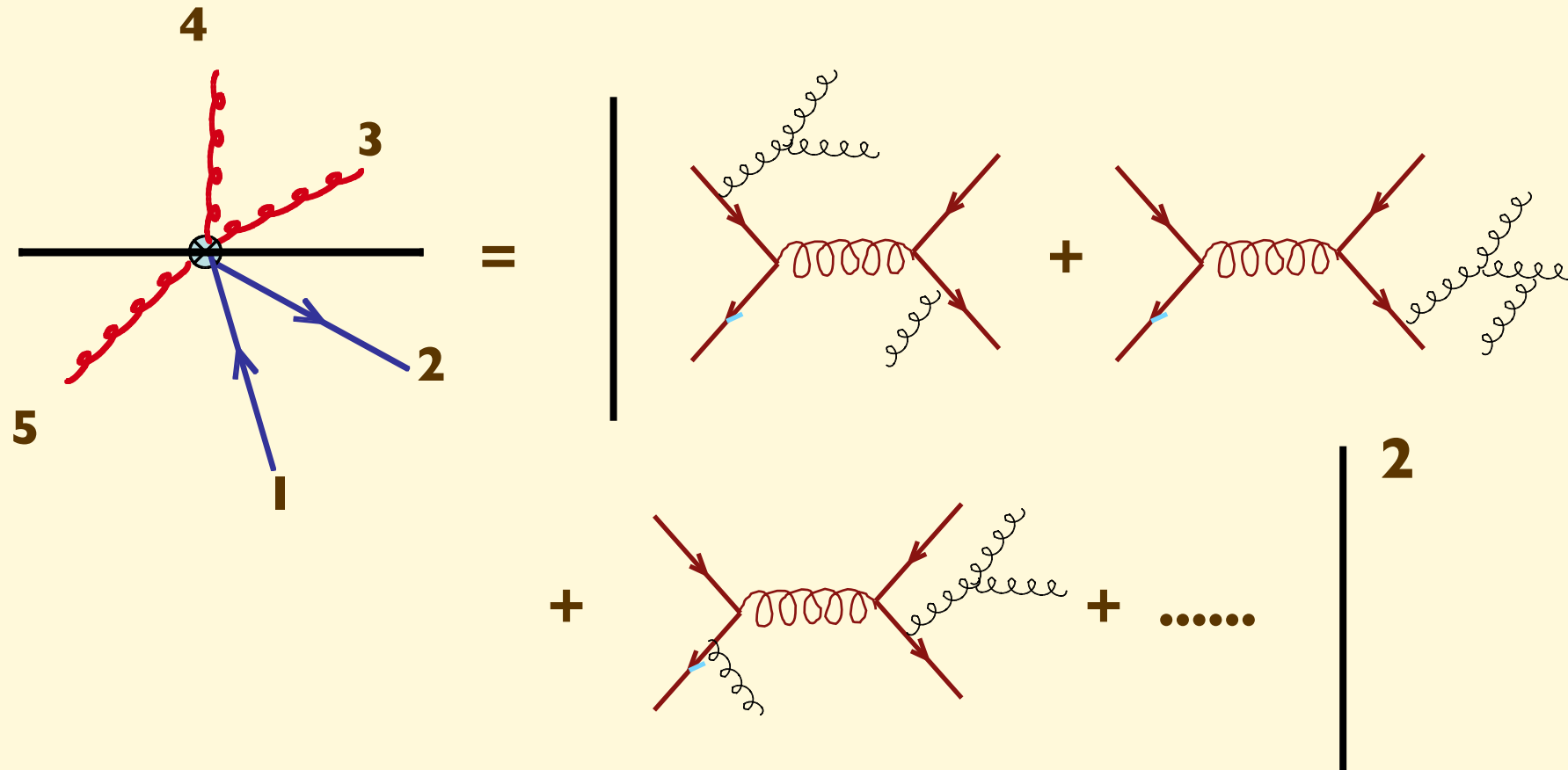
➔ **no emission outside  $C_1 \oplus C_2$ :**

- lack of hard, large-angle emission
- poor description of multijet events

➔ **incoherent emission inside  $C_1 \oplus C_2$ :**

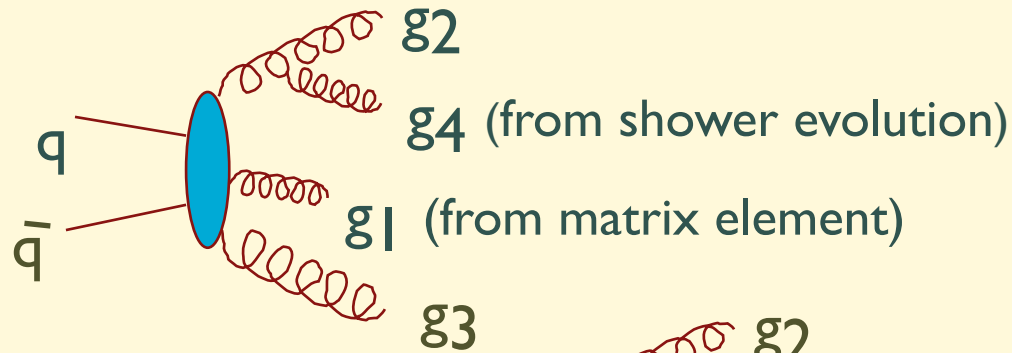
- loss of accuracy for intrajet radiation

The obvious solution is to start the shower from a higher-order process calculated at the parton level with the exact LO matrix element:



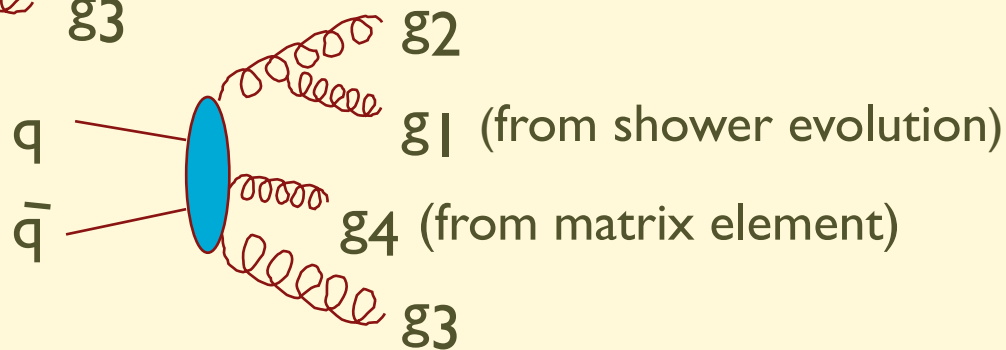
Each hard parton then undergoes the shower evolution according to the previous prescription.

## This approach has its own problems:



with  $p_{T1} \ll p_{T4} \ll p_{T2}, p_{T3}$

versus

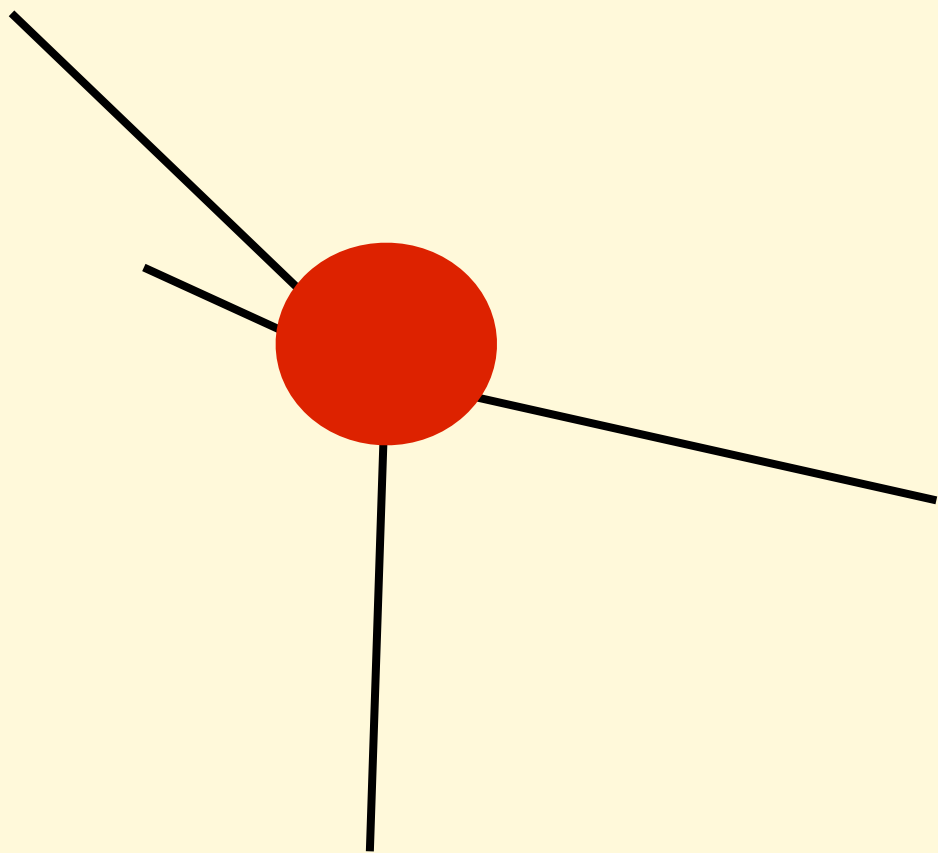


⇒ **double counting of the same phase-space points**

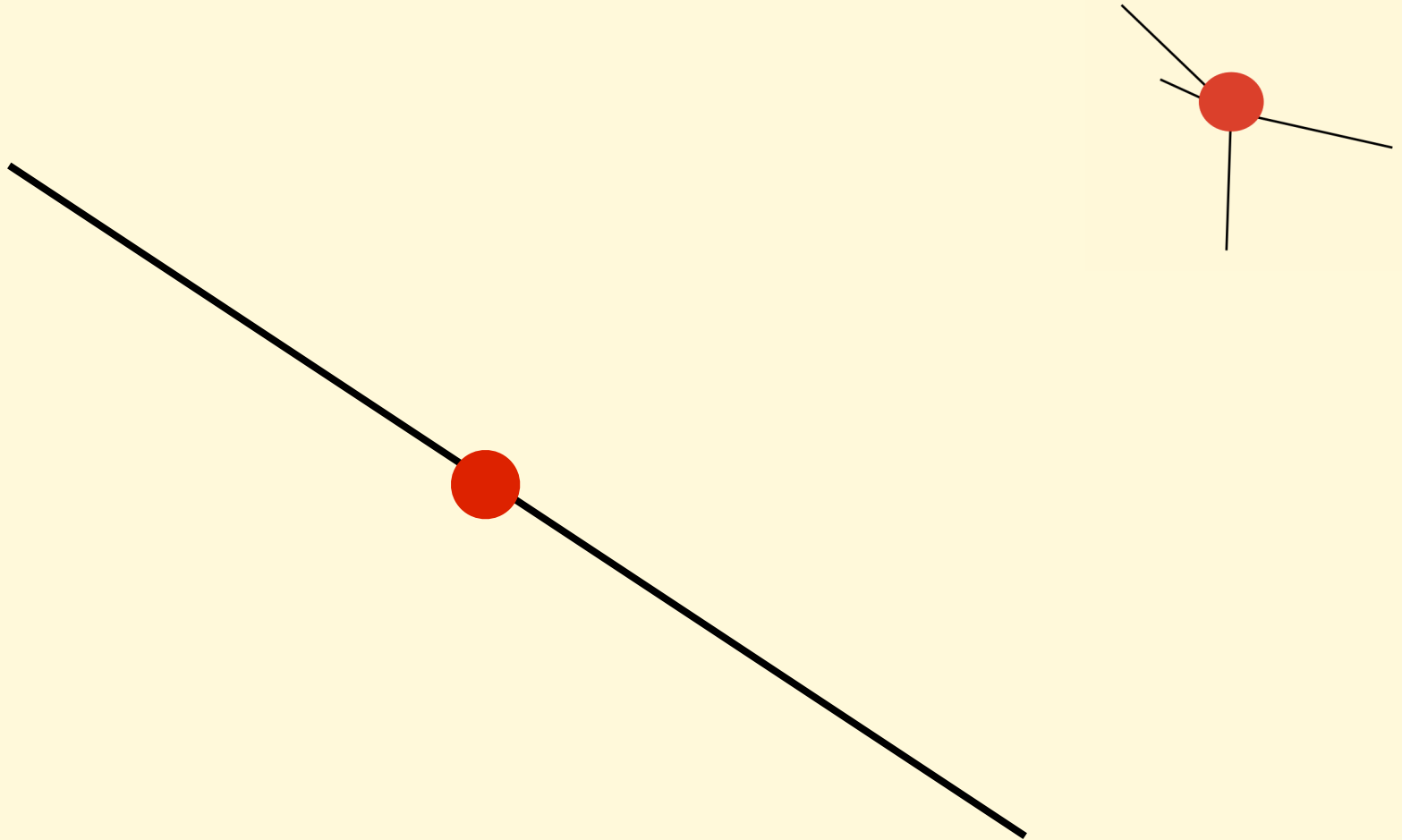
**The solution to these problems goes under the name of matching algorithms, which allow to combine higher-order ME and shower evolution avoiding the double counting (“CKKW”, “MLM matching”)**



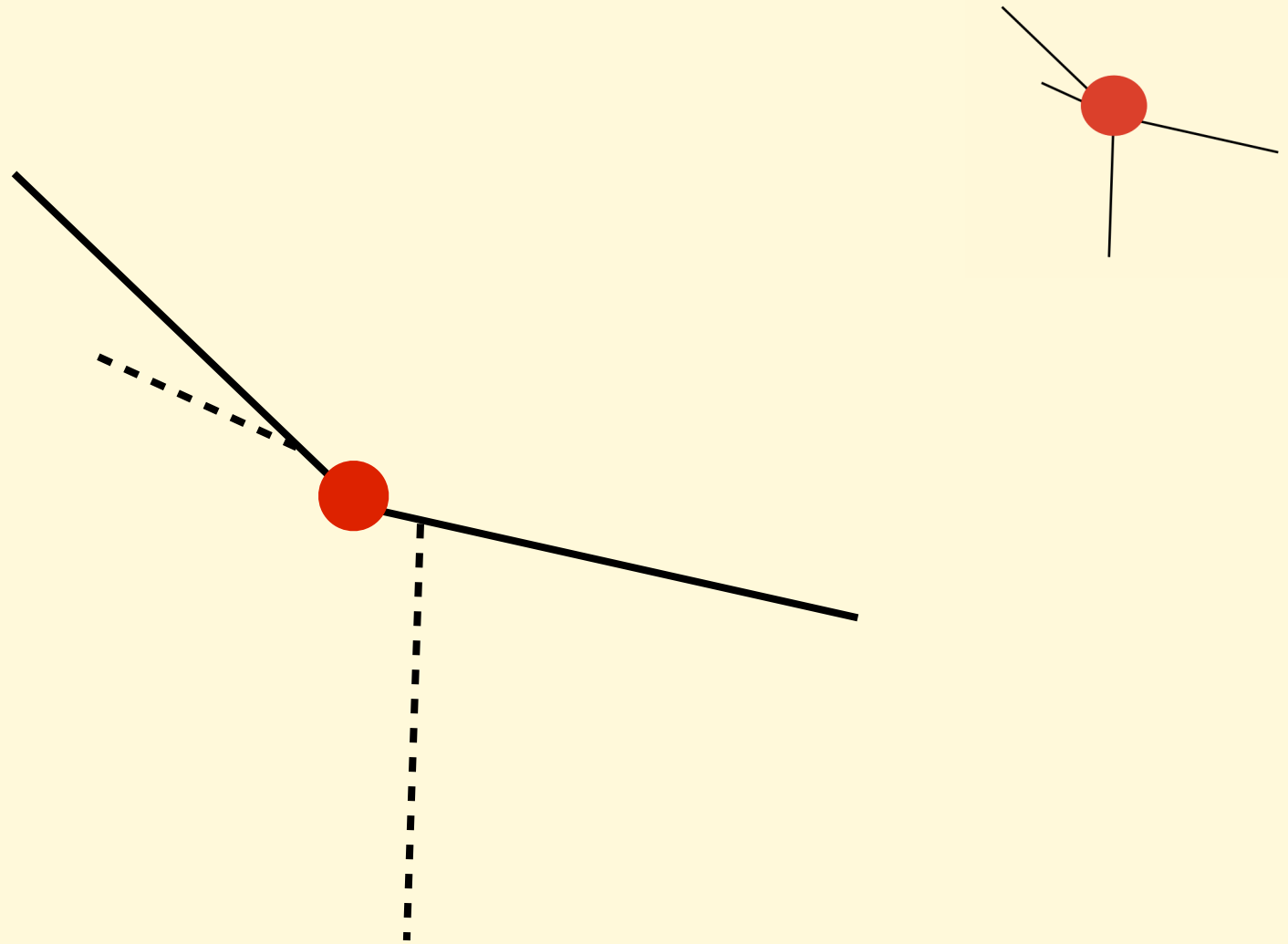
Example: possible ways of generating a 4-body final state



