## Standard Model (backgrounds) at the LHC

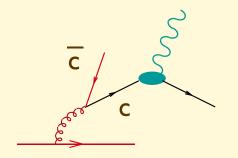
(part 2)

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# Exercise: charm in the proton



$$\frac{dc(x,Q)}{dt} = \frac{\alpha_s}{2\pi} \int_x^1 \frac{dy}{y} g(y,Q) P_{qg}(\frac{x}{y})$$

Assuming a typical behaviour of the gluon density:  $g(x,Q) \sim A/x$ 

and using 
$$P_{qg}(x) = \frac{1}{2} [x^2 + (1-x)^2]$$
 we get:

$$\frac{dc(x,Q)}{dt} = \frac{\alpha_s}{2\pi} \int_x^1 \frac{dy}{y} g(x/y,Q) P_{qg}(y) = \frac{\alpha_s}{2\pi} \int_x^1 dy \frac{A}{x} \frac{1}{2} [y^2 + (1-y)^2] = \frac{\alpha_s}{6\pi} \frac{A}{x}$$

and therefore:

$$c(x,Q) \sim \frac{\alpha_s}{6\pi} \log(\frac{Q^2}{m_c^2}) g(x,Q)$$

Corrections to this simple formula will arise due to the Q dependence of g(x) and of  $\alpha s$ 

## Evolution of hadronic final states

Asymptotic freedom implies that at E<sub>CM</sub> >> I GeV

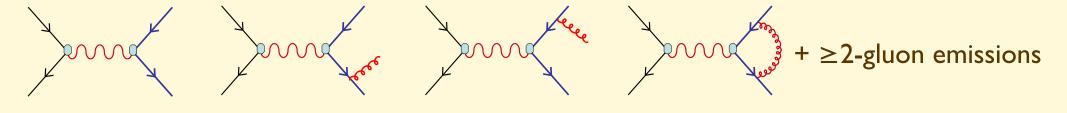
$$\sigma(e^+ e^- \rightarrow hadrons)$$
  $\sigma(e^+ e^- \rightarrow quarks/gluons)$ 

At the Leading Order (LO) in PT:

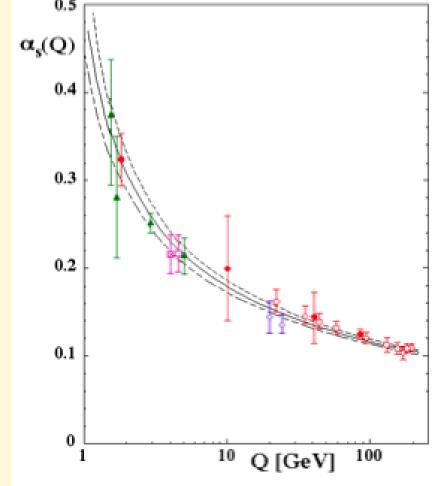
$$\sigma_0(e^+e^- o qq) = rac{4\pi\,lpha^2}{9_S}\,N_c\,\sum_{f=u,d,...}\,e_{q_J}^2$$

$$rac{\sigma_0(e^+e^- o qq)}{\sigma_0(e^+e^- o \mu^+\mu^-)} = N_c \sum_{f=u,d,...} e_{q_f}^2$$

#### Adding higher-order perturbative terms:



$$\sigma_1(e^+e^- \to qq(g)) = \sigma_0(e^+e^- \to qq) \left(1 + \frac{\alpha_s(E_{CM})}{\pi} + O(\alpha_s^2)\right)$$



O(3%) at Mz

Excellent agreement with data, provided N<sub>c</sub>=3

Extraction of  $\alpha$ s consistent with the Q evolution predicted by QCD

### To which extent the mapping

#### partons ⇔ particles

holds beyond the total cross section, e.g. for:

- momentum distributions
- angular distributions
- other kinematical correlations



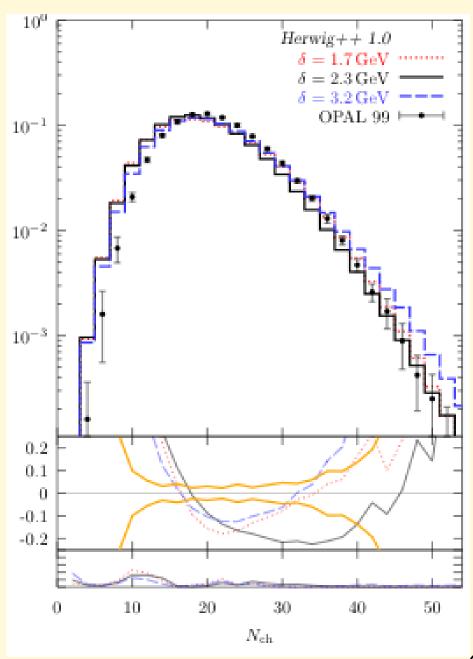
This is crucial to establish the connection between the physical observables, and the fundamental couplings of the underlying theory (e.g. to extract SUSY couplings, or to verify the spin of new particles, which are detected through hadronic final states)

Experimentally, the final states contain a large number of particles, not the 2 or 3 which apparently saturate the perturbative cross-section.

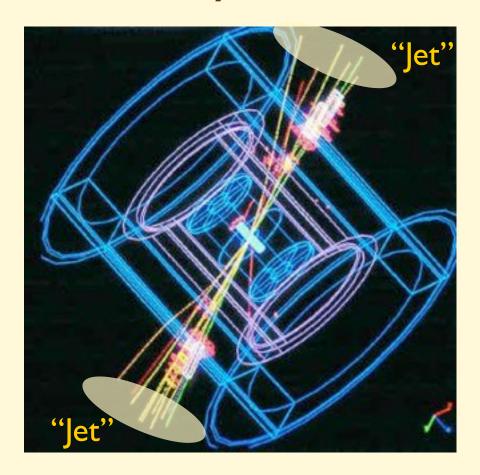
Experimental multiplicity distribution

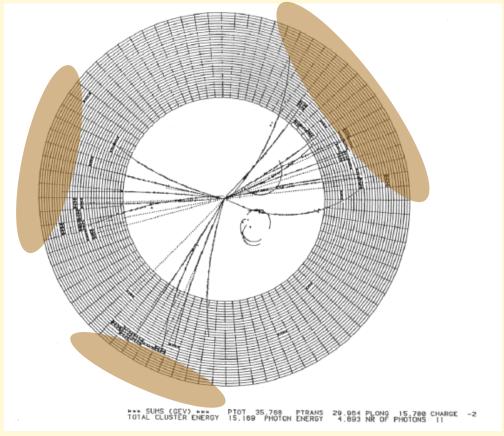
$$< n_{charged} > = 20.9$$

This appears to jeopardize the hope to use particles to learn about the initial properties of partons