Representation I:  
Double shower emission from a 2-parton final state



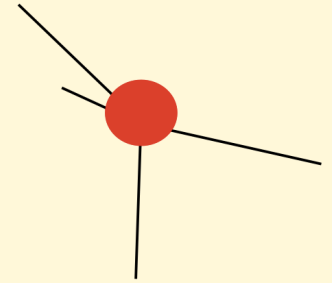
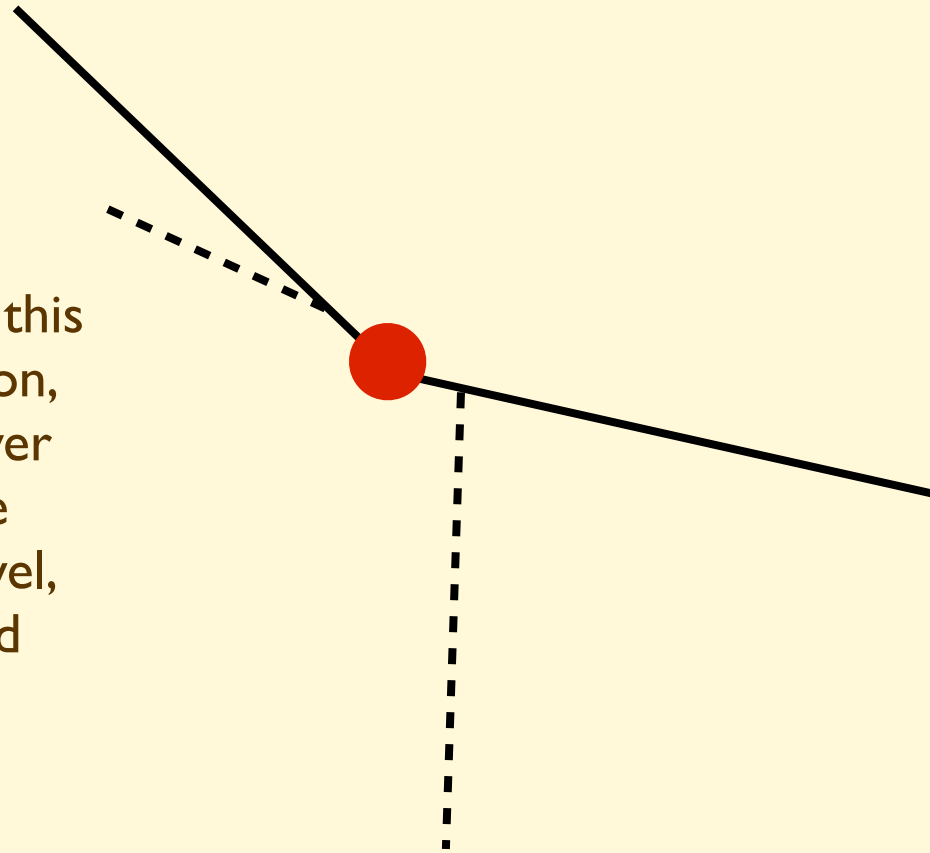
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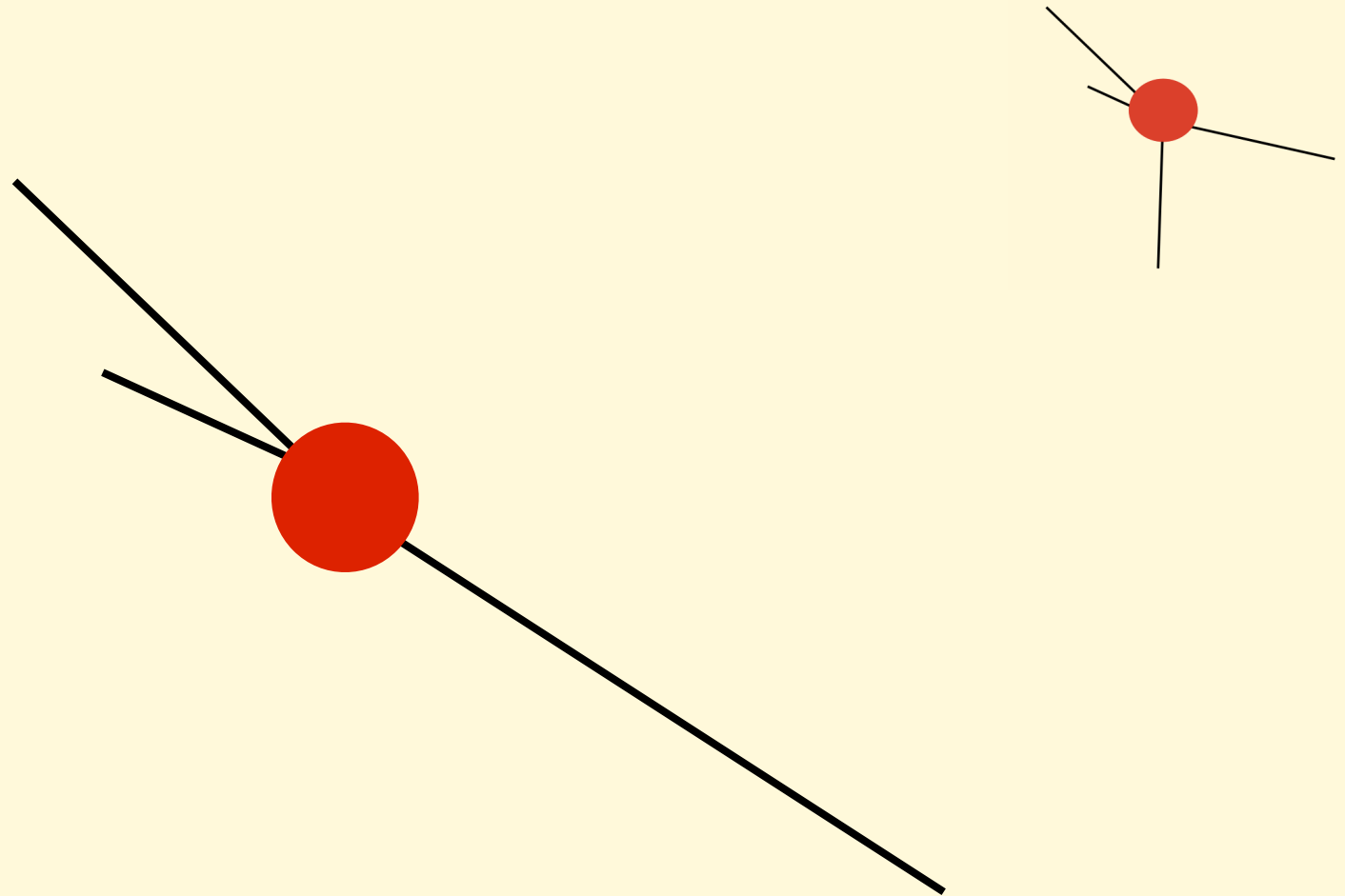
# Representation I: Double shower emission from a 2-parton final state

**Good** description of this  
~collinear configuration,  
since it uses the shower  
(which includes, at the  
leading logarithmic level,  
virtual corrections and  
resummation)

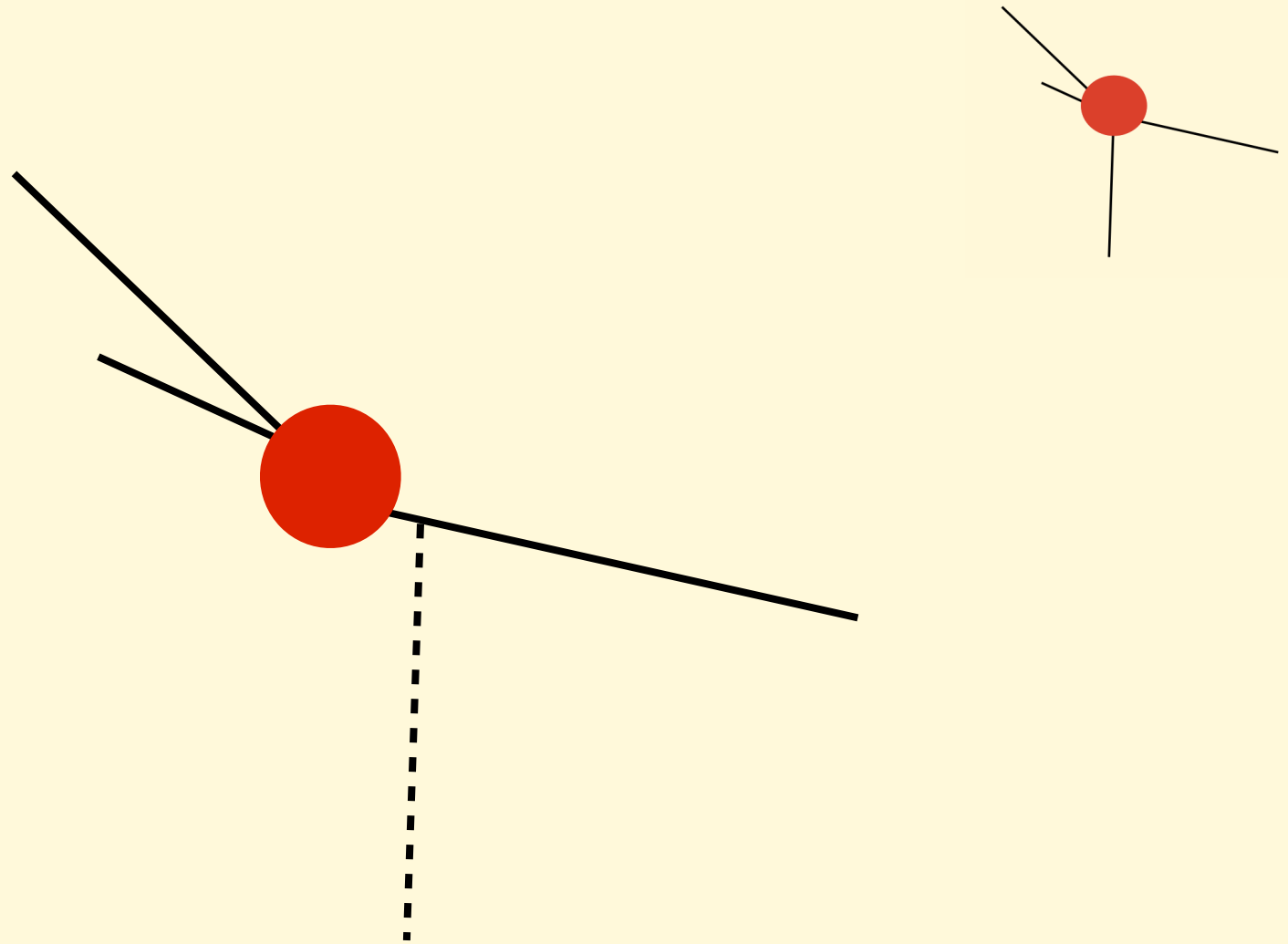
**Poor** description of this emission,  
since it's hard and at large angle



Representation 2:  
Shower emission from a 3-parton final state

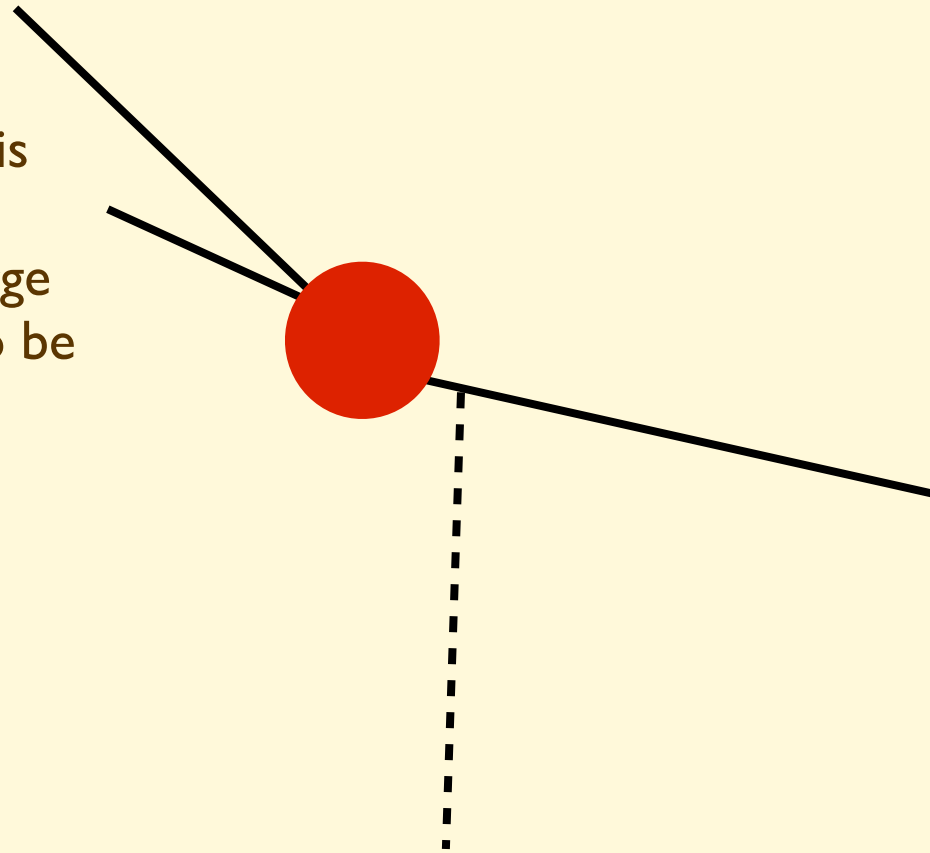


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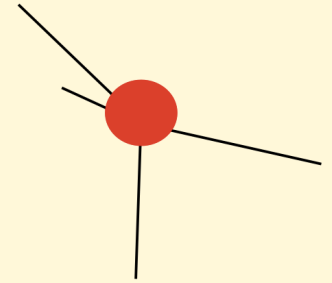


## Representation 2: Shower emission from a 3-parton final state

**Poor** description of this configuration, since it's  $\sim$ collinear, leads to a large logarithm, that needs to be absorbed by virtual corrections and by resummation

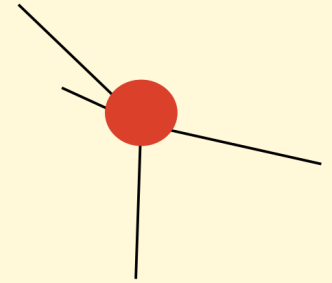
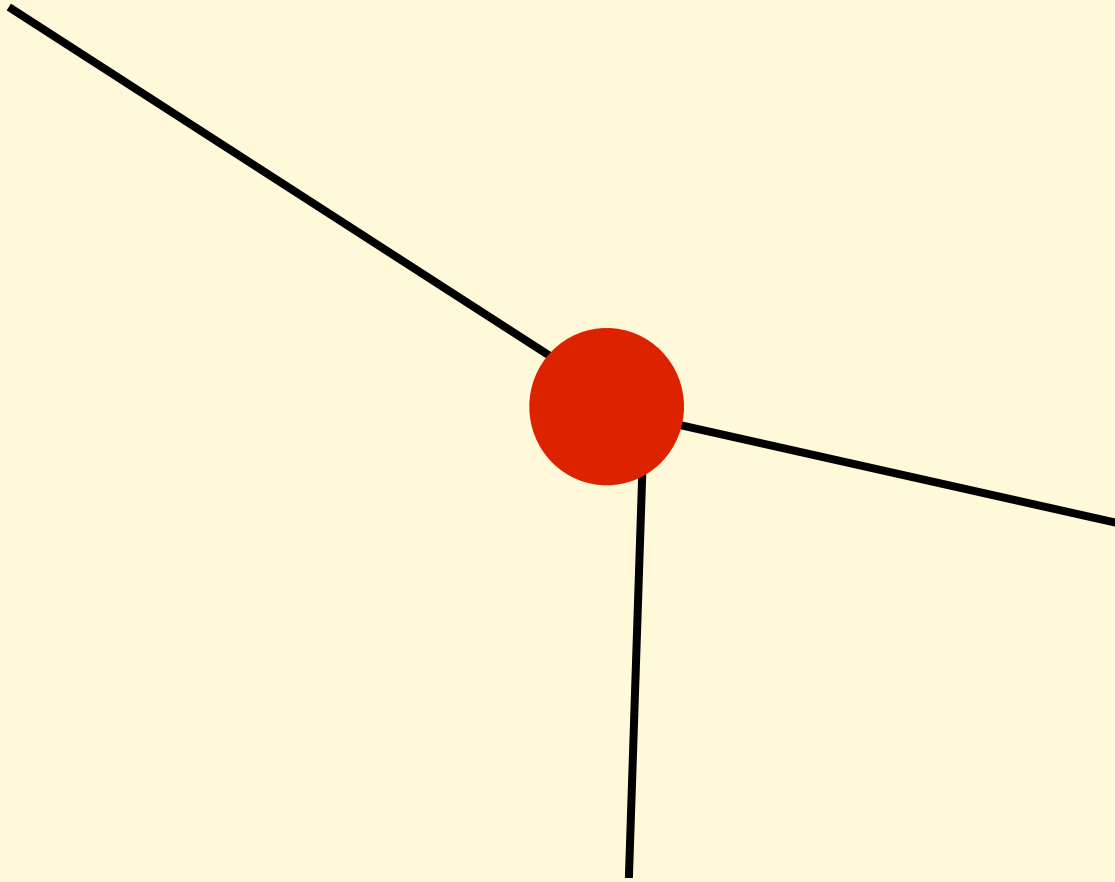


**Poor** description of this emission, since it's hard and at large angle



### Representation 3:

Shower emission from a different choice of 3-parton final state



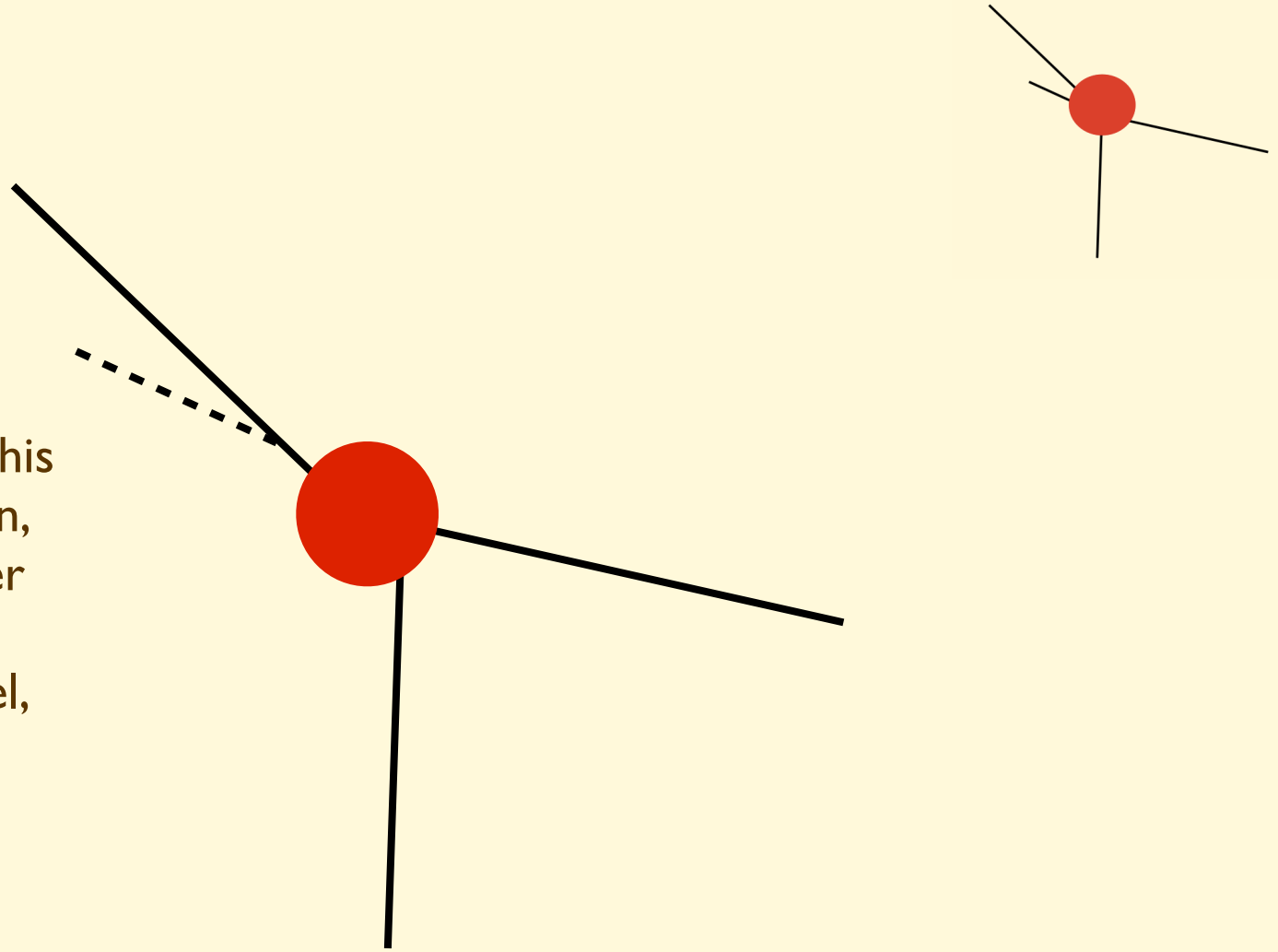


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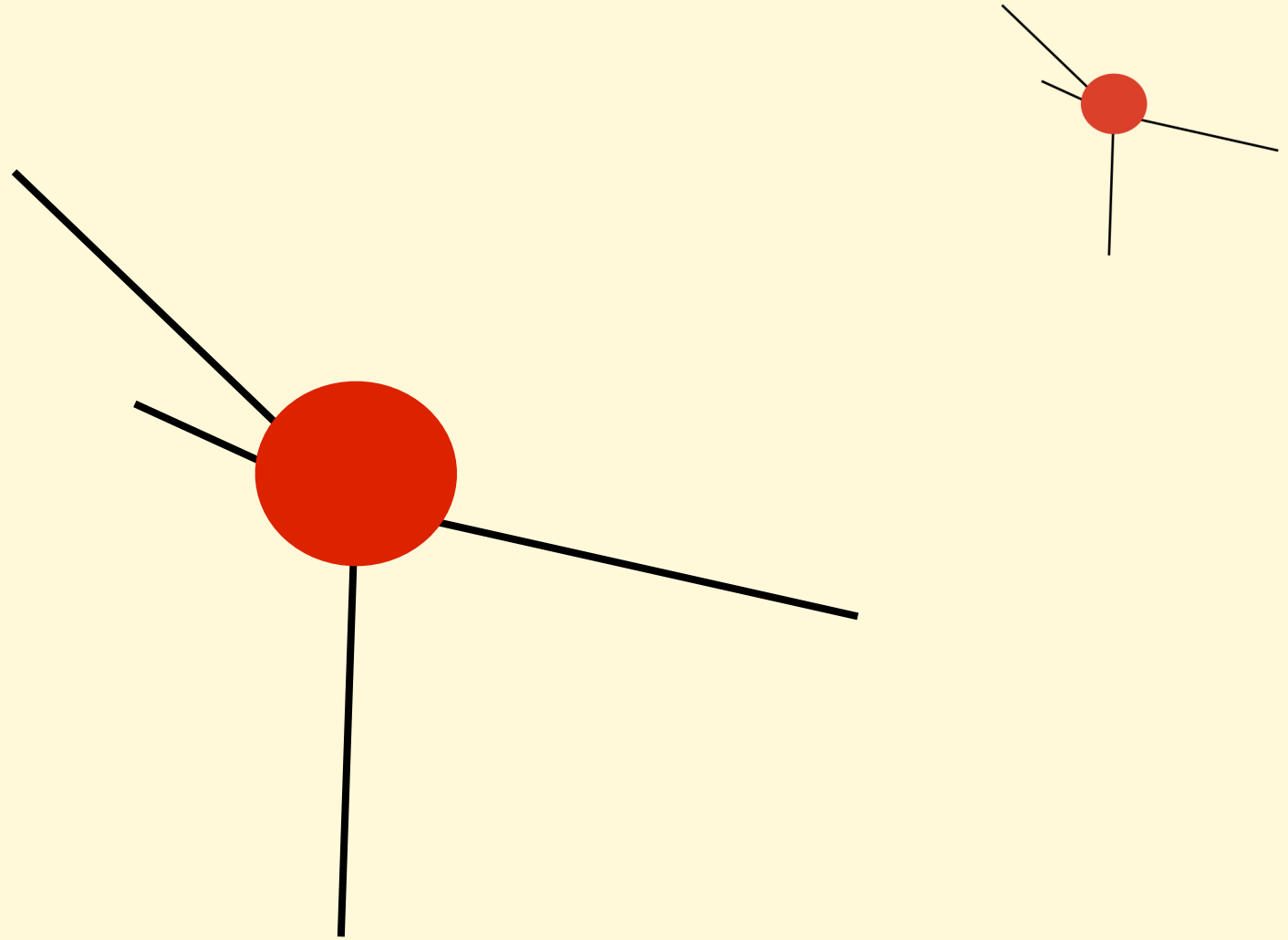
Shower emission from a different choice of 3-parton final state

**Good** description of this  
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**Good** description of this hard/  
large-angle emission, since it's using  
the matrix element

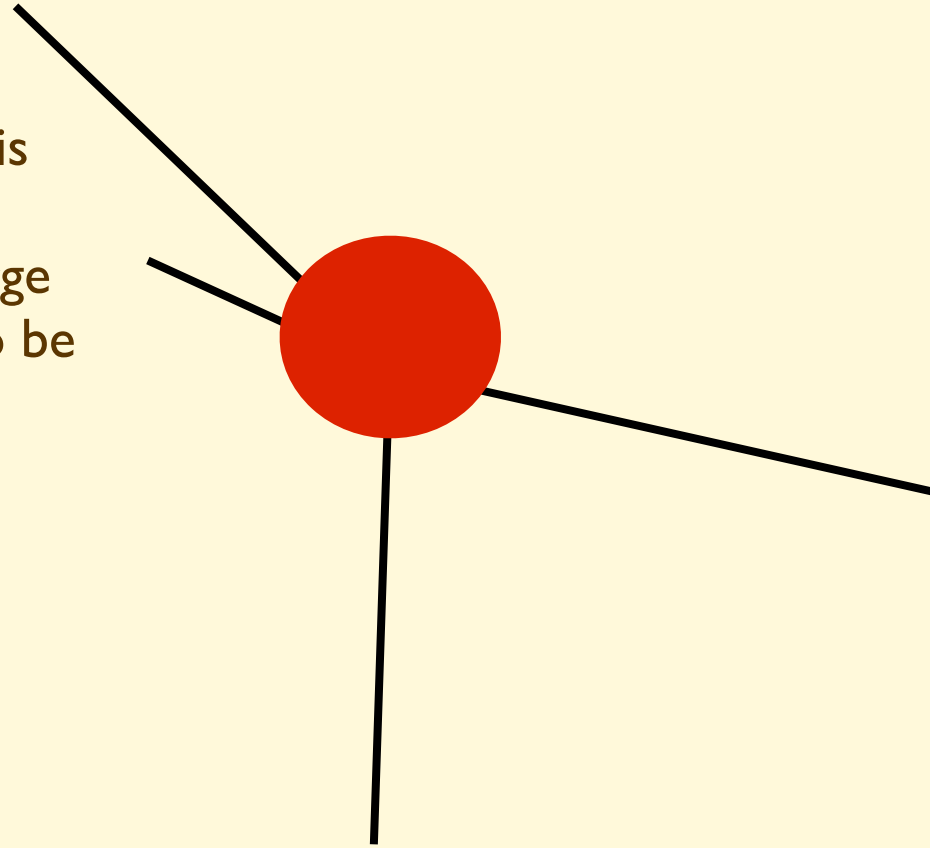


Representation 4:  
Generated directly as a 4-parton final state

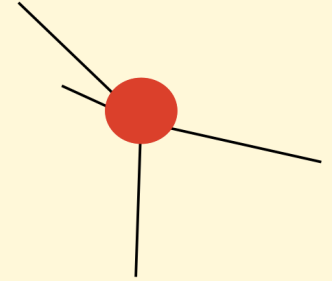


Representation 4:  
Generated directly as a 4-parton final state

**Poor** description of this configuration, since it's  $\sim$ collinear, leads to a large logarithm, that needs to be absorbed by virtual corrections and by resummation



**Good** description of this hard/  
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As we generate an inclusive sample of events, including events of any multiplicity, we should apply a “filter” (matching algorithm) that decides which representation gives the most accurate description of a given event. In our example, this means:

Event 1 ( $2 \rightarrow 2$ plus double shower emission)	$\Rightarrow$ throw away
Event 2 ( $2 \rightarrow 3$ , config (a), plus shower emission)	$\Rightarrow$ throw away
Event 3 ( $2 \rightarrow 3$ , config (b), plus shower emission)	$\Rightarrow$ <b>keep</b>
Event 4 ( $2 \rightarrow 4$ )	$\Rightarrow$ throw away

# MLM merging algorithm for multijet final states

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- **Generate parton-level configurations** for a given hard-parton multiplicity  $N_{\text{part}}$ , with partons constrained by  $p_T > p_{T,\text{min}}$  and  $\Delta R_{jj} > R_{\text{min}}$

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  - if all partons are matched, **keep** the event, else **discard** it

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  - a jet can only be matched to a single parton
  - if all partons are matched, **keep** the event, else **discard** it
- **If additional jets are present:**

# MLM merging algorithm for multijet final states

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# MLM merging algorithm for multijet final states

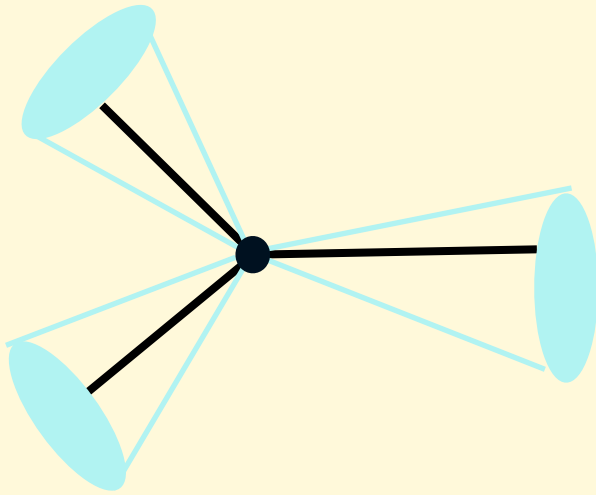
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- After matching, combine all samples to obtain an **inclusive sample containing events with all multiplicities**



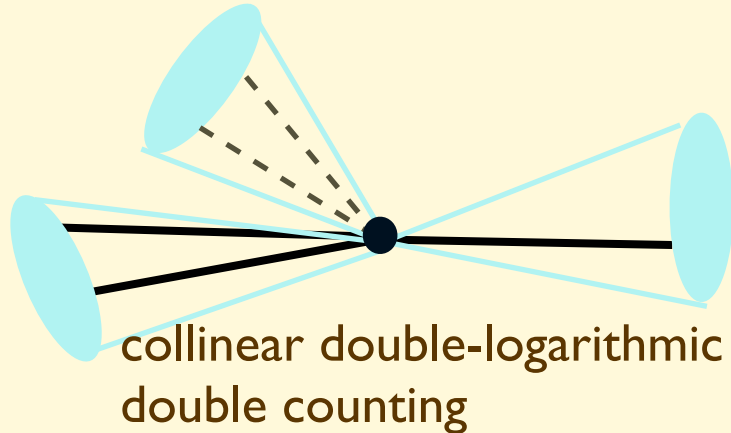
## Few examples of matching:

————— hard parton

- - - - - parton emitted by the shower

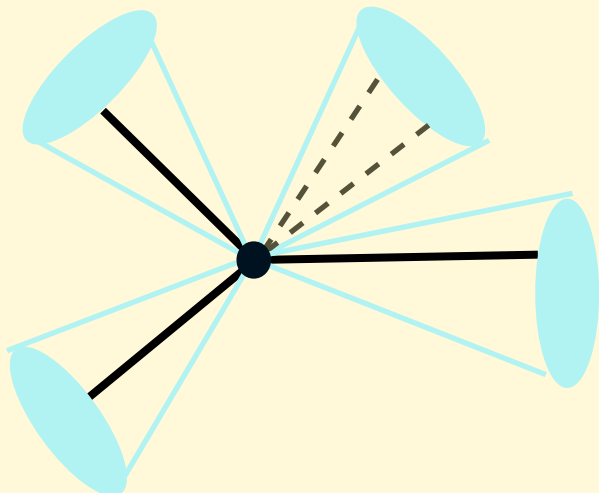
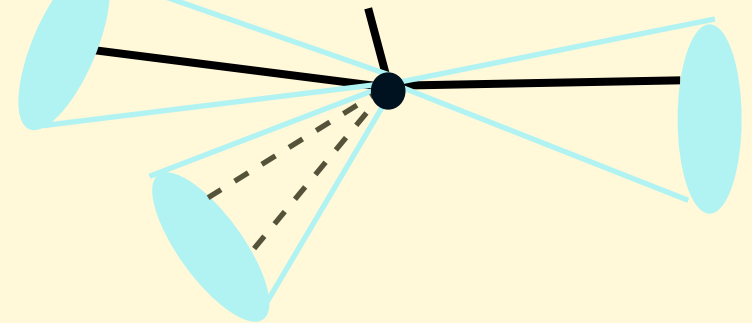


Event matched,  $N_{\text{jet}} = N_{\text{part}} = 3$ , keep



NOT matched,  
 $N_{\text{jet}} = N_{\text{part}} = 3$ ,  
but  $N_{\text{match}} = 2$   
Throw away

soft single-logarithmic  
double counting

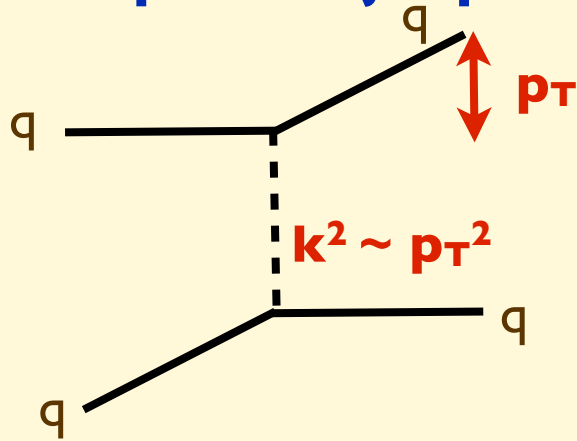


Event matched,  $N_{\text{jet}} > N_{\text{part}}$  :

- o Keep for inclusive sample **if the unmatched jet is softer than all matched ones.**
- o Throw away otherwise, or for exclusive samples.

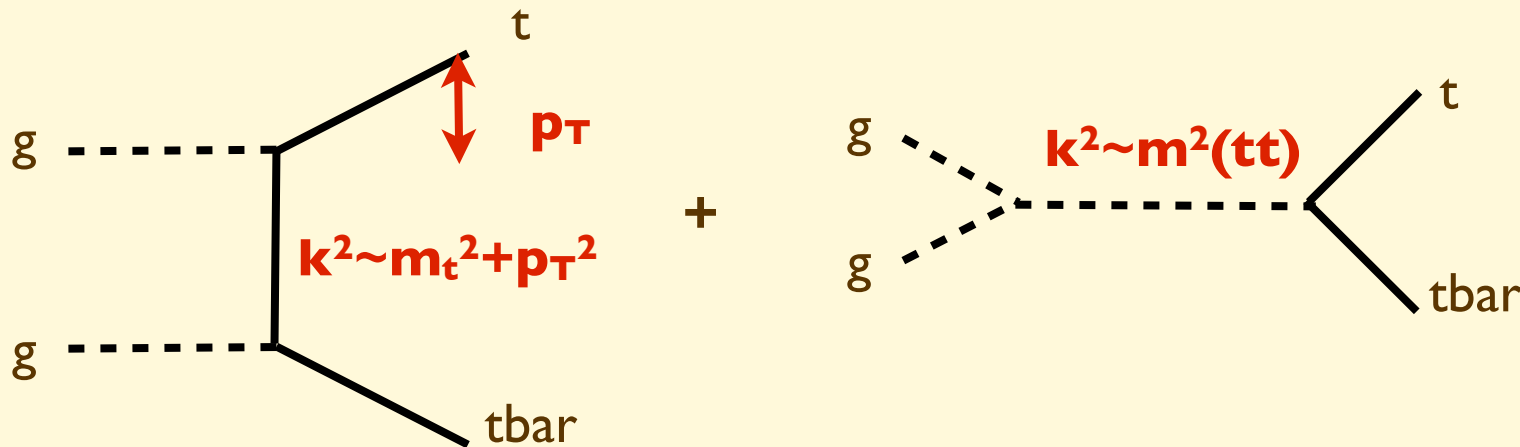
# Issues in setting the proper scale for $\alpha_s(Q^2)$

## Example 1: 2-jet production



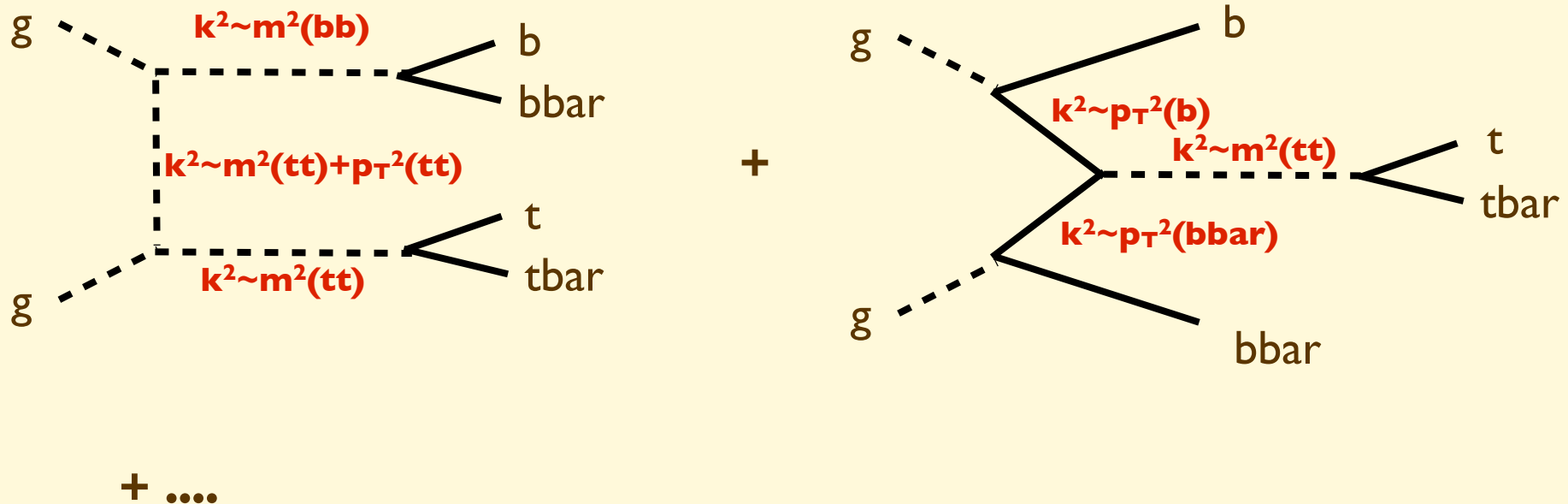
$\Rightarrow Q=p_T$  is the natural, and only, scale present in this process

## Example 2: t-tbar production



$\Rightarrow$  Here we have two scales,  $Q_a^2 = m_t^2 + p_T^2$  and  $Q_b^2 = m^2(tt)$ . However they are numerically similar  $\Rightarrow$  small difference in using  $\alpha_s(Q_a)$  vs  $\alpha_s(Q_b)$

### Example 3: $t \bar{t} + b \bar{b}$ production

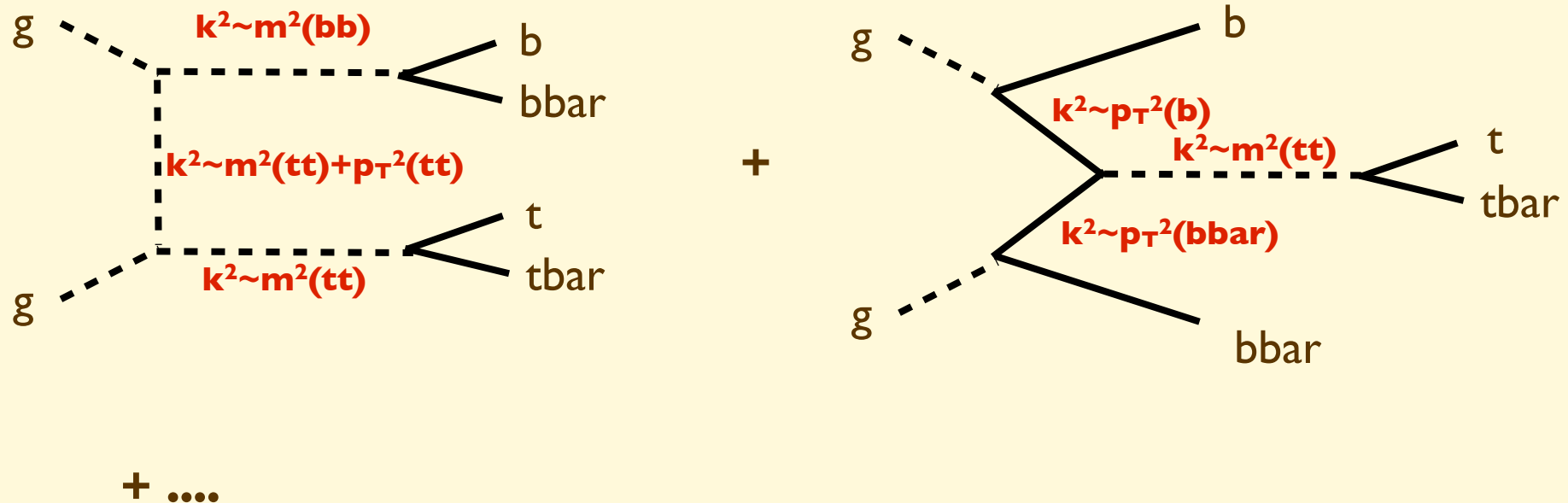


$\Rightarrow$  Now we have several scales, which can be numerically very very different. E.g. we can certainly have kinematical configurations with  $p_T(b) \ll m(bb) \ll m(tt)$