#### Look more closely at the structure of these events:



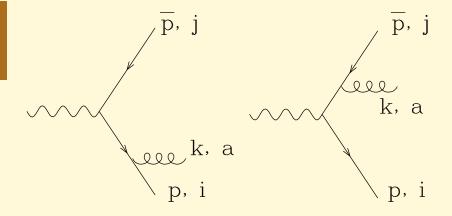


$$e^+ e^- \rightarrow qq \Rightarrow e^+ e^- \rightarrow 2 jets$$

$$e^+e^- \rightarrow qqg \Rightarrow e^+e^- \rightarrow 3 \text{ jets}$$

The puzzle appears to be solved by associating partons to collimated "jets" of hadrons

## Soft gluon emission



$$\begin{array}{lll} A & = & \bar{u}(p)\epsilon(k)(ig)\,\frac{-i}{\not\!p+\not\!k}\,\Gamma^\mu\,v(\bar{p})\,\,\lambda^a_{ij}\,+\,\bar{u}(p)\,\Gamma^\mu\,\frac{i}{\not\!p+\not\!k}\,(ig)\epsilon(k)\,v(\bar{p})\,\,\lambda^a_{ij} \\ \\ & = & \left[\frac{g}{2p\cdot k}\,\bar{u}(p)\epsilon(k)\,(\not\!p+\not\!k)\Gamma^\mu\,v(\bar{p})\,-\frac{g}{2\bar{p}\cdot k}\,\bar{u}(p)\,\Gamma^\mu\,(\not\!p+\not\!k)\epsilon(k)\,v(\bar{p})\right]\lambda^a_{ij} \end{array}$$

 $p \cdot k = p_0 k_0 (1 - \cos \theta) \Rightarrow$  singularities for collinear  $(\cos \theta \rightarrow 1)$  or soft  $(k_0 \rightarrow 0)$  emission

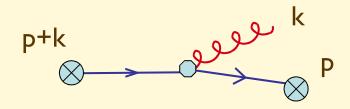
**Collinear emission** does not alter the global structure of the final state, since its preserves its "pencil-like-ness". **Soft emission** at large angle, however, could spoil the structure, and leads to strong interferences between emissions from different legs. So soft emission needs to be studied in more detail.

In the soft  $(k_0 \rightarrow 0)$  limit the amplitude simplifies and factorizes as follows:

$$A_{soft} = g\lambda_{ij}^{a} \left(\frac{p \cdot \varepsilon}{p \cdot k} - \frac{\overline{p} \cdot \varepsilon}{\overline{p} \cdot k}\right) A_{Born}$$

**Factorization:** it is the expression of the independence of long-wavelength (soft) emission on the nature of the hard (short-distance) process.

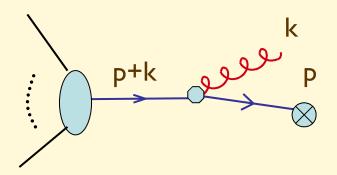
# Another simple derivation of soft-gluon emission rules



$$\psi(p)\gamma_{\mu}\psi(p+k)\varepsilon^{\mu}(k) \stackrel{k\to 0}{\to}$$

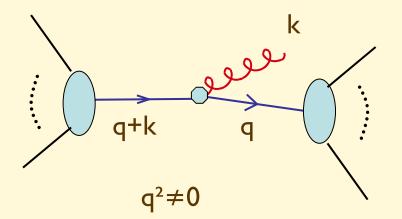
charge current of a free fermion

$$\psi(p)\gamma_{\mu}\psi(p)\varepsilon^{\mu}(k) = 2p \cdot \varepsilon$$



$$\frac{1}{\not p+\not k}\gamma_{\mu}\psi(p)\,\varepsilon^{\mu}(k) \quad \stackrel{k\to 0}{\to}$$

$$\frac{1}{2p \cdot k} \not p \gamma_{\mu} \psi(p) \varepsilon^{\mu}(k) = \frac{p \cdot \varepsilon}{p \cdot k} \psi(p)$$



$$\frac{1}{\sqrt{q}+\cancel{k}}\gamma_{\mu}\frac{1}{\sqrt{q}}\varepsilon^{\mu}(k) \stackrel{q^{2}\neq0,\ k\to0}{\longrightarrow} \frac{1}{q^{2}}\sqrt{q}\gamma_{\mu}\sqrt{q}\frac{1}{q^{2}}\varepsilon^{\mu}(k)$$

=> finite

<< Begin Exercise: Small-angle jet production, a useful approximation for the determination of the matrix elements and of the cross-section

At small scattering angle,  $t=(p_1-p_3)^2\sim (1-\cos\theta)\to 0$  and the  $1/t^2$  propagators associated with t-channel gluon exchange dominate the matrix elements for all <u>processes</u>. In this limit it is easy to evaluate the matrix

where we used the fact that, for k=p-p'<<p (small angle scattering),

$$u(p')\gamma_{\mu}u(p) \sim u(p)\gamma_{\mu}u(p) = 2p_{\mu}$$

Using our colour algebra results, we then get:  $\overline{\sum_{col,spin}} |M|^2 = \frac{1}{N_c^2} \frac{N_c^2 - 1}{4} \frac{4s^2}{t^2}$ 

Noting that the result must be symmetric under s↔u exchange, and setting

Nc=3, we finally obtain: 
$$\sum_{col,spin} |M|^2 = \frac{4}{9} \frac{s^2 + u^2}{t^2}$$

which turns out to be the exact result!

elements. For example:

<< Continue Exercise>>

## Quark-gluon and gluon-gluon scattering

We repeat the exercise in the more complex case of qg scattering, assuming the dominance of the t-channel gluon-exchange diagram:

c,k 
$$\sim f^{abc} \lambda^c_{ij} 2p_\mu \frac{1}{t} 2q_\mu = 2 \frac{s}{t} f^{abc} \lambda^c_{ij}$$