$\Rightarrow$  What is the right scale to be used for all 4 powers of  $\alpha_s(Q)$  appearing in the cross section ??

$$[ \alpha_s(2m_{\text{bottom}}) / \alpha_s(2m_{\text{top}}) ]^4 \sim 16 !!$$

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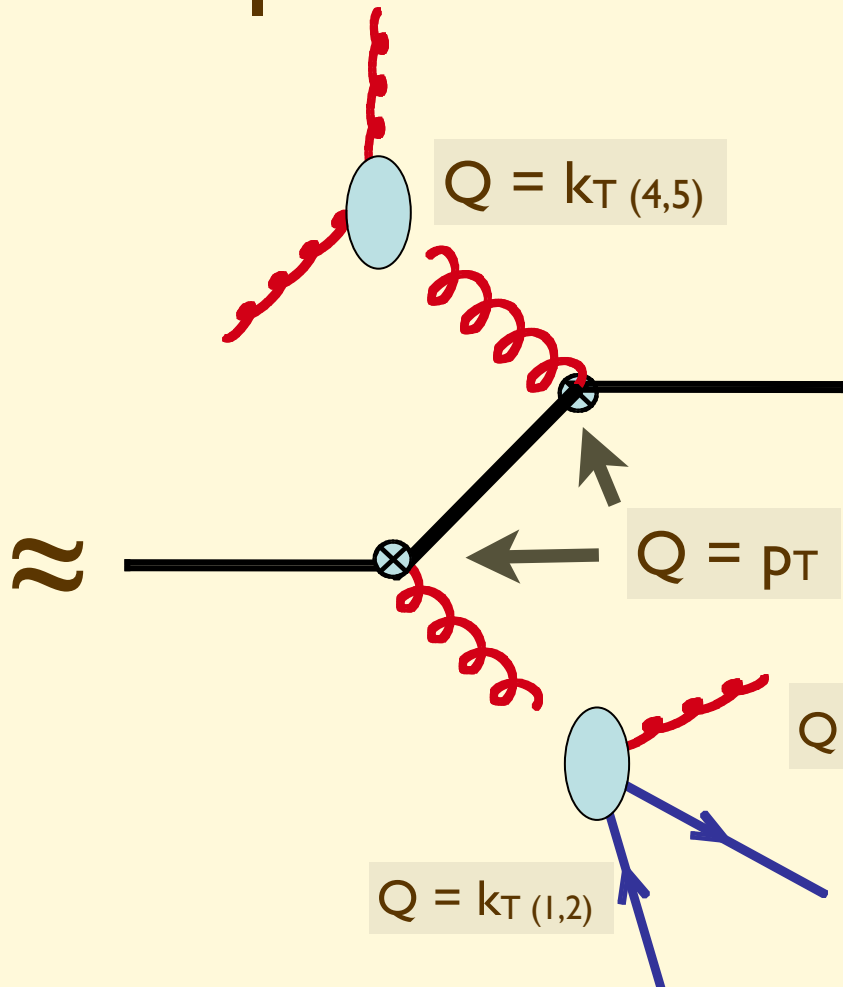
$$[ \alpha_s(2m_{\text{bottom}}) / \alpha_s(2m_{\text{top}}) ]^4 \sim 16 !!$$

**Similar problems arise each time we deal with multijet final states, in configurations with multiple mass scales**

## Scale setting in calculations with matching (a.k.a. CKKW scale setting)

$$k_{T[1,2]} < k_{T[\bar{2},3]} < k_{T[4,5]}$$

Only pairings allowed by colour and flavour flows are considered



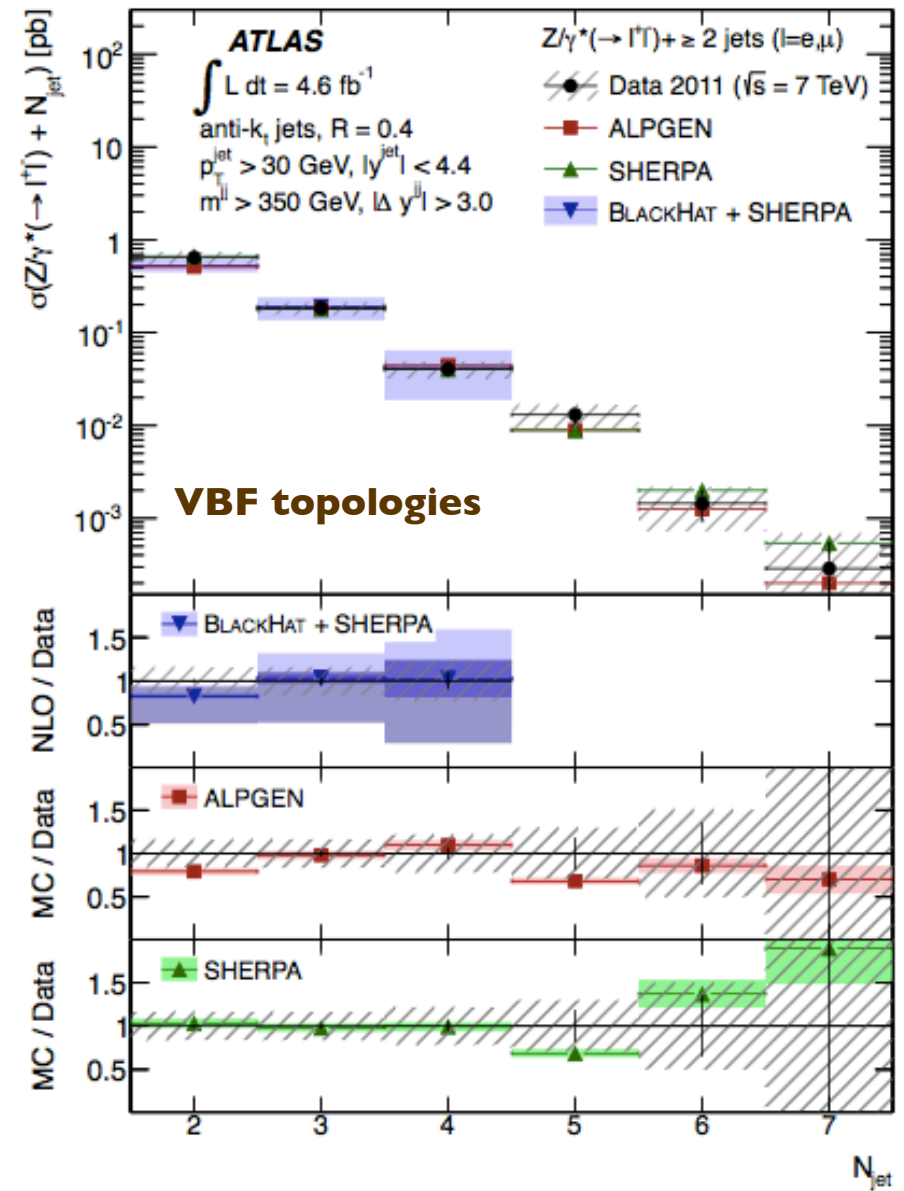
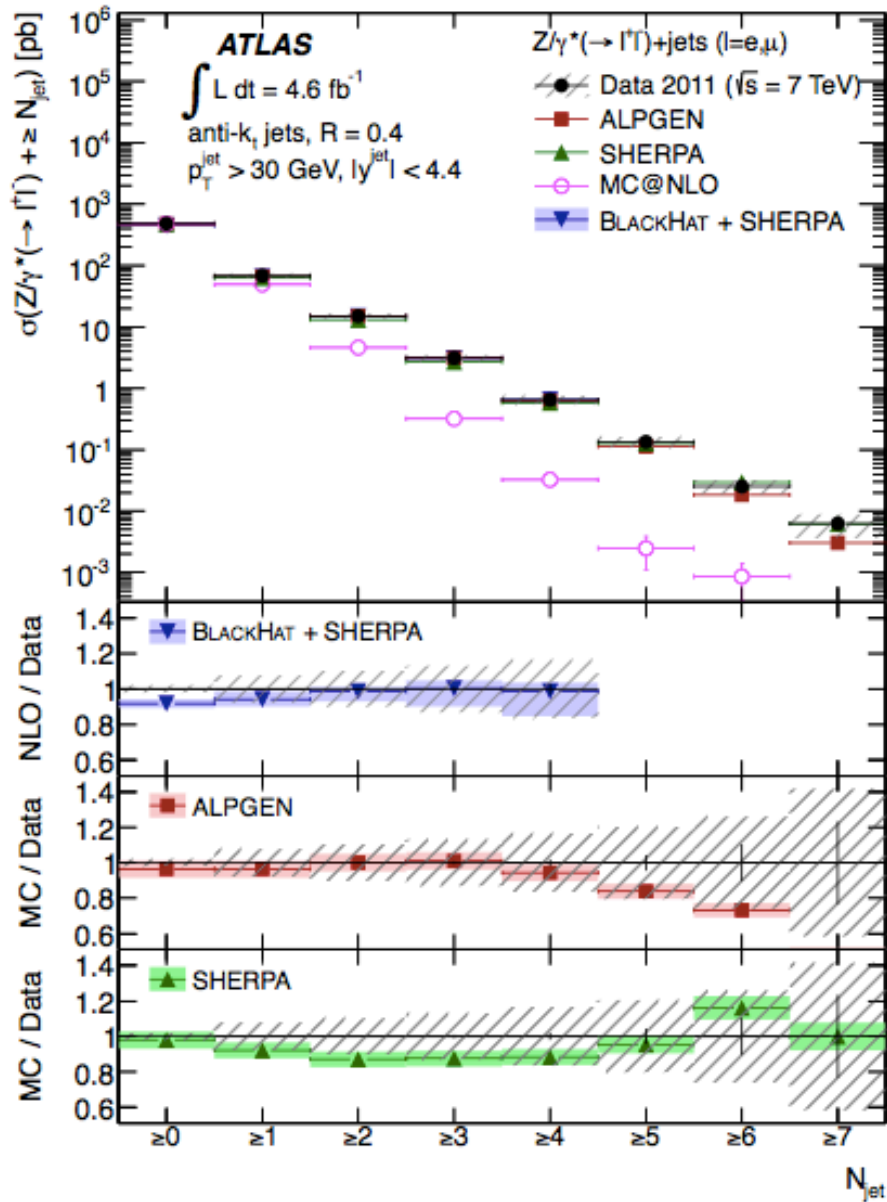
This is the hard scale as defined by **iqopt**, and depends on the hard process considered

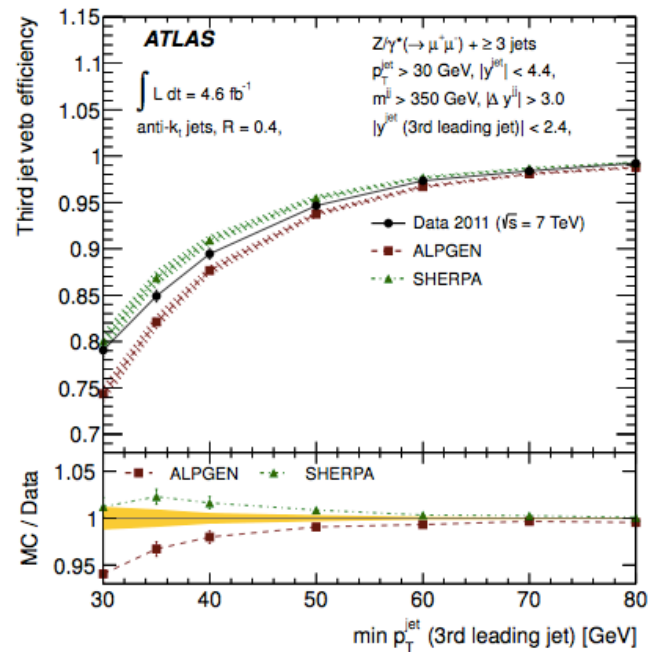
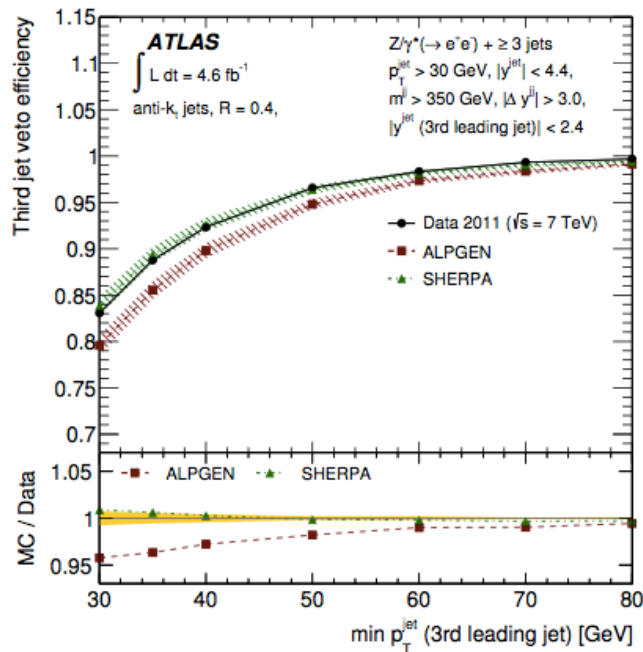
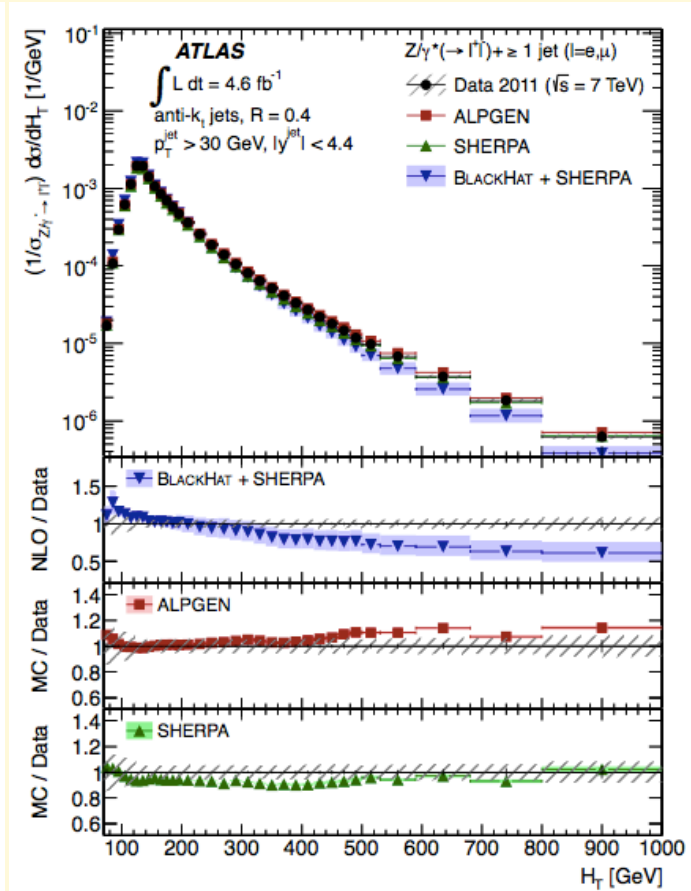
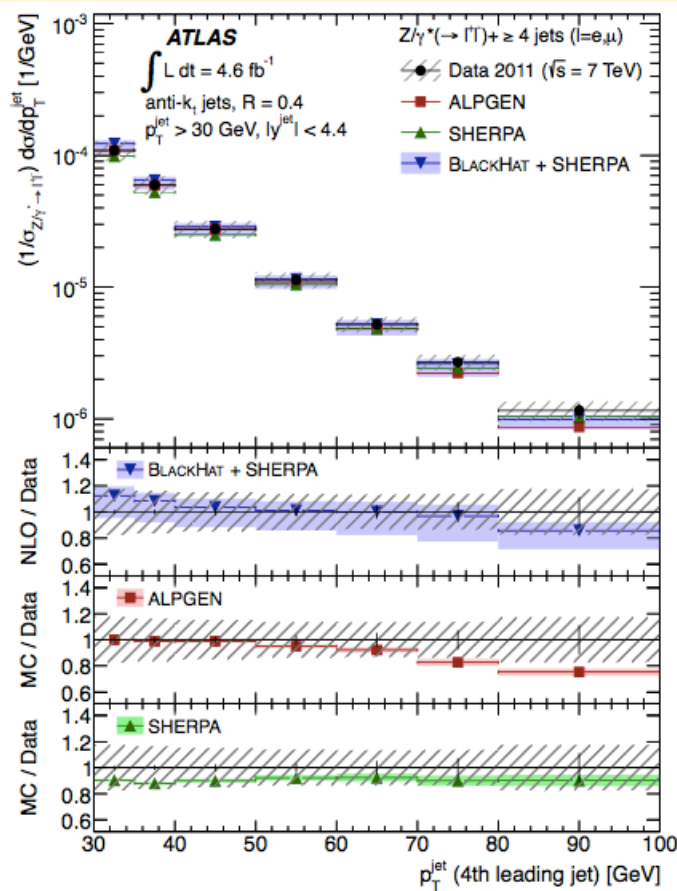
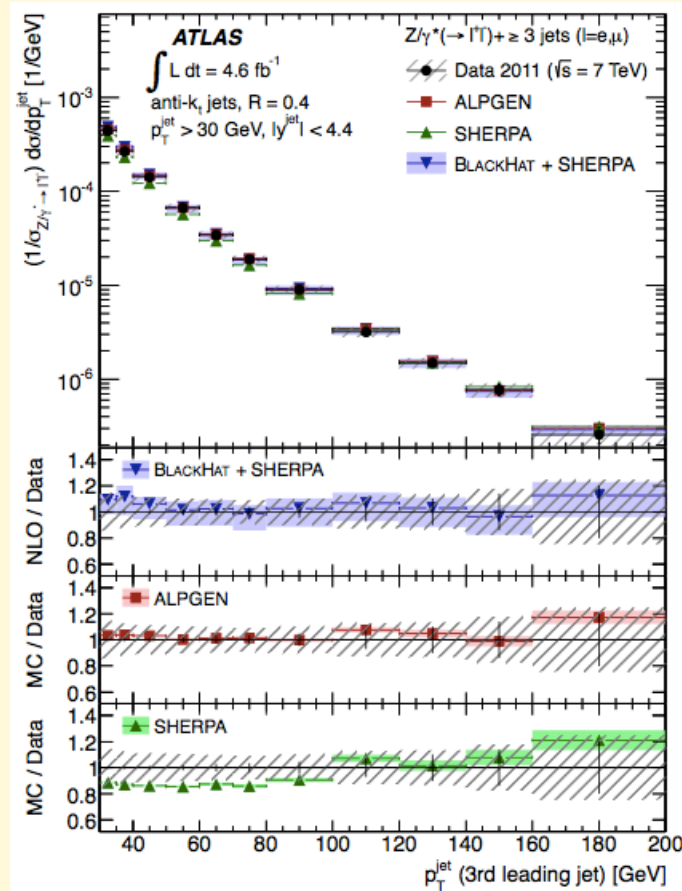
$$\approx \alpha^2(p_T) \alpha(k_{T(1,2)}) \alpha(k_{T(12,3)}) \alpha(k_{T(4,5)})$$

$$\otimes F_1(x_1, p_T) \otimes F_2(x_2, p_T)$$

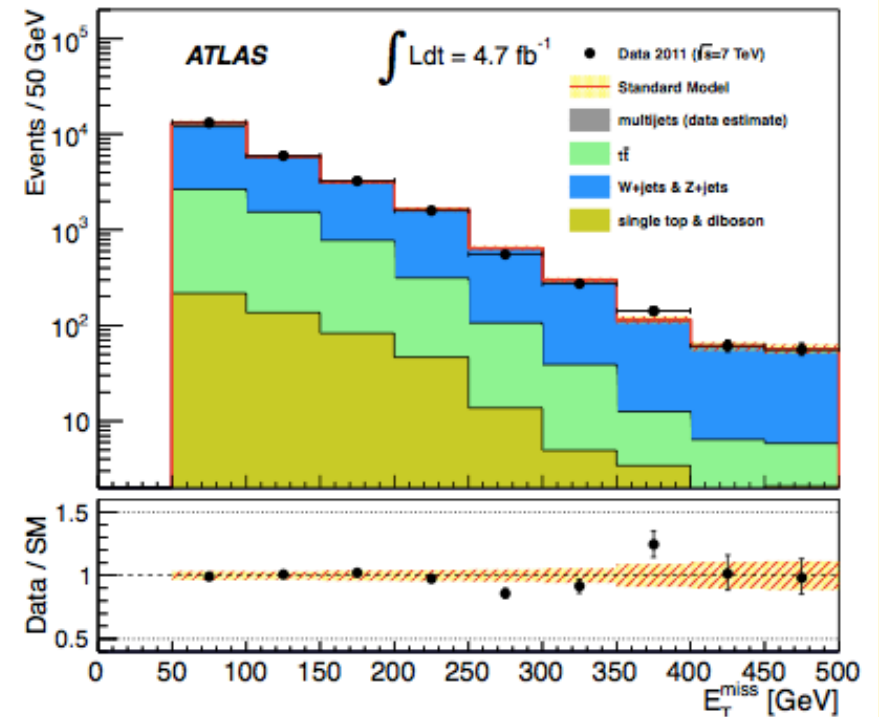
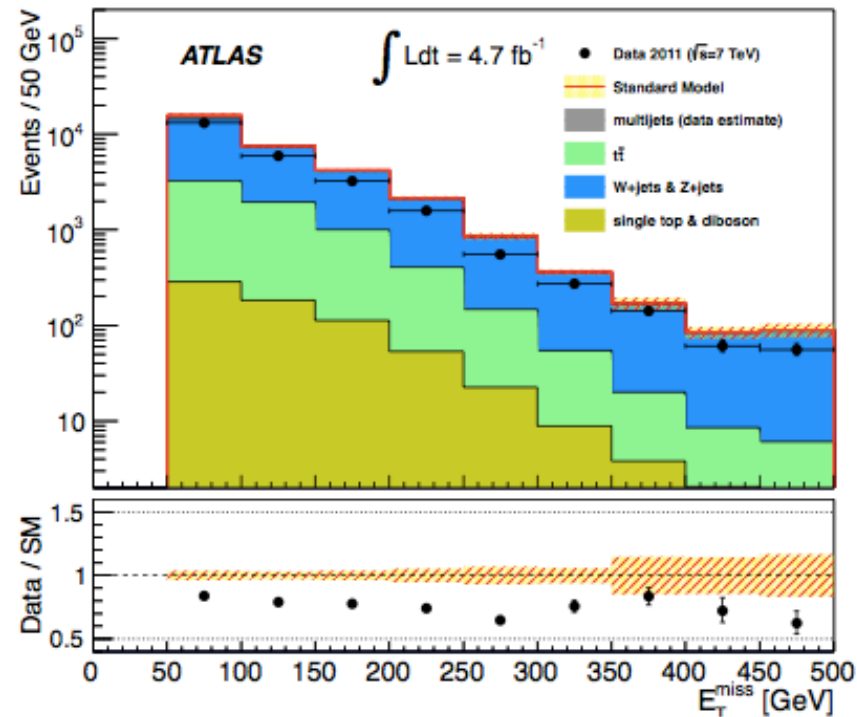
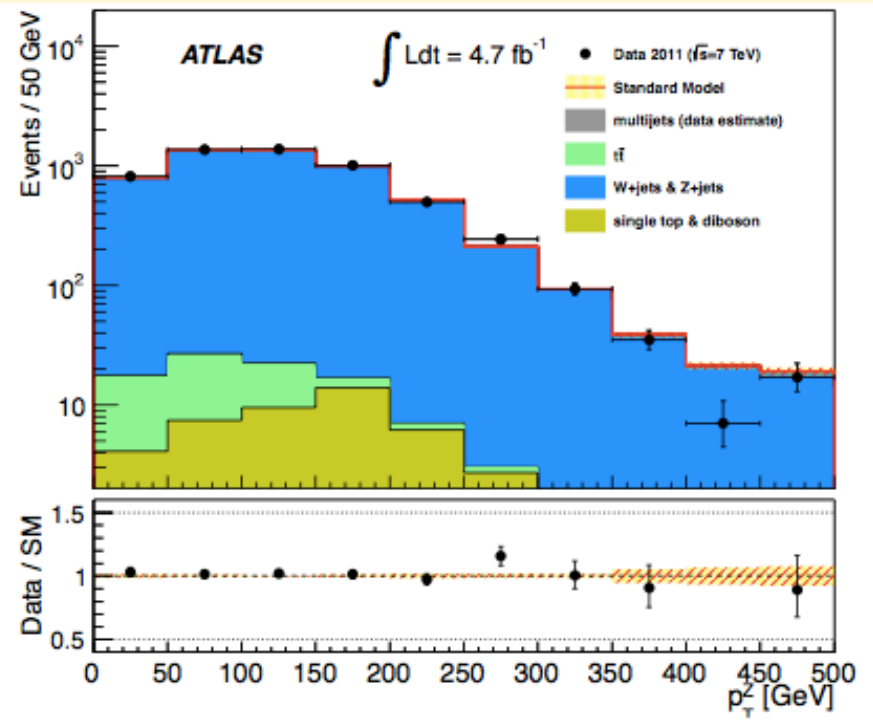
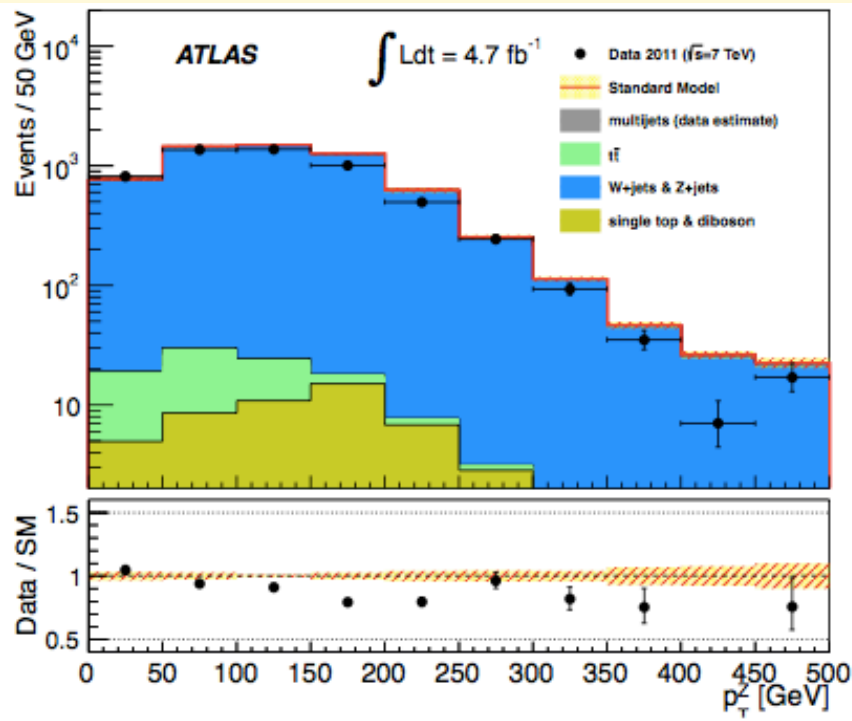
# Examples: Z+jets, data vs theory

ATLAS, arXiv:1304.7098











# **Using LHC data to improve our knowledge about PDF**

## Example: precision Higgs physics

**Theoretical uncertainties on production rates** (Higgs XSWG, arXiv:1101.0593)

14 TeV	$\delta(\text{pert. theory})$	$\delta(\text{PDF}, \alpha_s)$
$gg \rightarrow H$	$\pm 10 \%$	$\pm 7\%$
VBF ( $WW \rightarrow H$ )	$\pm 1 \%$	$\pm 2\%$
$qq \rightarrow WH$	$\pm 0.5 \%$	$\pm 4\%$
$(qq, gg) \rightarrow ZH$	$\pm 2 \%$	$\pm 4\%$
$(qq, gg) \rightarrow ttH$	$\pm 8 \%$	$\pm 9\%$

Improve with higher-loop  
calculations:  
 **$gg \rightarrow H$  @ NNNLO**  
 **$ttH$  @ NNLO**

Improve with  
dedicated QCD  
measurements,  
and appropriate  
calculations

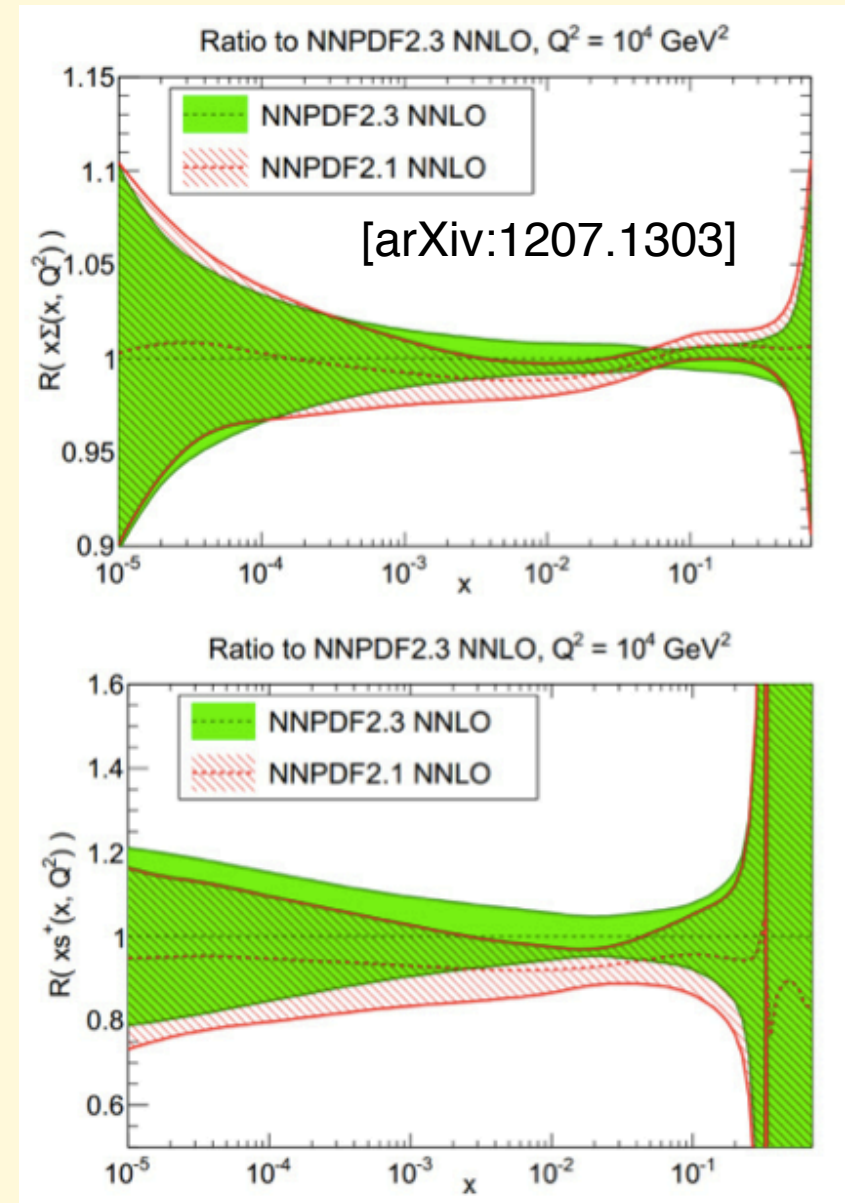
# PDF progress

**NNPDF2.3:** First publicly available PDF set that includes LHC data in the fit.  
Global fit, includes all relevant LHC data that were available with full covariance matrix

- ATLAS Inclusive Jets,  $36\text{pb}^{-1}$
- ATLAS W/Z lepton rapidity distributions,  $36\text{pb}^{-1}$
- CMS W lepton asymmetry,  $840\text{pb}^{-1}$
- LHCb W rapidity distributions,  $36\text{pb}^{-1}$

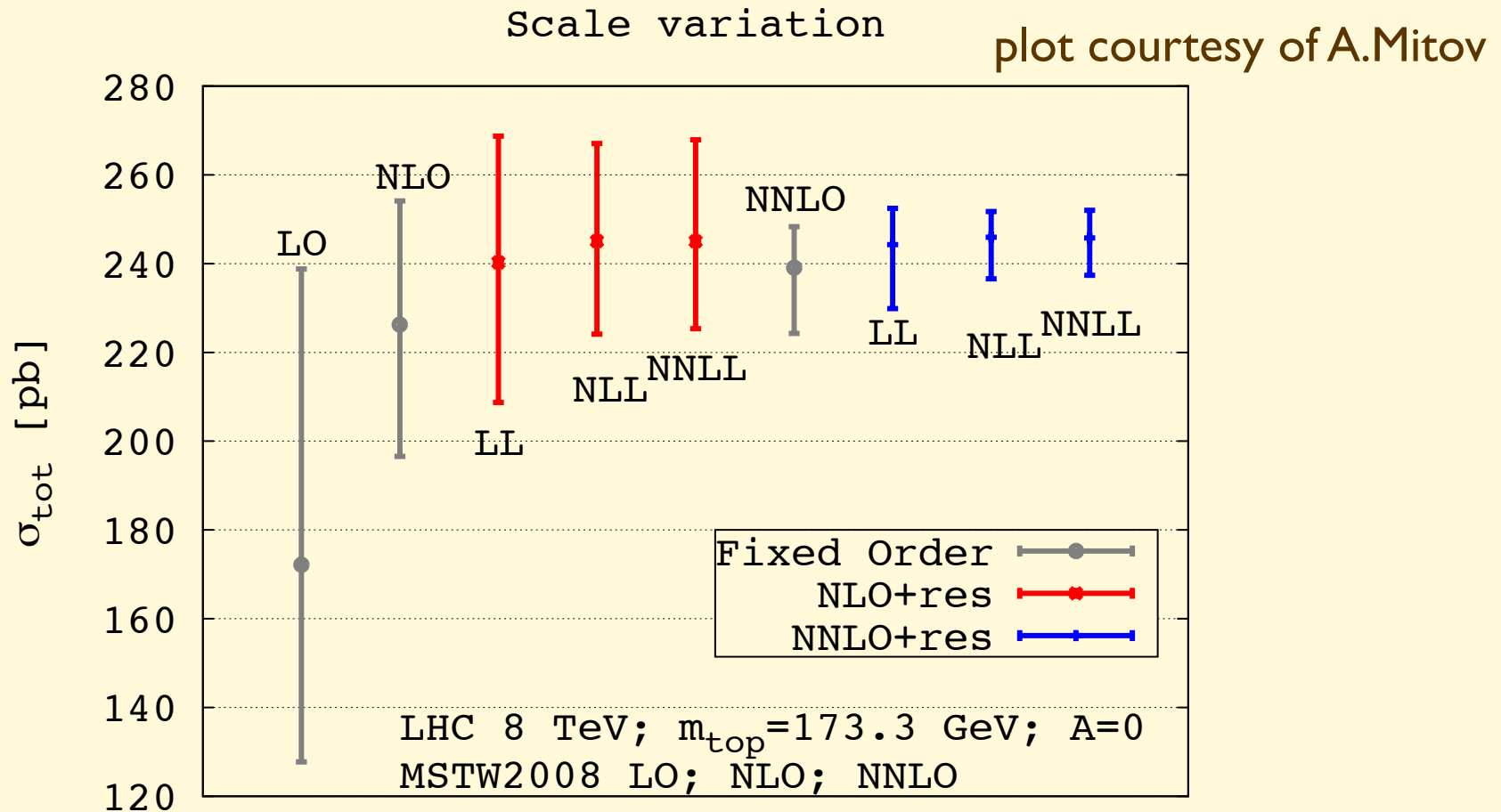
Impact of LHC data:

- Moderate effect from LHC data, generally less than half a sigma in central values.
- Largest impact is for Singlet and strange distributions.
- Expect more substantial improvements with 2011 and 2012 data.



Further progress from more data, and more accurate (NNLO) theory for a variety of processes probing different flavours and ranges of  $x$  and  $Q$ .