Using the colour algebra results, and enforcing the  $s \leftrightarrow u$  symmetry, we get:

$$\sum_{col,spin} |M|^2 = \frac{s^2 + u^2}{t^2}$$

which differs by only 20% from the exact result  $\sum_{col,spin} |M|^2 = \frac{s^2 + u^2}{t^2} - \frac{4s^2 + u^2}{9us}$  even in the large-angle region, at 90°

$$\sum_{col.spin} |M|^2 = \frac{s^2 + u^2}{t^2} - \frac{4s^2 + u^2}{9us}$$

In a similar way we obtain for gg scattering (using the t↔u symmetry):

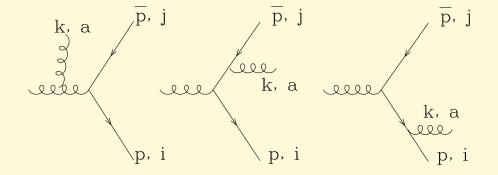
$$\sum_{col,spin} |M(gg \to gg)|^2 = \frac{9}{2} \left( \frac{s^2}{t^2} + \frac{s^2}{u^2} \right)$$

compared to the exact result

gg metry): 
$$\frac{1}{col,spin} |M(gg \to gg)|^2 = \frac{9}{2} \left( \frac{s^2}{t^2} + \frac{s^2}{u^2} \right)$$
  
 $\frac{1}{col,spin} |M(gg \to gg)|^2 = \frac{9}{2} \left( 3 - \frac{ut}{s^2} - \frac{us}{t^2} - \frac{st}{u^2} \right)$ 

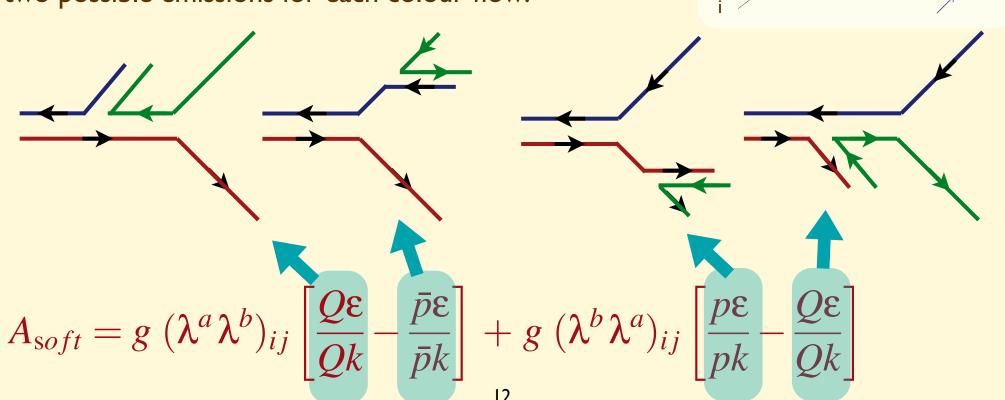
with a 20% difference at 90°

Similar, but more structured, result in the case of a fully coloured process:

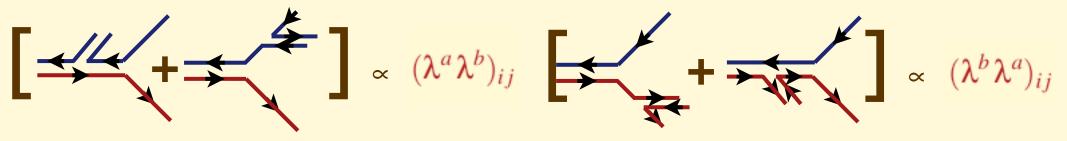


$$A_{soft} = g (\lambda^a \lambda^b)_{ij} \left[ \frac{Q \varepsilon}{Q k} - \frac{\bar{p} \varepsilon}{\bar{p} k} \right] + g (\lambda^b \lambda^a)_{ij} \left[ \frac{p \varepsilon}{p k} - \frac{Q \varepsilon}{Q k} \right]$$

The four terms correspond to the two possible ways colour can flow, and to the two possible emissions for each colour flow:



The interference between the two colour structures



is suppressed by  $I/N_c^2$ :

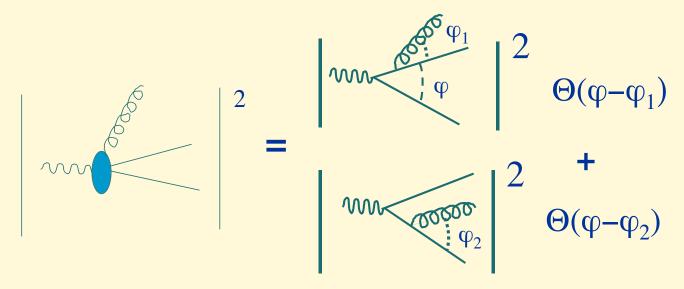
$$\sum_{a,b,i,j} |(\lambda^a \lambda^b)_{ij}|^2 = \sum_{a,b} tr \left(\lambda^a \lambda^b \lambda^b \lambda^a\right) = \frac{N^2 - 1}{2} C_F = O(N^3)$$

$$\sum_{a,b,i,j} (\lambda^a \lambda^b)_{ij} [(\lambda^b \lambda^a)_{ij}]^* = \sum_{a,b} tr(\lambda^a \lambda^b \lambda^a \lambda^b) = \frac{N^2 - 1}{2} \underbrace{(C_F - \frac{C_A}{2})}_{-\frac{1}{2N}} = O(N)$$

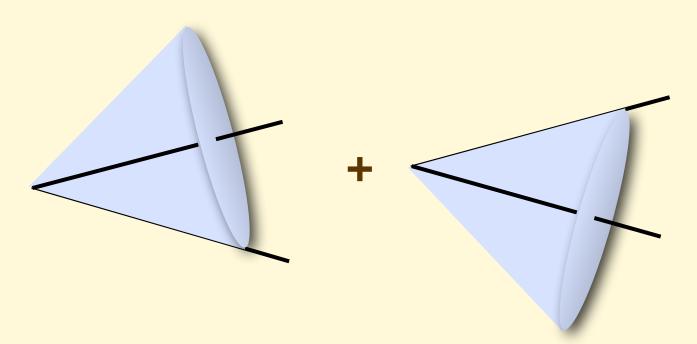
As a result, the emission of a soft gluon can be described, to the leading order in  $I/N_c^2$ , as the incoherent sum of the emission from the two colour currents

What about the interference between the two diagrams corresponding to the same colour flow?