# Inclusive tt cross section at NNLO

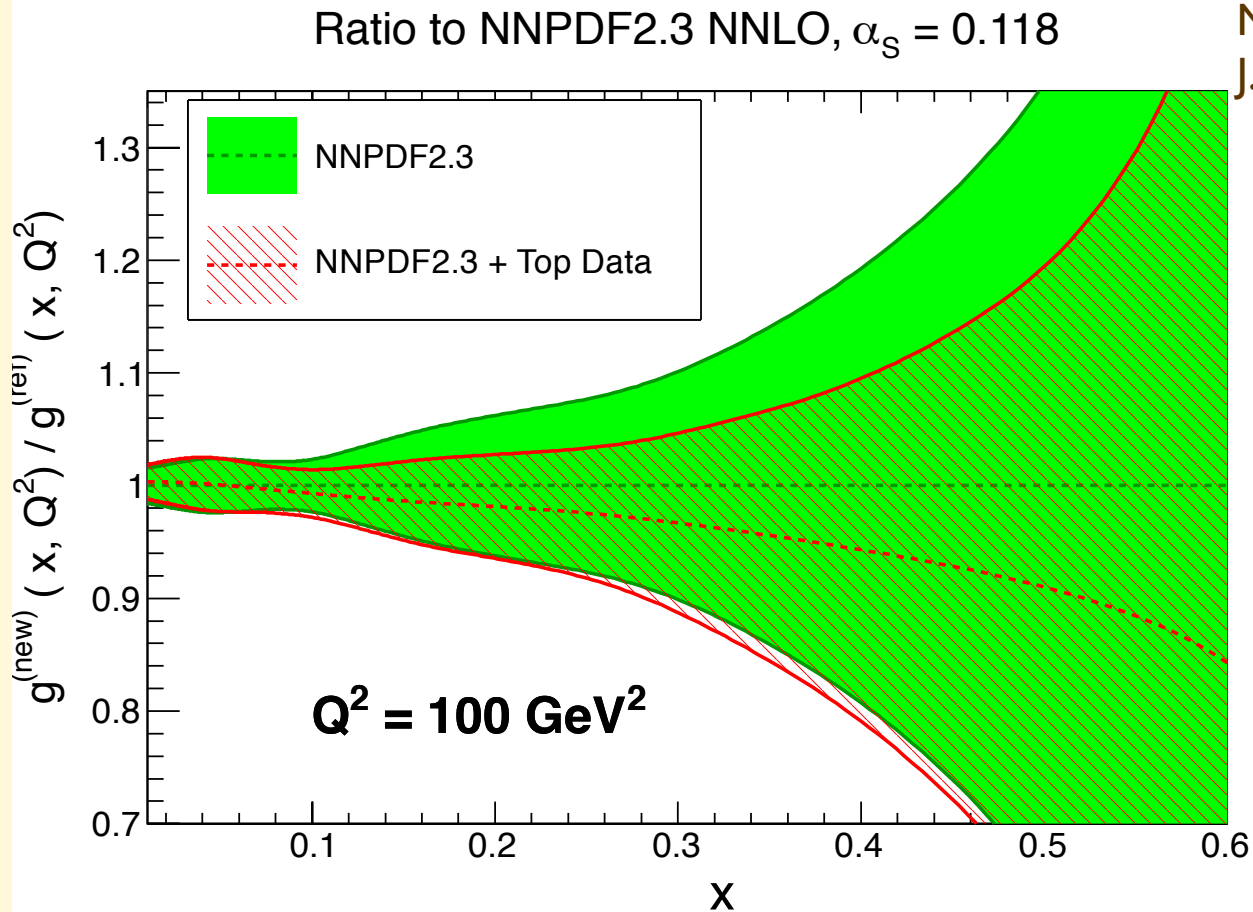


## TH and parametric uncertainties are all of similar size:

- **Scale:** Independent  $\mu_R$ ,  $\mu_F$  variation,  $\Rightarrow$  3%  
 $0.5 \mu_0 < \mu_{R,F} < 2 \mu_0$  at  $\mu_0 = m_{\text{top}}$ ,  
 with  $0.5 < \mu_R / \mu_F < 2$
- **PDF** (at 68%CL)  $\Rightarrow$  2-3%
- $\Delta\alpha_s = \pm 0.0007$   $\Rightarrow$  1.5%
- $\Delta m_{\text{top}} = \pm 1$  GeV  $\Rightarrow$  3%

# Constraining the gluon PDF with LHC $\sigma(t\bar{t})$

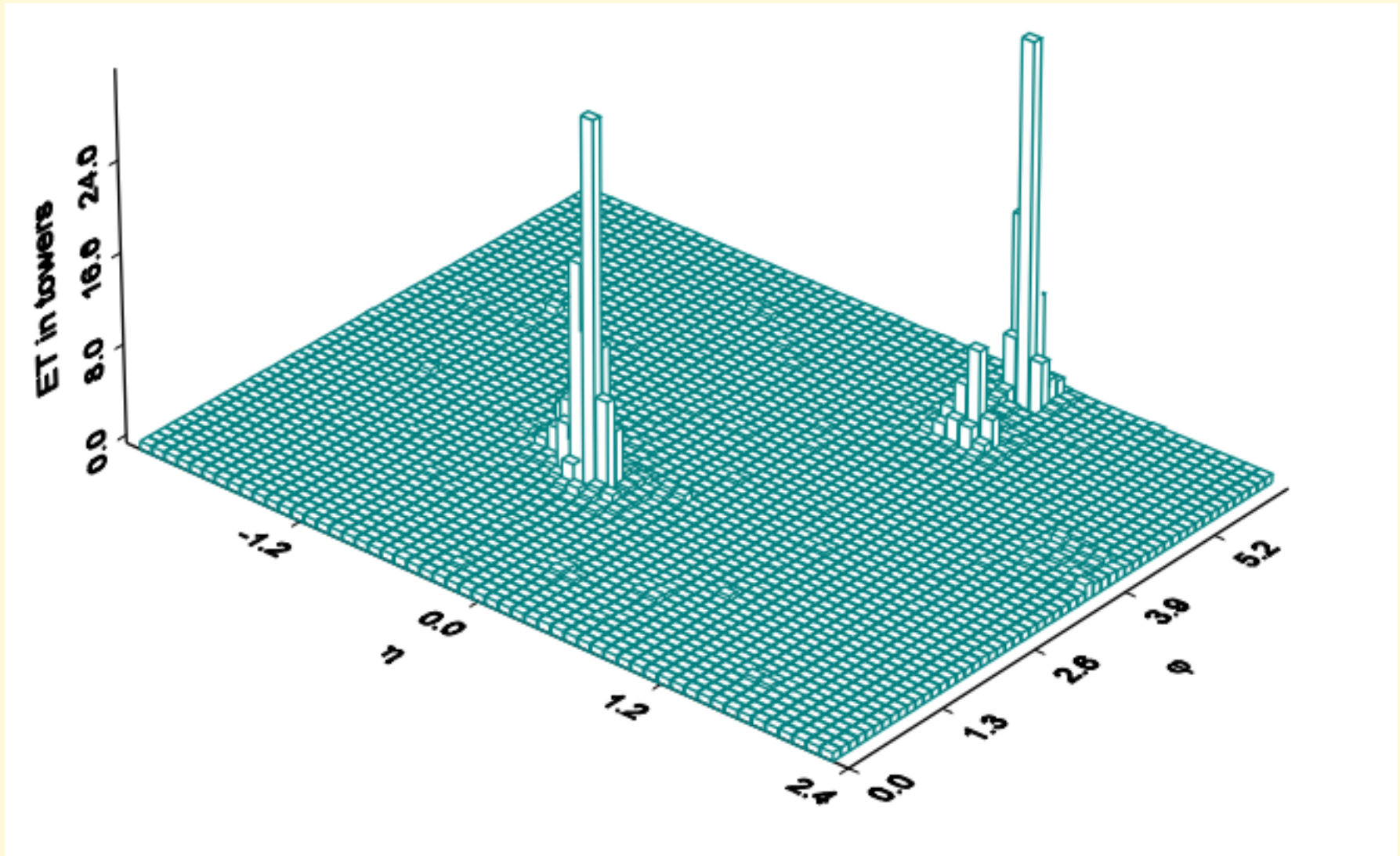
M. Czakon, MLM, A. Mitov,  
J. Rojo, arXiv:1303.7215



Collider	Ref	Ref+TeV	Ref +TeV+LHC7	Ref+TeV+LHC7+8
Tevatron	$7.26 \pm 0.12$	-	-	-
LHC 7 TeV	$172.5 \pm 5.2$	$172.7 \pm 5.1$	-	-
LHC 8 TeV	$247.8 \pm 6.6$	$248.0 \pm 6.5$	$245.0 \pm 4.6$	-
LHC 14 TeV	$976.5 \pm 16.4$	$976.2 \pm 16.3$	$969.8 \pm 12.0$	$969.6 \pm 11.6$

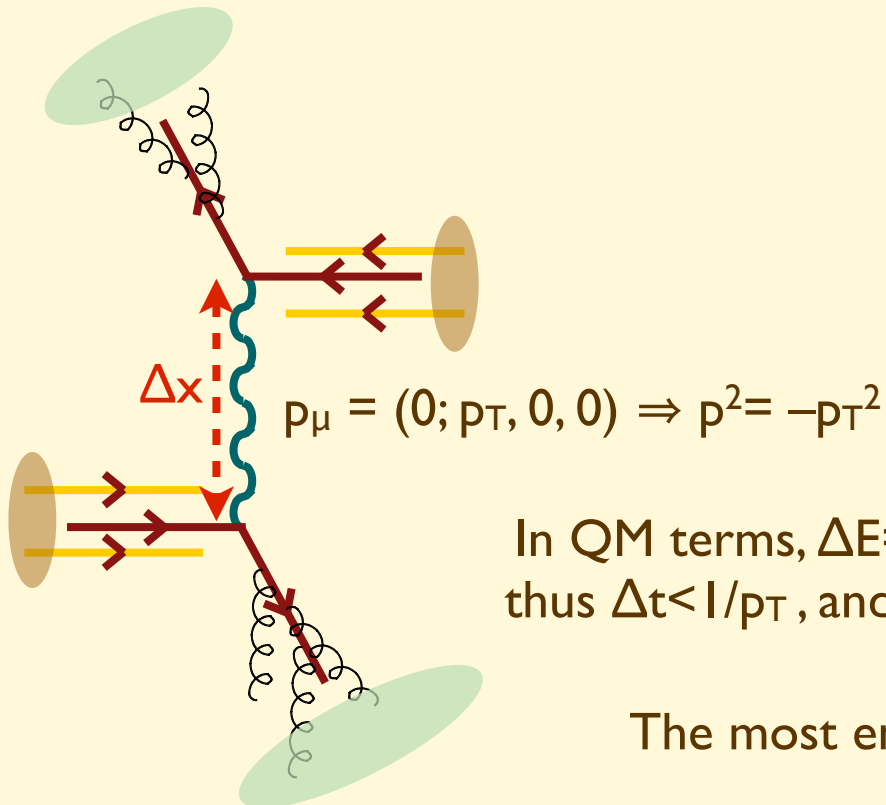
x-range relevant for  $gg \rightarrow H$  is smaller. Direct probe:  $d\sigma/dp_T(Z)$ , to be calculated at NNLO

# Jets in hadronic collisions



# Jets

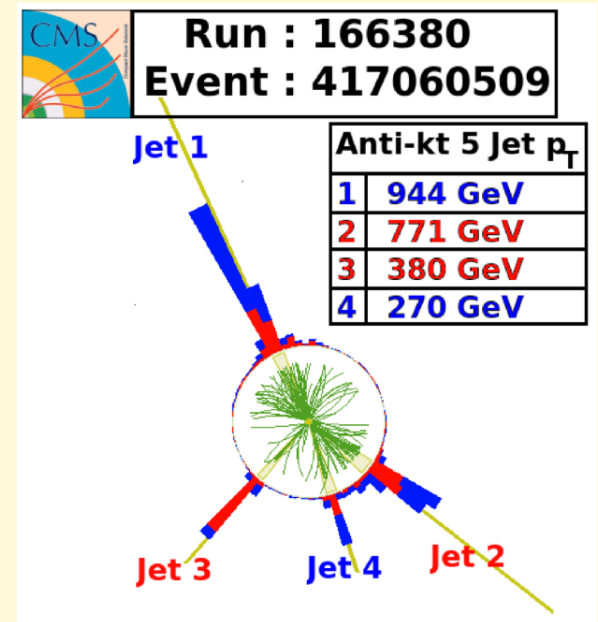
- Jet: focused stream of particles resulting from the evolution of a single accelerated quark or gluon
- Jet are used as probes of the quark structure (possible substructure implies departures from point-like behaviour of cross-section), or as probes of new particles (peaks in the invariant mass distribution of jet pairs)



In QM terms,  $\Delta E = p_T$ , and thus  $\Delta t < 1/p_T$ , and  $\Delta x < 1/p_T$

The most energetic jets observed at the LHC have  $p_T \sim 2 \text{ TeV}$

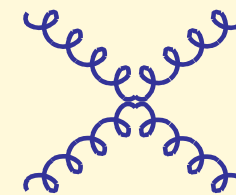
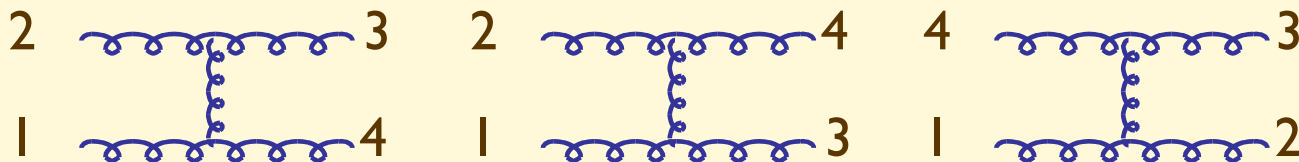
$\Rightarrow \Delta x \sim 10^{-4}$  of  $R_{\text{proton}} \sim 10^{-17} \text{ cm} \sim 1 \text{ n}\text{\AA} \sim 10^{18} \text{ GHz}$



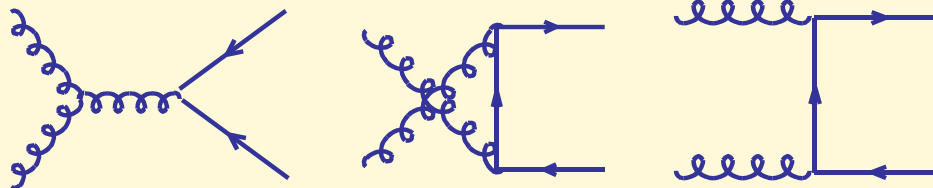
- Inclusive production of jets is the largest component of high- $Q$  phenomena in hadronic collisions
- QCD predictions are known up to NLO accuracy
- Intrinsic theoretical uncertainty (at NLO) is approximately 10%
- Uncertainty due to knowledge of parton densities varies from 5-10% (at low transverse momentum,  $p_T$  to 100% (at very high  $p_T$  corresponding to high- $x$  gluons)
- Jet are used as probes of the quark structure (possible substructure implies departures from point-like behaviour of cross-section), or as probes of new particles (peaks in the invariant mass distribution of jet pairs)



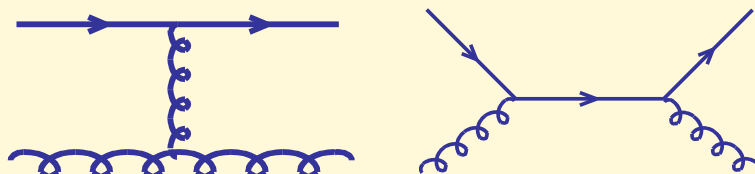
$gg \rightarrow gg$



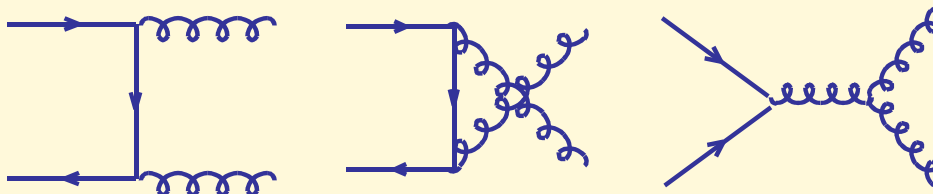
$gg \rightarrow q\bar{q}$



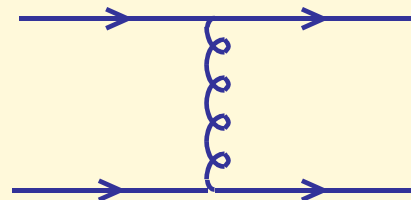
$qg \rightarrow qg$



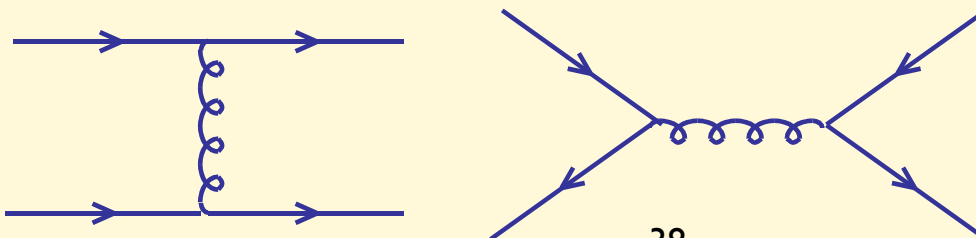
$q\bar{q} \rightarrow gg$



$qq' \rightarrow qq'$



$q\bar{q} \rightarrow q\bar{q}$



# Phase space and cross-section for LO jet production

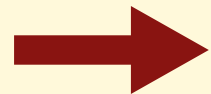
$$d[PS] = \frac{d^3 p_1}{(2\pi)^2 2p_1^0} \frac{d^3 p_2}{(2\pi)^2 2p_2^0} (2\pi)^4 \delta^4(P_{in} - P_{out}) dx_1 dx_2$$

$$(a) \quad \delta(E_{in} - E_{out}) \delta(P_{in}^z - P_{out}^z) dx_1 dx_2 = \frac{1}{2E_{beam}^2}$$

$$(b) \quad \frac{dp^z}{p^0} = dy \equiv d\eta$$



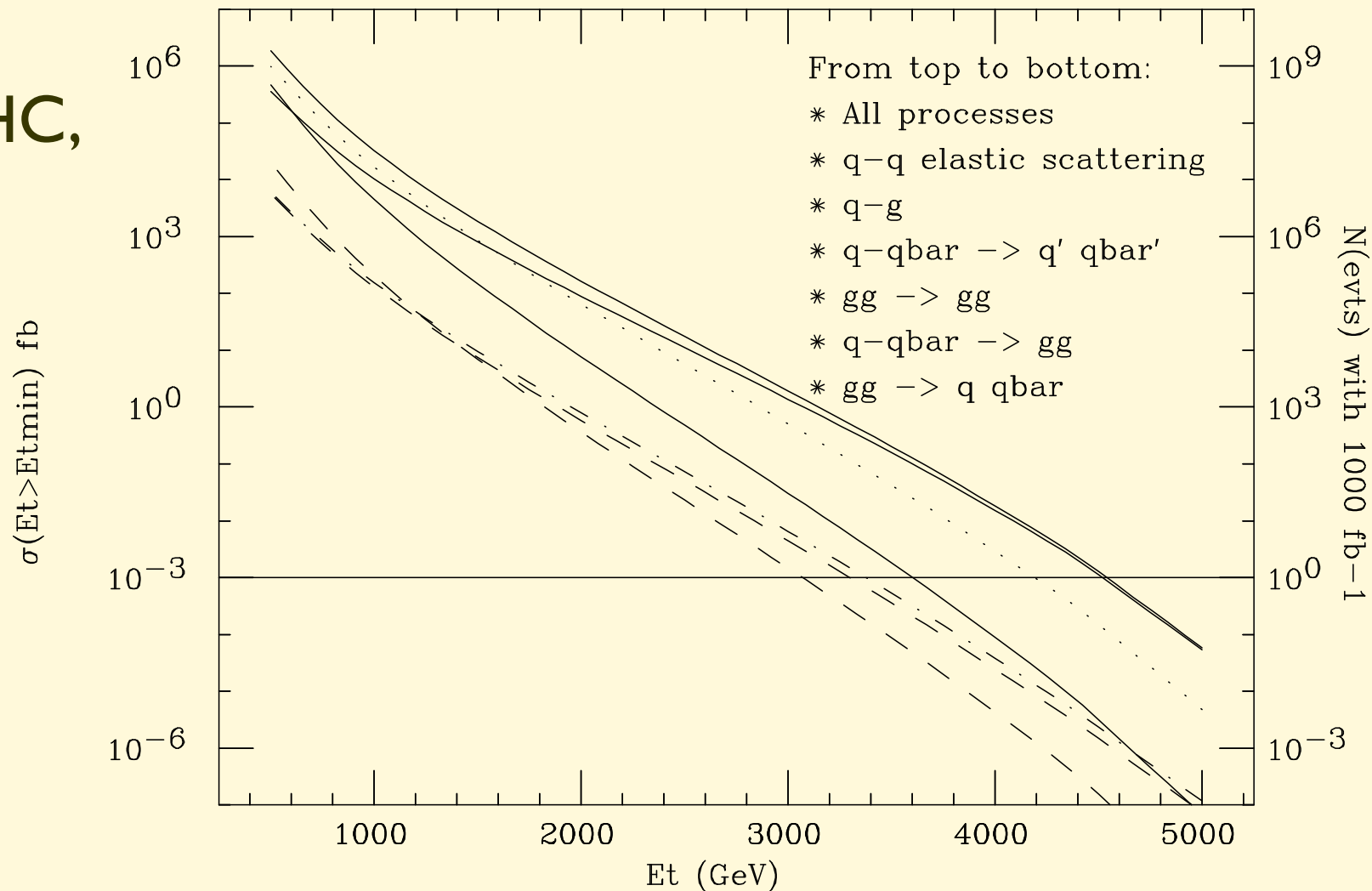
$$d[PS] = \frac{1}{4\pi S} p_T dp_T d\eta_1 d\eta_2$$



$$\frac{d^3 \sigma}{dp_T d\eta_1 d\eta_2} = \frac{p_T}{4\pi S} \sum_{i,j} f_i(x_1) f_j(x_2) \frac{1}{2\hat{s}} \sum_{kl} \overline{|M(ij \rightarrow kl)|^2}$$