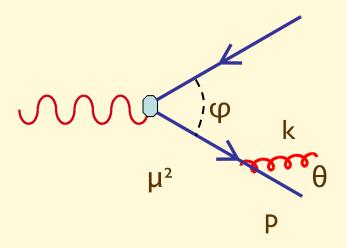
# Angular ordering



Radiation inside the cones is allowed, and described by the eikonal probability, radiation outside the cones is suppressed and averages to 0 when integrated over the full azimuth



## An intuitive explanation of angular ordering



Lifetime of the virtual intermediate state:

$$\tau < \gamma/\mu = E/\mu^2 = I/(k_0\theta^2) = I/(k_\perp\theta)$$

$$\mu^2 = (p+k)^2 = 2E k_0 (I-\cos\theta)$$

$$\sim E k_0 \theta^2 \sim E k_\perp \theta$$

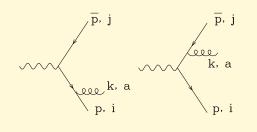
Distance between q and qbar after T:

$$d = \varphi \tau = (\varphi/\theta) I/k \perp$$

If the transverse wavelength of the emitted gluon is longer than the separation between q and qbar, the gluon emission is suppressed, because the q qbar system will appear as colour neutral (=> dipole-like emission, suppressed)

Therefore  $d > 1/k \perp$ , which implies

## The formal proof of angular ordering



$$d\sigma_{g} = \sum |A_{soft}|^{2} \frac{d^{3}k}{(2\pi)^{3}2k^{0}} \sum |A_{0}|^{2} \frac{-2p^{\mu}p^{\nu}}{(pk)(pk)} g^{2} \sum \varepsilon_{\mu} \varepsilon_{\nu}^{*} \frac{d^{3}k}{(2\pi)^{3}2k^{0}}$$

$$= d\sigma_{0} \frac{\alpha_{s}C_{F}}{\pi} \frac{dk^{0}}{k^{0}} \frac{d\phi}{2\pi} \frac{1 - \cos\theta_{ij}}{(1 - \cos\theta_{ik})(1 - \cos\theta_{jk})} d\cos\theta$$

You can easily prove that:

$$\frac{1-\cos\theta_{ij}}{(1-\cos\theta_{ik})(1-\cos\theta_{jk})} = \frac{1}{2} \left[ \frac{\cos\theta_{jk} - \cos\theta_{ij}}{(1-\cos\theta_{ik})(1-\cos\theta_{jk})} + \frac{1}{1-\cos\theta_{ik}} \right] + \frac{1}{2} [i \leftrightarrow j] \equiv W_{(i)} + W_{(j)}$$

where: 
$$W_{(i)} o finite \ if \ k \parallel j \ (\cos \theta_{jk} o 1) \ W_{(j)} o finite \ if \ k \parallel i \ (\cos \theta_{ik} o 1)$$

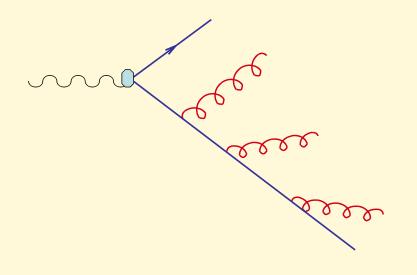
The probabilistic interpretation of W(i) and W(j) is a priori spoiled by their nonpositivity. However, you can prove that after azimuthal averaging:

$$= \frac{2}{\sqrt{2}} \left[ \begin{array}{c|c} 2 & -\sqrt{2} & -\sqrt{2} \\ -\sqrt{2} & -\sqrt{2} \\ -\sqrt{2} & -\sqrt{2} \end{array} \right] \left[ \begin{array}{c|c} 2 & -\sqrt{2} \\ -\sqrt{2} & -\sqrt{2} \end{array} \right] \left[ \begin{array}{c|c} 2 & -\sqrt{2} \\ -\sqrt{2} & -\sqrt{2} \end{array} \right] \left[ \begin{array}{c|c} 2 & -\sqrt{2} \\ -\sqrt{2} & -\sqrt{2} \end{array} \right] \left[ \begin{array}{c|c} 2 & -\sqrt{2} \\ -\sqrt{2} & -\sqrt{2} \end{array} \right] \left[ \begin{array}{c|c} 2 & -\sqrt{2} \\ -\sqrt{2} & -\sqrt{2} \end{array} \right] \left[ \begin{array}{c|c} 2 & -\sqrt{2} \\ -\sqrt{2} & -\sqrt{2} \end{array} \right] \left[ \begin{array}{c|c} 2 & -\sqrt{2} \\ -\sqrt{2} & -\sqrt{2} \end{array} \right] \left[ \begin{array}{c|c} 2 & -\sqrt{2} \\ -\sqrt{2} & -\sqrt{2} \end{array} \right] \left[ \begin{array}{c|c} 2 & -\sqrt{2} \\ -\sqrt{2} & -\sqrt{2} \end{array} \right] \left[ \begin{array}{c|c} 2 & -\sqrt{2} \\ -\sqrt{2} & -\sqrt{2} \end{array} \right] \left[ \begin{array}{c|c} 2 & -\sqrt{2} \\ -\sqrt{2} & -\sqrt{2} \end{array} \right] \left[ \begin{array}{c|c} 2 & -\sqrt{2} \\ -\sqrt{2} & -\sqrt{2} \end{array} \right] \left[ \begin{array}{c|c} 2 & -\sqrt{2} \\ -\sqrt{2} & -\sqrt{2} \end{array} \right] \left[ \begin{array}{c|c} 2 & -\sqrt{2} \\ -\sqrt{2} & -\sqrt{2} \end{array} \right] \left[ \begin{array}{c|c} 2 & -\sqrt{2} \\ -\sqrt{2} & -\sqrt{2} \end{array} \right] \left[ \begin{array}{c|c} 2 & -\sqrt{2} \\ -\sqrt{2} & -\sqrt{2} \end{array} \right] \left[ \begin{array}{c|c} 2 & -\sqrt{2} \\ -\sqrt{2} & -\sqrt{2} \end{array} \right] \left[ \begin{array}{c|c} 2 & -\sqrt{2} \\ -\sqrt{2} & -\sqrt{2} \end{array} \right] \left[ \begin{array}{c|c} 2 & -\sqrt{2} \\ -\sqrt{2} & -\sqrt{2} \end{array} \right] \left[ \begin{array}{c|c} 2 & -\sqrt{2} \\ -\sqrt{2} & -\sqrt{2} \end{array} \right] \left[ \begin{array}{c|c} 2 & -\sqrt{2} \\ -\sqrt{2} & -\sqrt{2} \end{array} \right] \left[ \begin{array}{c|c} 2 & -\sqrt{2} \\ -\sqrt{2} & -\sqrt{2} \end{array} \right] \left[ \begin{array}{c|c} 2 & -\sqrt{2} \\ -\sqrt{2} & -\sqrt{2} \end{array} \right] \left[ \begin{array}{c|c} 2 & -\sqrt{2} \\ -\sqrt{2} & -\sqrt{2} \end{array} \right] \left[ \begin{array}{c|c} 2 & -\sqrt{2} \\ -\sqrt{2} & -\sqrt{2} \end{array} \right] \left[ \begin{array}{c|c} 2 & -\sqrt{2} \\ -\sqrt{2} & -\sqrt{2} \end{array} \right] \left[ \begin{array}{c|c} 2 & -\sqrt{2} \end{array} \right]$$

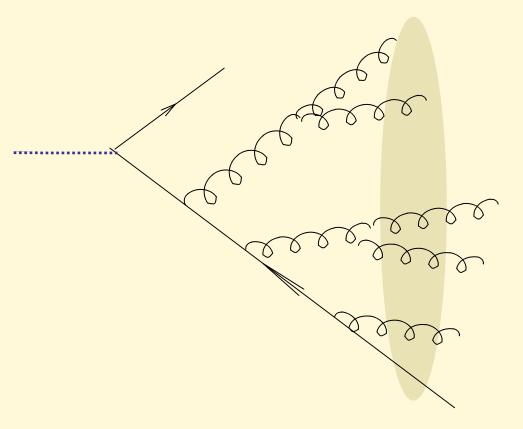
$$\int \frac{d\phi}{2\pi} W_{(i)} = \frac{1}{1 - \cos \theta_{ik}} \text{ if } \theta_{ik} < \theta_{ij} , \quad 0 \text{ otherwise}$$

$$\int \frac{d\phi}{2\pi} W_{(j)} = \frac{1}{1 - \cos \theta_{jk}} \text{ if } \theta_{jk} < \theta_{ij} , \quad 0 \text{ otherwise}$$

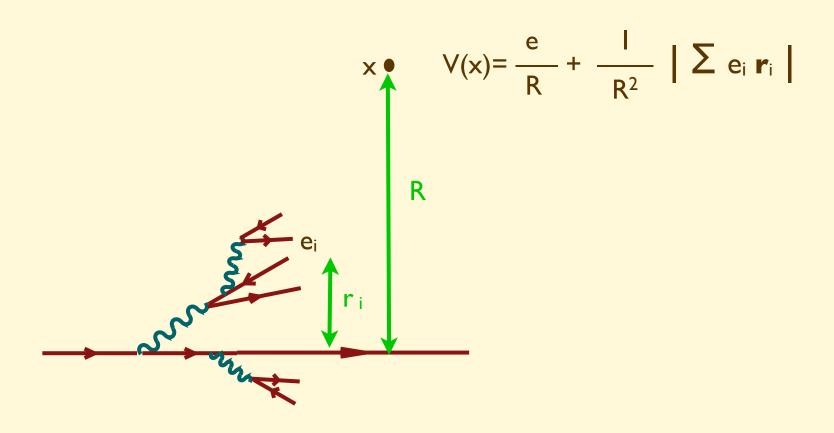
Further branchings will obey angular ordering relative to the new angles. As a result emission angles get smaller and smaller, squeezing the jet



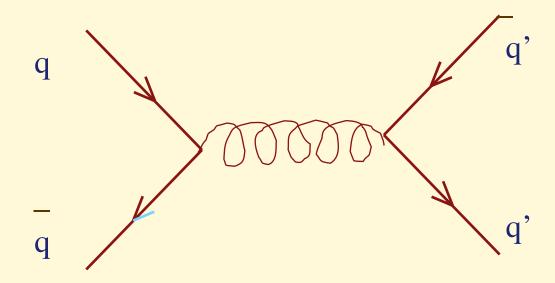
The construction can be iterated to the next emission, with the result that emission angles keep getting smaller and smaller => jet structure



Total colour charge of the system is equal to the quark colour charge. Treating the system as the incoherent superposition of N gluons would lead to artificial growth of gluon multiplicity. Angular ordering enforces coherence, and leads to the proper evolution with energy of particle multiplicities.



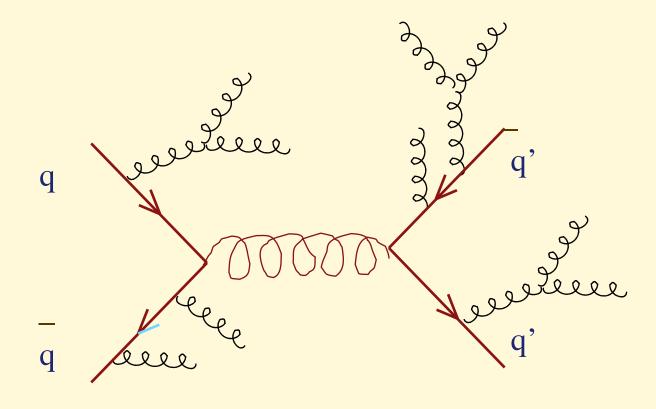
## I: Generate the parton-level hard event