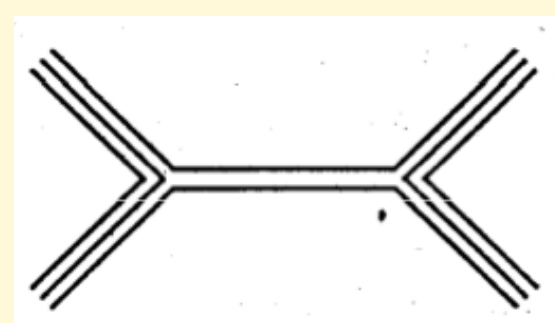
The measurement of  $p_T$  and rapidities for a dijet final state uniquely determines the parton momenta  $x_1$  and  $x_2$ . Knowledge of the partonic cross-section allows therefore the determination of partonic densities  $f(x)$

# Jet production rates at the LHC, subprocess composition



The presence of a quark substructure would manifest itself via contact interactions (as in Fermi's theory of weak interactions). On one side these new interactions would lead to an increase in cross-section, on the other they would affect the jets' angular distributions. In the dijet CMF, **QCD implies Rutherford law**, and extra point-like interactions can then be isolated using a fit. With the anticipated statistics of 300 fb-1, **limits on the scale of the new interactions in excess of 40 TeV should be reached** (to increase to 60 TeV with 3000 fb-1)

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**From the supercollider-bible of the 80's,**

**EHLQ (Eichten, Hinchliffe, Lane, Quigg):  
"Supercollider Physics",**

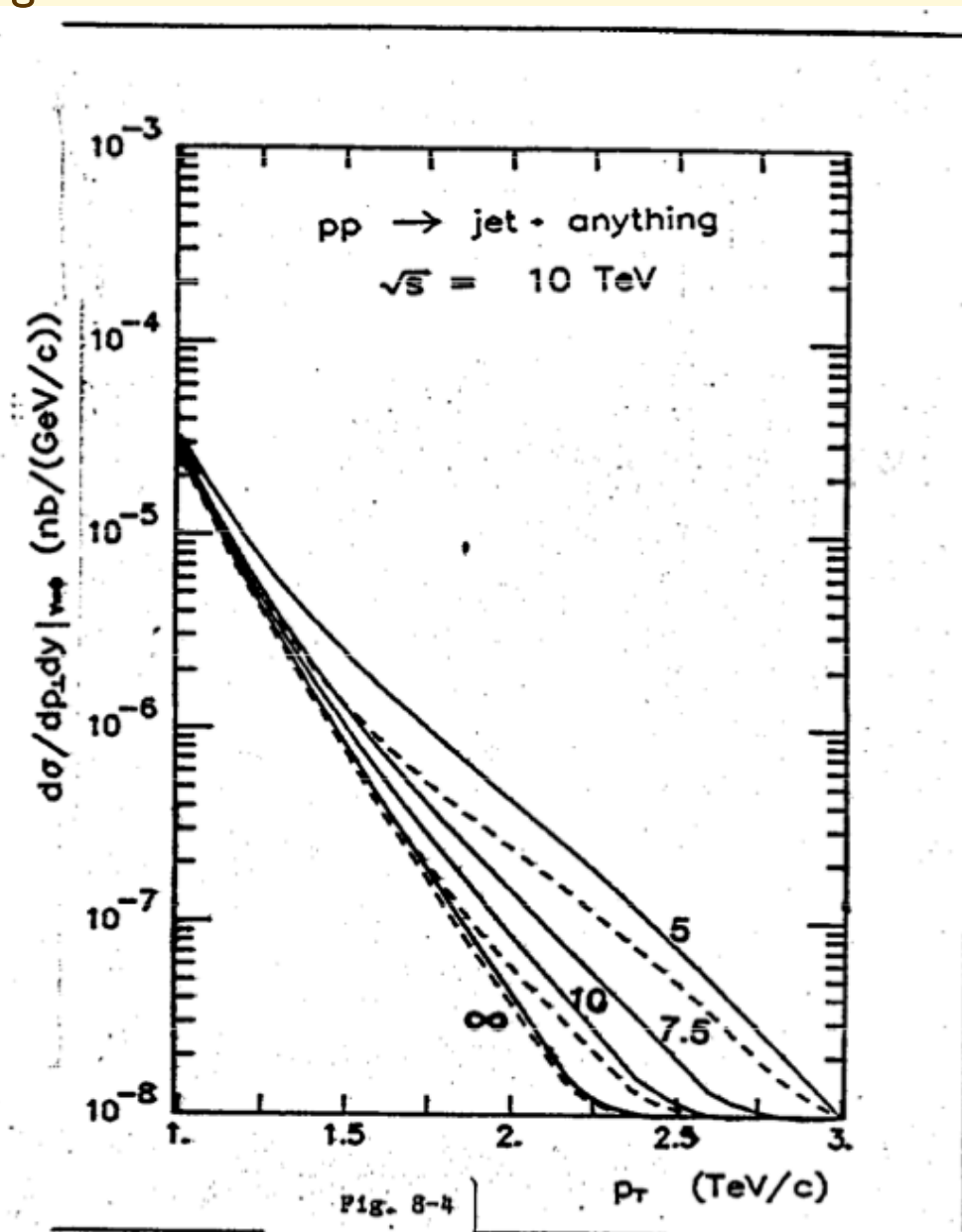
**Rev.Mod.Phys. 56 (1984) 579-707**

$$|A(u\bar{u} \rightarrow u\bar{u})|^2 = |A(d\bar{d} \rightarrow d\bar{d})|^2 =$$

$$\frac{4}{9} \alpha_s^2(Q^2) \left[ \frac{(\hat{u}^2 + \hat{s}^2)}{\hat{t}^2} + \frac{(\hat{u}^2 + \hat{t}^2)}{\hat{s}^2} - \frac{2}{3} \cdot \frac{\hat{u}^2}{\hat{s}\hat{t}} \right]$$

$$+ \frac{8}{9} \alpha_s(Q^2) \frac{\eta_0}{\Lambda^2} \left( \frac{\hat{u}^2}{\hat{t}} + \frac{\hat{u}^2}{\hat{s}} \right) + \frac{8}{3} \left( \frac{\eta_0 \hat{u}}{\Lambda^2} \right)^2;$$

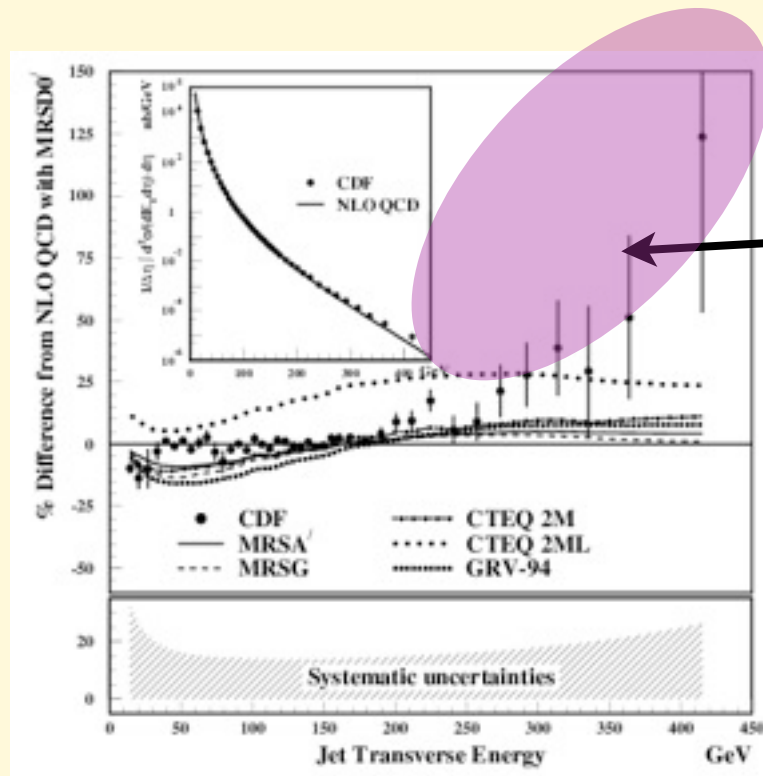
At the LHC, with the anticipated statistics of 300 fb<sup>-1</sup>, limits on the scale of the new interactions in excess of 40 TeV should be reached (to increase to 60 TeV with 3000 fb<sup>-1</sup>)



# Possible surprises from jet physics, an example from the past (1995)

## Analysis of large-ET jet production at the Tevatron

[ $QCD_{NLO} / \text{data} - 1$ ] (%)

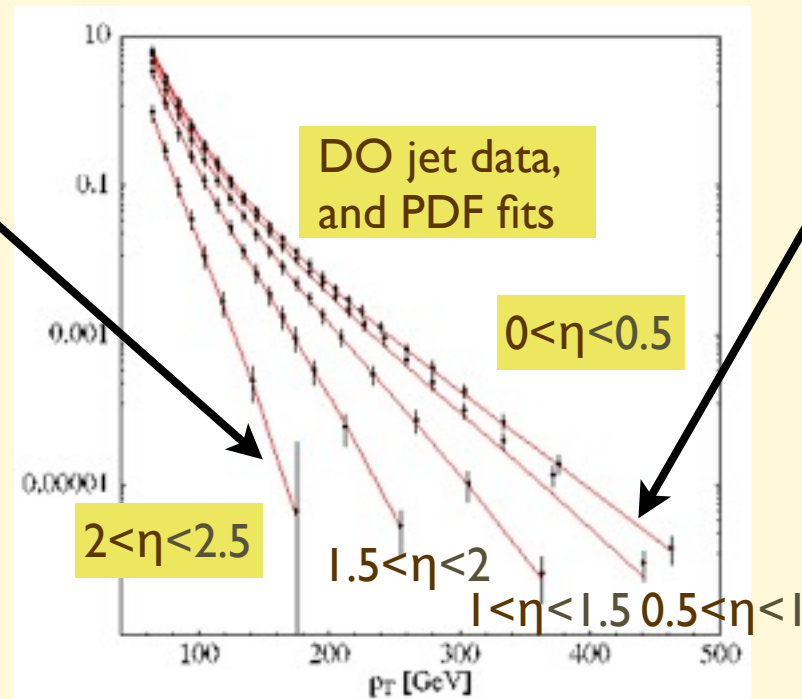
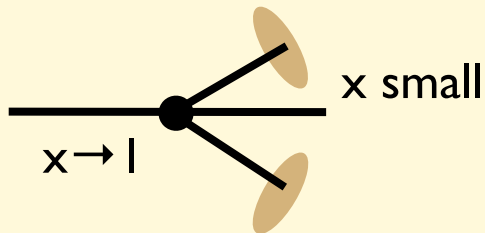


Large excess  $\Rightarrow$  **quark substructure ??**

**Effect later understood as poor knowledge/  
parameterization of the gluon density of the proton at  
 $x \rightarrow 1$ , using asymmetric, low-ET final states:**

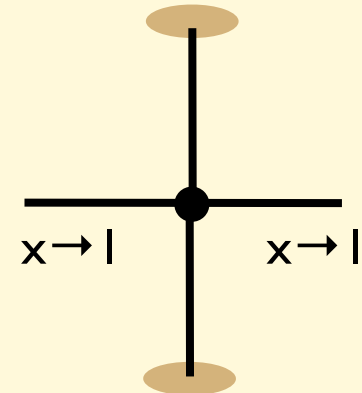
### Control region

fwd jets - low ET, small  $\sqrt{s}$ ,  
no BSM “contamination”,  
extract large- $x$  PDF