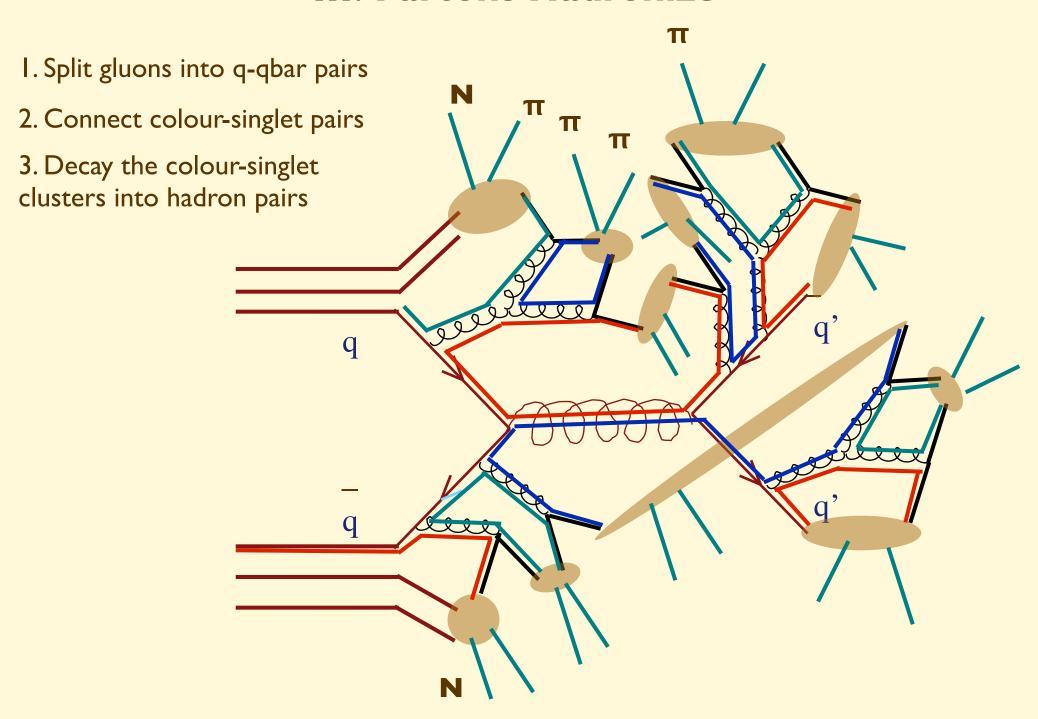
## II: Develop the parton shower

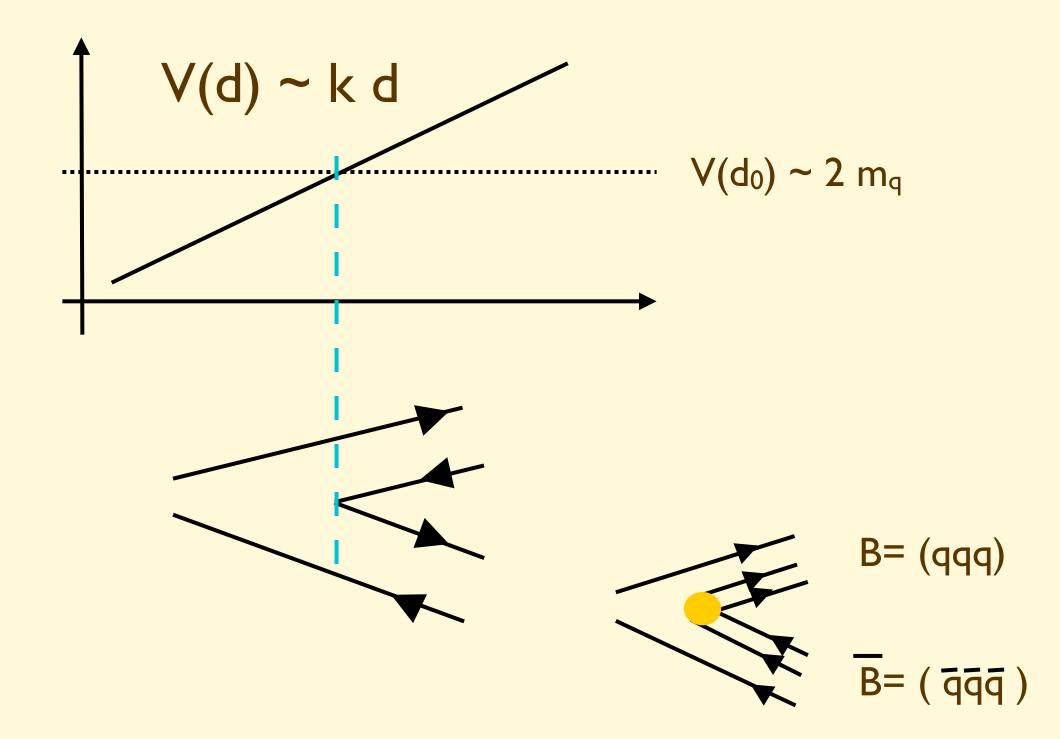
#### I. Final state

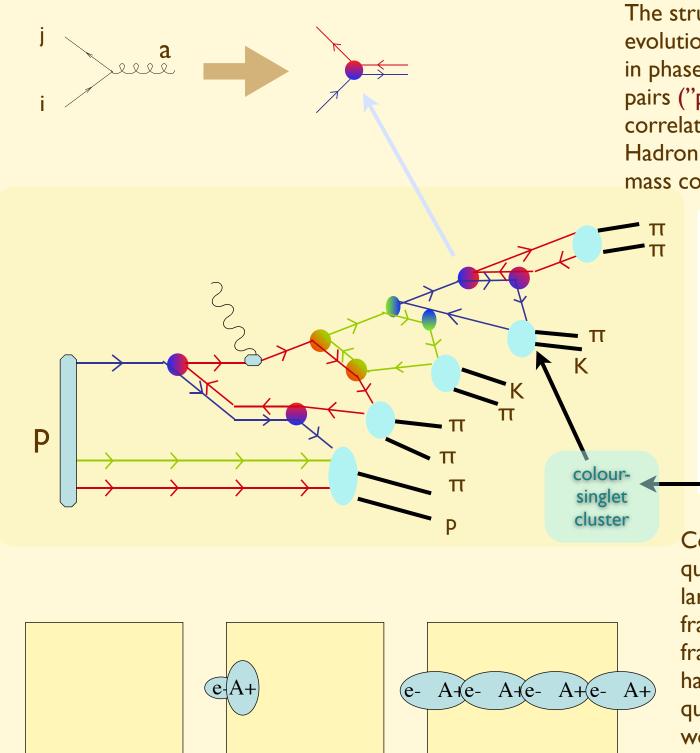
#### 2. Initial state



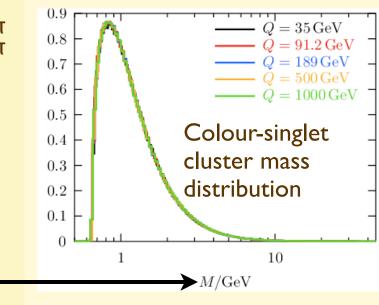
#### **III: Partons Hadronize**







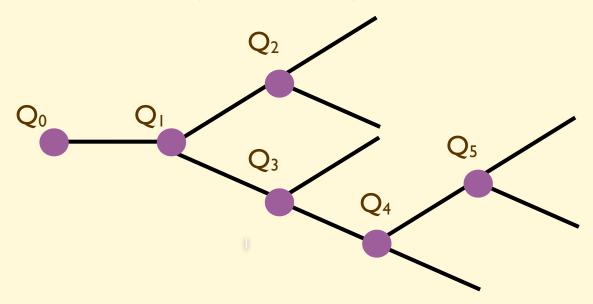
The structure of the perturbative evolution leads naturally to the clustering in phase-space of colour-singlet parton pairs ("preconfinement"). Long-range correlations are strongly suppressed. Hadronization will only act locally, on lowmass colour-singlet clusters.



Colour is left "behind" by the struck quark. The first soft gluon emitted at large angle will connect to the beam fragments, ensuring that the beam fragments can recombine to form hadrons, and will allow the struck quark to evolve without having to worry about what happens to the proton fragments.

# The shower algorithm

Sequential probabilistic evolution (Markov chain)

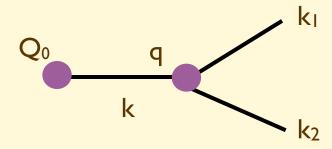


The probability of each emission only depends on the state of the splitting parton, and of the daughters. The QCD dynamics is encoded in these splitting probabilities.

The total probability of all possible evolutions is **I** (unitary evolution).

- The shower evolution does not change the event rate inherited from the parton level, matrix element computation.
- No K-factors from the shower, even though the shower describes higher-order corrections to the leading-order process

# Single emission



**q²** ≈ virtuality scale of the branching:

**z=P(k<sub>2</sub>)/P(k)**≈ energy/ momentum fraction carried by one of the two partons after splitting

$$\frac{d\operatorname{Prob}(Q_0 \to q^2)}{dq^2 dz d\phi} = P_0 \frac{\alpha_s(\mu)}{2\pi} \frac{1}{q^2} P(z)$$

- $(k_1 + k_2)^2$
- $\cdot k_1 \cdot k_2$
- **k**<sub>\(\\_\)</sub><sup>2</sup>
- ....
- P=k<sup>0</sup>
- P=k / /
- P=k / / +

K<sup>0</sup>

•

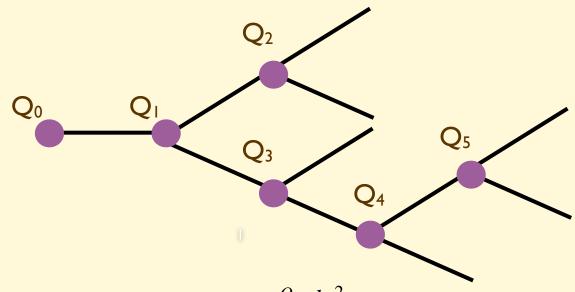
$$P_0 \Rightarrow \int d Prob = I$$

 $\phi$  = azimuth

$$\mu = f(z,q)$$

While at leading-logarithmic order (LL) all choices of evolution variables and of scale for  $\alpha$ s are equivalent, specific choices can lead to improved description of NLL effects and allow a more accurate and easy-to-implement inclusion of angular-ordering constraints and mass effects, as well as to a better merging of multijet ME's with the shower

# Multiple emission



$$\operatorname{Prob}(Q_0 o Q_1) = P_0 \frac{\alpha_s}{2\pi} \int_{Q_1}^{Q_0} \frac{dq^2}{q^2} dz P(z) d\phi$$

$$Prob(Q_{0} \to Q_{1} \to Q_{2}) = P_{0} \frac{\alpha_{s}}{2\pi} \int_{Q_{1}}^{Q_{0}} \frac{dq^{2}}{q^{2}} dz P(z) d\phi \frac{\alpha_{s}}{2\pi} \int_{Q_{2}}^{Q_{1}} \frac{dq^{2}}{q^{2}} dz P(z) d\phi \\ \sim P_{0} \frac{1}{2!} \left[ \frac{\alpha_{s}}{2\pi} \int_{Q_{2}}^{Q_{0}} \frac{dq^{2}}{q^{2}} dz P(z) d\phi \right]^{2}$$

$$\operatorname{Prob}(Q_0 \to X) = P_0 \times \sum \frac{1}{n!} \left[ \frac{\alpha_s}{2\pi} \int_{\Lambda}^{Q_0} \frac{dq^2}{q^2} dz P(z) d\phi \right]^n = 1 \qquad \Lambda = \operatorname{infrared cutoff}$$



$$P_0 = \exp\{-\frac{\alpha_s}{2\pi} \int_{\Lambda}^{Q_0} \frac{dq^2}{q^2} dz P(z) d\phi\}$$

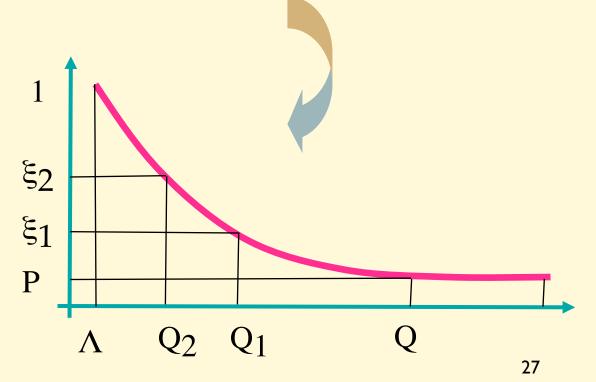
 $P_0$  = Sudakov form factor ~ probability of no emission between the scale  $Q_0$  and  $\Lambda$ 

# Generation of splittings

$$P(Q,\Lambda) = exp\left[-\int_{\Lambda}^{Q} \frac{dq^{2}}{q^{2}} \frac{\alpha_{s}(q)}{2\pi} P(z)dz\right]$$

**(** 

prob. of no radiation between Q and  $\Lambda$ 



I.Generate  $0 < \xi_1 < 1$ 

2.If  $\xi_1 < P(Q, \Lambda) \Rightarrow$  no radiation, q' goes directly on-shell at scale  $\Lambda \approx GeV$ 