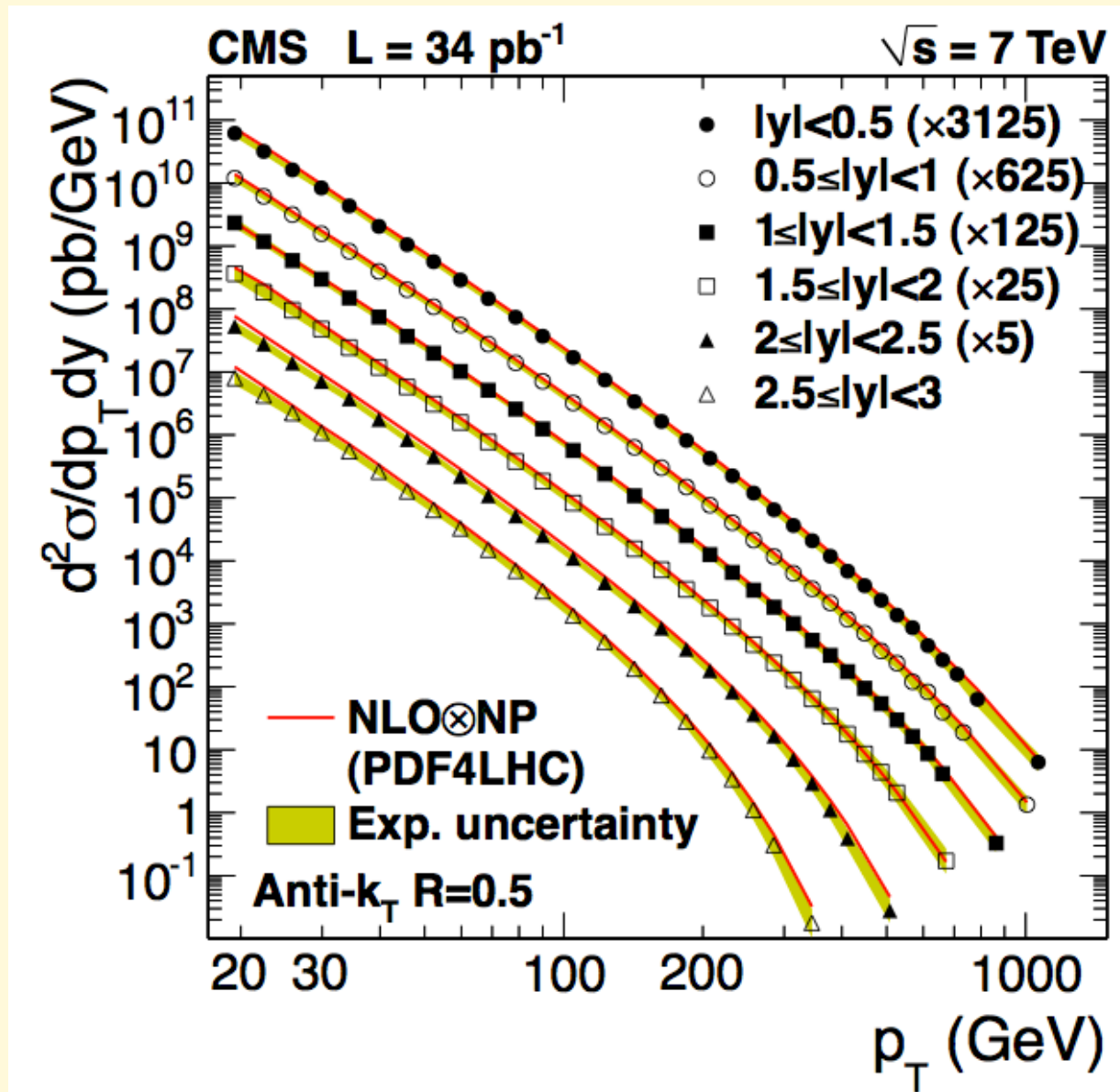


### Signal region

central jets - high ET, large  
 $\sqrt{s}$ , explore quark  
substructure



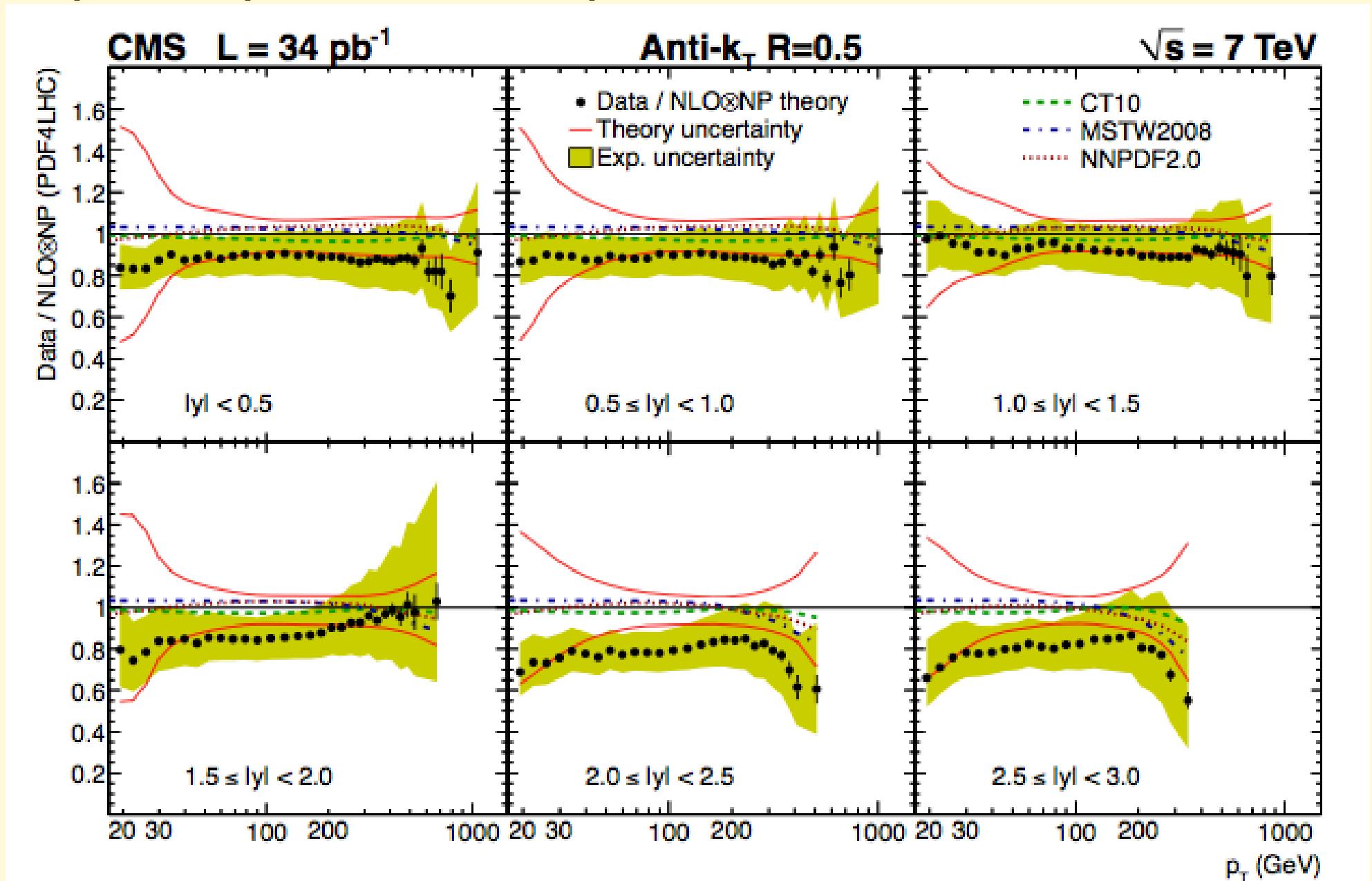
# Jet production at the LHC, data vs TH



**Rates span 10 orders of magnitude!**

# Jet cross section: data vs NLO

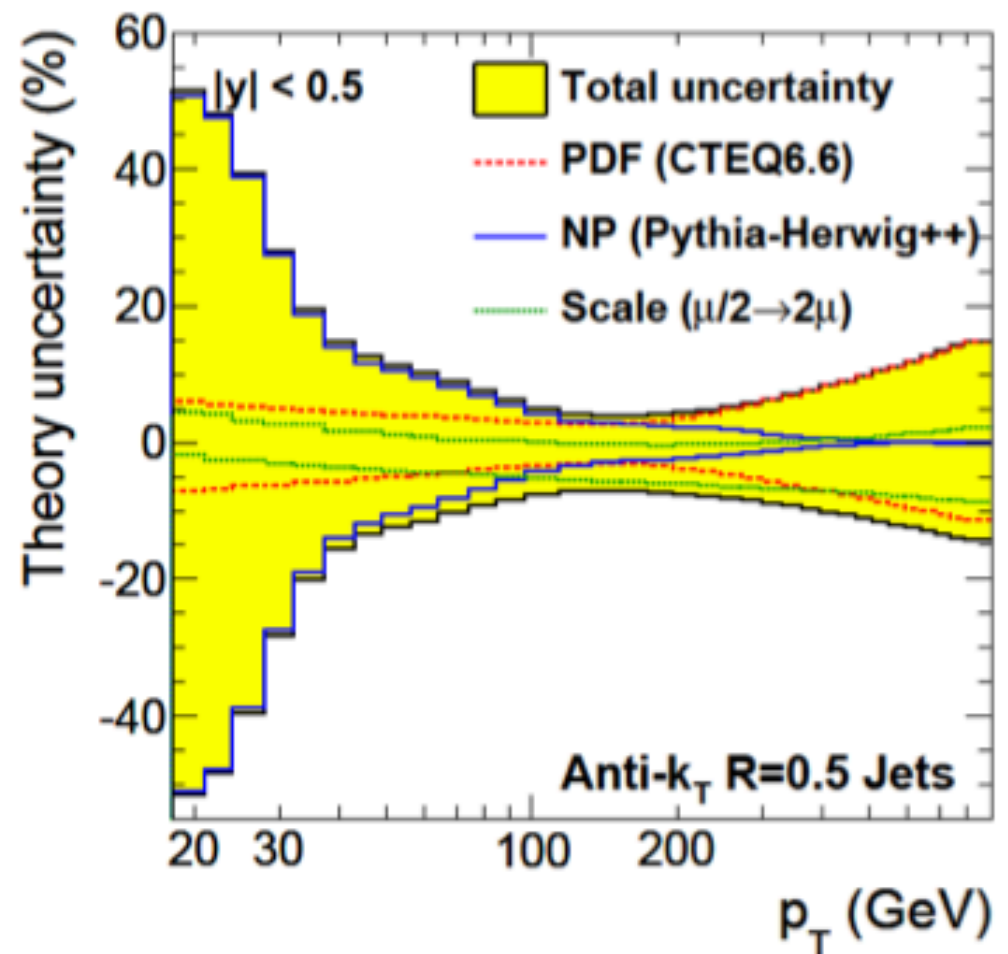
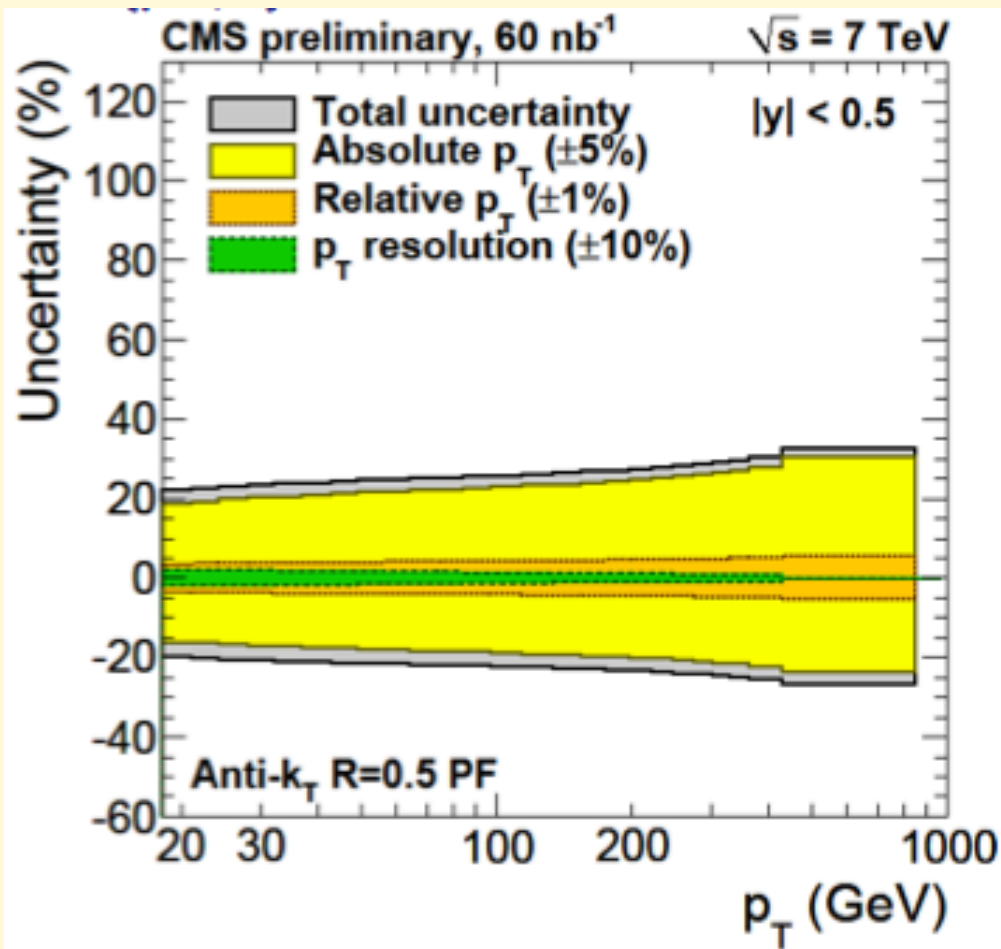
Theory: absolute prediction for both shape and normalization



Agreement to within 20% (over 10 orders of magnitude!)

Residual discrepancy consistent with PDF and perturbative NLO uncertainties

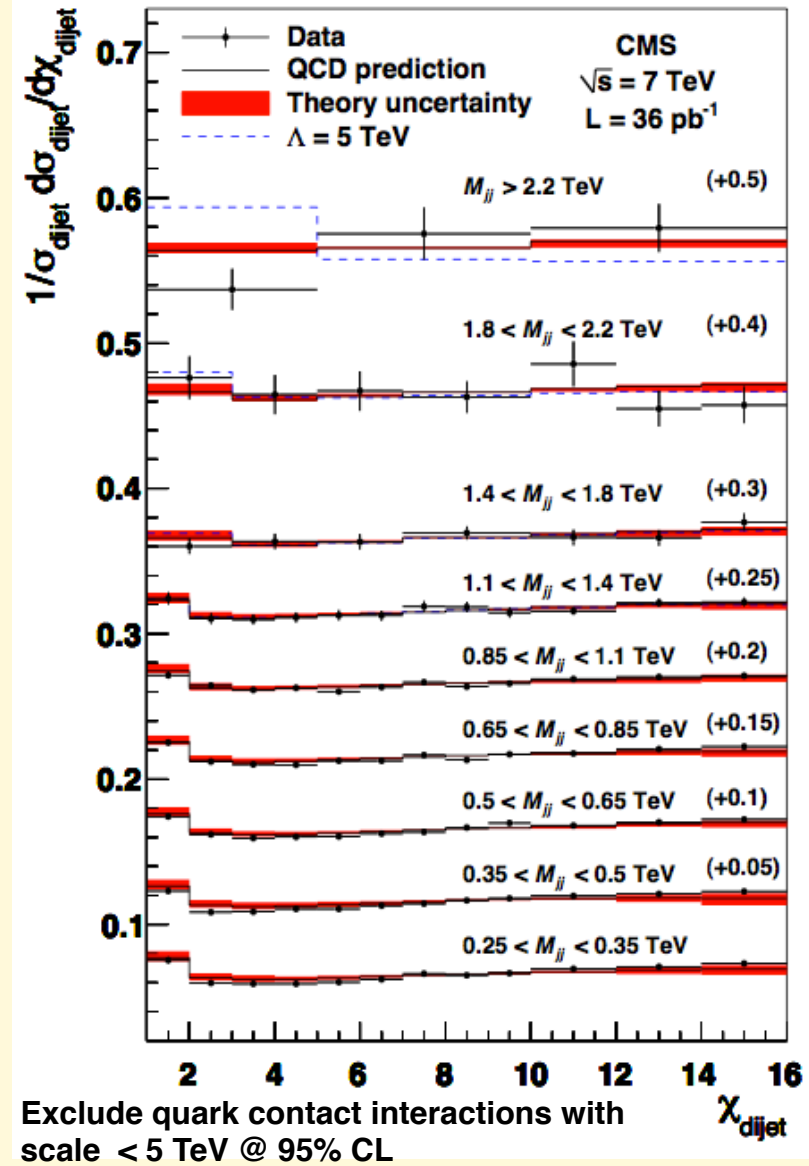
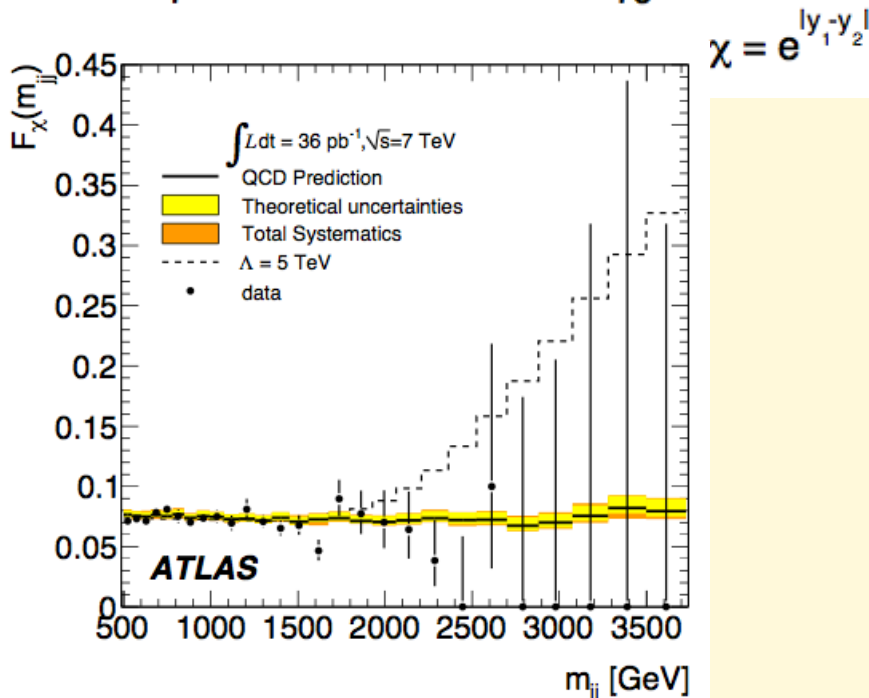
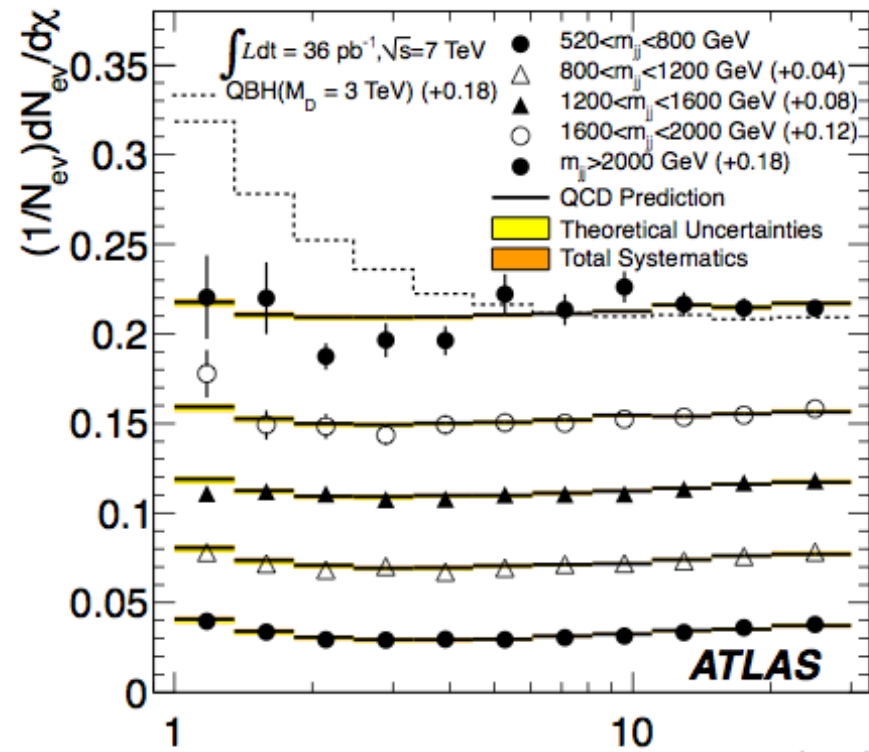




**PDF will be dominant source of theoretical systematics at large  $E_T$**

# Constraints on quark contact interactions

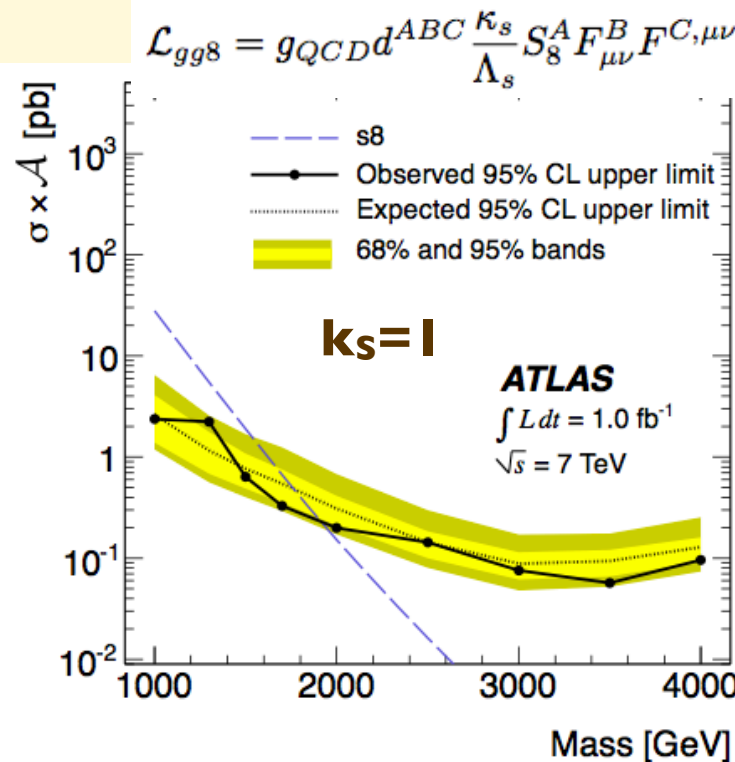
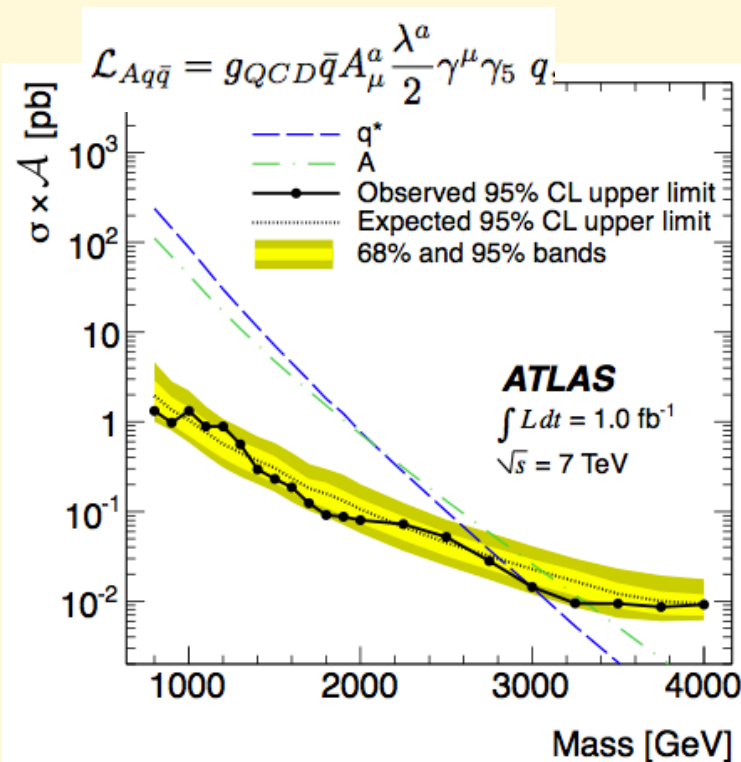
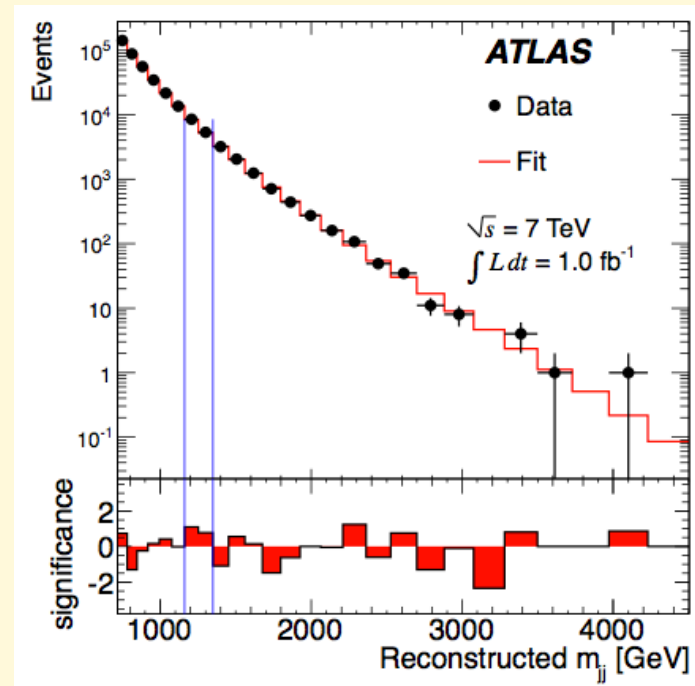
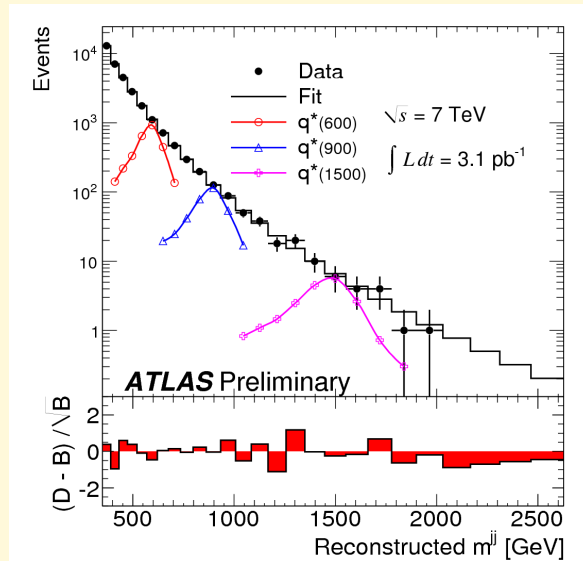
$$\chi = \frac{1 + |\cos \theta^*|}{1 - |\cos \theta^*|}$$



Quarks appear pointlike even at the distances probed by the LHC

# Dijet resonance searches

ATLAS: arXiv:1108.6311



No evidence for forces acting on quarks in addition to the SM ones

Model	95% CL Limits (TeV)	
	Expected	Observed
Excited Quark $q^*$	2.81	2.99
Axigluon	3.07	3.32
Colour Octet Scalar	1.77	1.92

**A useful ref:**

**Hard Interactions of Quarks and Gluons:  
a Primer for LHC Physics**

**<http://arXiv.org/abs/hep-ph/0611148>**