3.Else

1.calculate  $Q_1$  such that  $P(Q_1, \Lambda) = \xi_1$ 

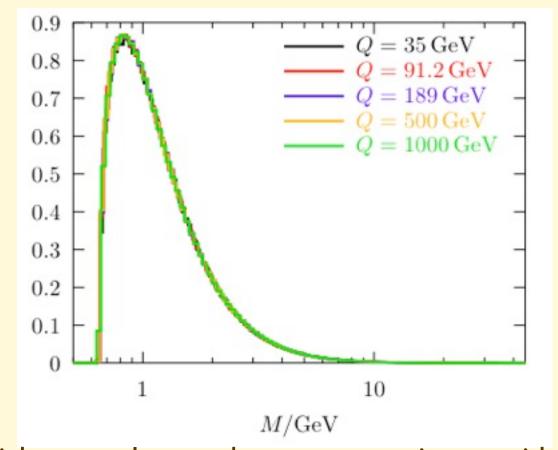
2.emission at scale Q<sub>1</sub>:



4. Select z according to P(z)

5.Reconstruct the full kinematics of the splitting

6.Go back to 1) and reiterate, until shower stops in 2). At each step the probability of emission gets smaller and smaller



The existence of high-mass clusters, however rare, is unavoidable, due to IR cutoff which leads to a non-zero probability that no emission takes place. This is particularly true for evolution of massive quarks (as in, e.g.  $Z \rightarrow bb$  or cc). Prescriptions have to be defined to deal with the "evolution" of these clusters. This has an impact on the  $z \rightarrow t$  behaviour of fragmentation functions.

Phenomenologically, this leads to uncertainties, for example, in the background rates for  $H \rightarrow \gamma \gamma$  (jet  $\rightarrow \gamma$ ).

This approach is						
This approach is	All charged	M, A, D, L, O	20.924 ± 0.117	20.22*	20.814	20.532*
extremely						
successful in	γ	A, O	21.27 ± 0.6	23.03	22.67	20.74
	π <sup>0</sup>	A, D, L, O	9.59 ± 0.33	10.27	10.08	9.88
describing the	ρ(770) <sup>0</sup> π <sup>±</sup>	A, D	$1.295 \pm 0.125$	1.235	1.316	1.07
properties of	ρ(770) <sup>±</sup>	A, O O	$17.04 \pm 0.25$ $2.4 \pm 0.43$	16.30 1.99	16.95 2.14	16.74 2.06
		A, L, O	$0.956 \pm 0.049$	0.886	0.893	0.669*
hadronic final	η ω(782)	A, L, O	$1.083 \pm 0.088$	0.859	0.916	1.044
states!	η(958)	A, L, O	$0.152 \pm 0.03$	0.13	0.136	0.106
states.						
Ex:	K <sup>0</sup>	S, A, D, L, O	$2.027 \pm 0.025$	2.121*	2.062	2.026
	K*(892)0	A, D, O	$0.761 \pm 0.032$	0.667	0.681	0.583*
Particle multiplicities:	K*(1430)°	D, O	$0.106 \pm 0.06$	0.065	0.079	0.072
	K ±	A, D, O	$2.319 \pm 0.079$	2.335	2.286	2.250
	K*(892) <sup>±</sup>	A, D, O	$0.731 \pm 0.058$	0.637	0.657	0.578
	φ(1020)	A, D, O	$0.097 \pm 0.007$	0.107	0.114	0.134*
	p	A, D, O	$0.991 \pm 0.054$	0.981	0.947	1.027
	$^{p}_{\Delta^{++}}$	D, O	$0.088 \pm 0.034$	0.185	0.092	0.209*
	$\Sigma^-$	0	$0.083 \pm 0.011$	0.063	0.071	0.071
	Λ	A, D, L, O	$0.373 \pm 0.008$	0.325*	0.384	0.347*
	$\Sigma^0$	A, D, O	$0.074 \pm 0.009$	0.078	0.091	0.063
	$\Sigma^+$	O	$0.099 \pm 0.015$	0.067	0.077	0.088
	$\Sigma(1385)^{\pm}$	A, D, O	$0.0471 \pm 0.0046$	0.057	0.0312*	0.061*
	Ξ-	A, D, O	$0.0262 \pm 0.001$	0.024	0.0286	0.029
	$\Xi(1530)^0$	A, D, O	$0.0058 \pm 0.001$	0.026*	0.0288*	0.009*
	$\Omega^-$	A, D, O	$0.00125 \pm 0.00024$	0.001	0.00144	0.0009*
	f <sub>2</sub> (1270)	D, L, O	$0.168 \pm 0.021$	0.113	0.150	0.173
	f <sub>2</sub> '(1525)	D	$0.02 \pm 0.008$	0.003	0.012	0.012
	$\mathbf{D}^{\pm}$	A, D, O	$0.184 \pm 0.018$	0.322*	0.319*	0.283*
	D*(2010)*	A, D, O	$0.182 \pm 0.009$	0.168	0.180	0.151*
	$D^0$	A, D, O	$0.473 \pm 0.026$	0.625*	0.570*	0.501
	$D_s^{\pm}$	A, O	$0.129 \pm 0.013$	0.218*	0.195*	0.127
	$D_s^{\pm}$ $D_s^{*\pm}$	O	$0.096 \pm 0.046$	0.082	0.066	0.043
	$J/\Psi$	A, D, L, O	$0.00544 \pm 0.00029$	0.006	0.00361*	0.002*
	$\Lambda_{\rm c}^+$	D, O	$0.077 \pm 0.016$	0.006*	0.023*	0.001*
	$\Psi'(3685)$	D, L, O	$0.00229 \pm 0.00041$	0.001*	0.00178	0.0008*
	* Indicates a prediction	that differs from the meas	sured value by more than	three standard deviation	s.	
Tabl 1. Average particle multiplicities per event in e <sup>+</sup> e <sup>-</sup> collisions at 91.2 GeV. Experimental data were measured by the following collaborations at LEP and at SLC: ALEPH(A), DELPHI(D), L3(L), OPAL(O), MARK2(M), and SLD(S). The theoretical predictions in the last three columns, taken from Ref. [30] correspond to various implementations of the cluster hadronization model (see Ref. [30] for details).						

Measured

Old model

Herwig (C++)

Herwig (Fortran)

Experiment

Particle

Ref. [30], correspond to various implementations of the cluster hadronization model (see Ref. [30] for details).

Gieseke S et al. JHEP (02) 005 (2004) 30.

#### **Ex: Energy distributions**

(Winter, Krauss, Soff, hep-ph/03 I 1085)

